

Lecture II: Neutrino Mass Models in Context

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U Mass Amherst



AMHERST CENTER FOR FUNDAMENTAL INTERACTIONS

Physics at the interface: Energy, Intensity, and Cosmic frontiers

University of Massachusetts Amherst

<http://www.physics.umass.edu/acfi/>

ACFI NLDBD School
10/31-11/3 2017

Lecture II Goals

- *Provide broader BSM context for $0\nu\beta\beta$ decay*
- *Provide a simple overview of classes of neutrino mass models with example illustrations*
- *Discuss implications for the interpretation of $0\nu\beta\beta$ decay searches*
- *Invite questions !*

Lecture II Outline

- I. The BSM Context*
- II. $0\nu\beta\beta$ -decay: General Considerations*
- III. Neutrino Mass Models*
- IV. Implications for $0\nu\beta\beta$ -decay*

I. The BSM Context

Fundamental Questions

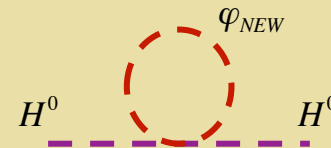
***MUST** answer*

***SHOULD** answer*

Fundamental Questions

MUST answer

SHOULD answer



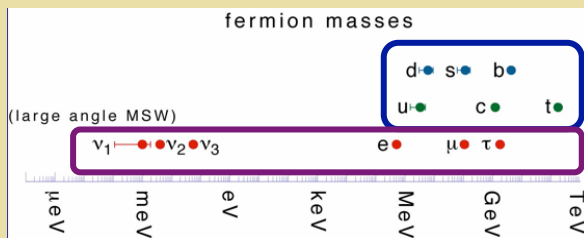
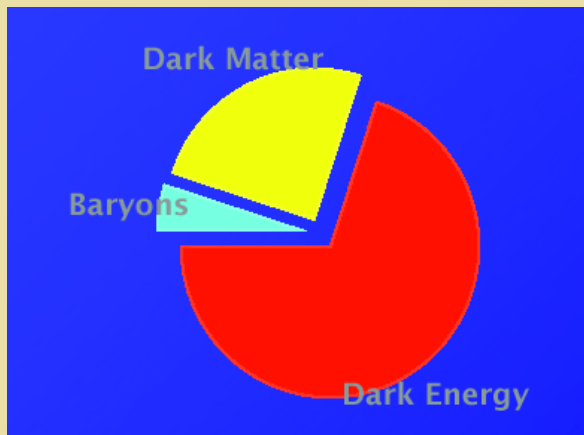
$\Delta m^2 \sim \lambda \Lambda^2$

Λ Cosmological

θ_{QCD} , parity, unification...

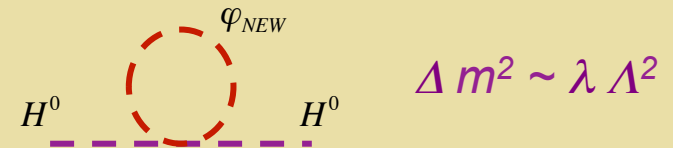
Fundamental Questions

MUST answer



*Origin of m_ν
flavor...*

SHOULD answer



Λ *Cosmological*

θ_{QCD} , parity, unification...

Naturalness Problem

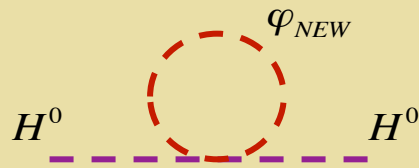
Scalar Fields in Particle Physics



Scalar Fields in Particle Physics

Scalar fields are a simple

Scalar fields are theoretically problematic



$$\Delta m^2 \sim \lambda \Lambda^2$$

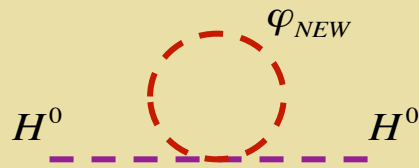
Discovery of a (probably) fundamental 125 GeV scalar :

Is it telling us anything about Λ ? Naturalness?

Scalar Fields in Particle Physics

Scalar fields are a simple

Scalar fields are theoretically problematic



$$\Delta m^2 \sim \lambda \Lambda^2$$

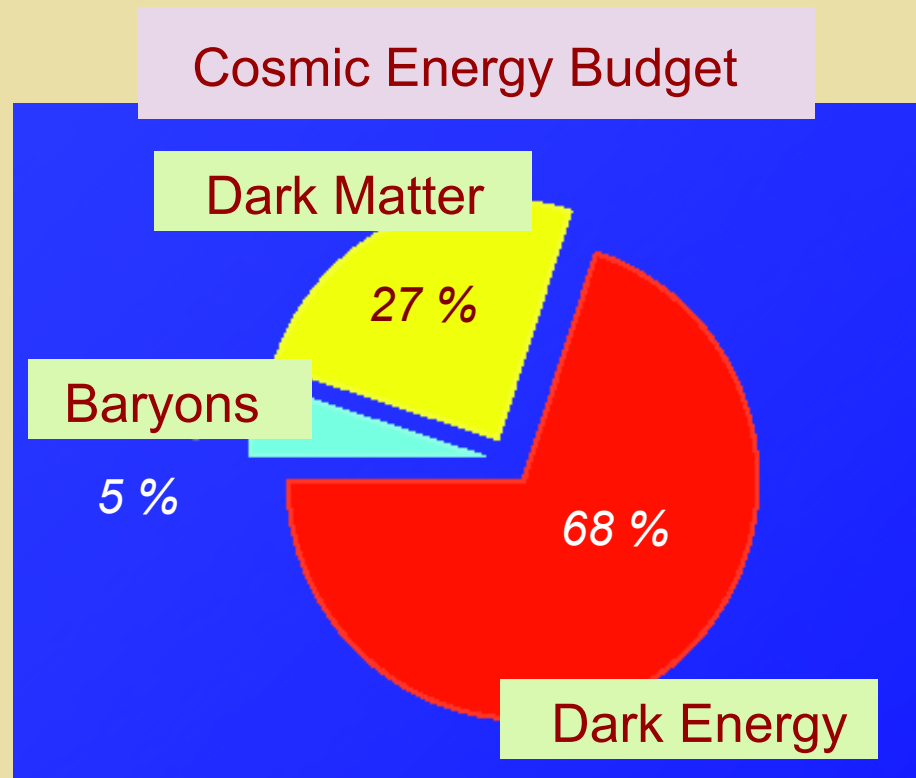
Discovery of a (probably) fundamental 125 GeV scalar :

$$m_h^2 \sim \lambda v^2 \text{ \& } G_F \sim 1/v^2 : \text{ what keeps } G_F \text{ "large" ?}$$

LHC Implications

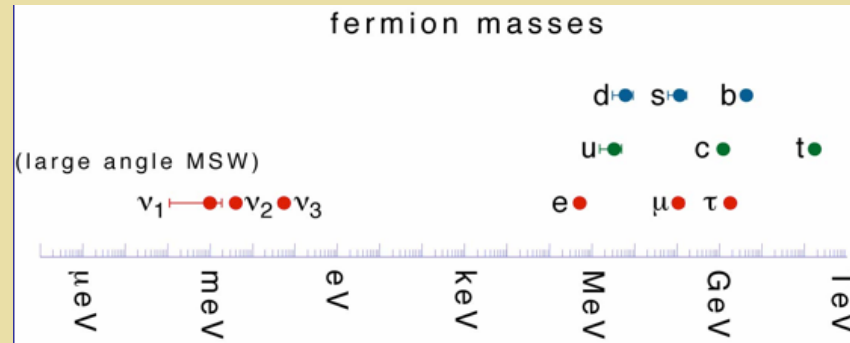
- *Weak scale BSM physics (e.g., SUSY) is there but challenging for the hadronic collider*
- *BSM physics is there but a bit heavy (some fine tuning)*
- *We are thinking about the problem incorrectly (cosmological constant???)*

The Origin of Matter

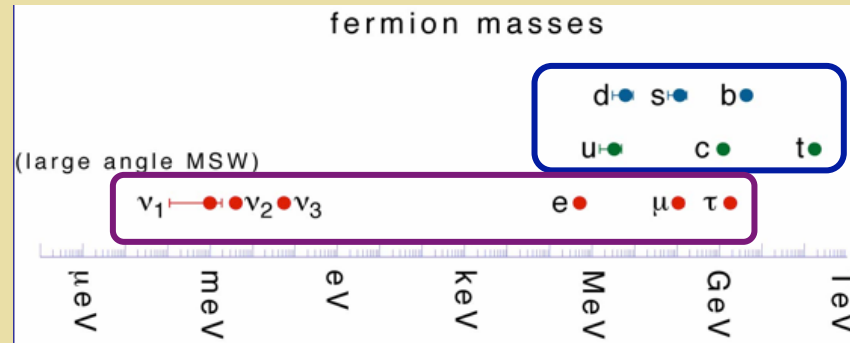


Explaining the origin, identity, and relative fractions of the cosmic energy budget is one of the most compelling motivations for physics beyond the Standard Model

Neutrino Masses



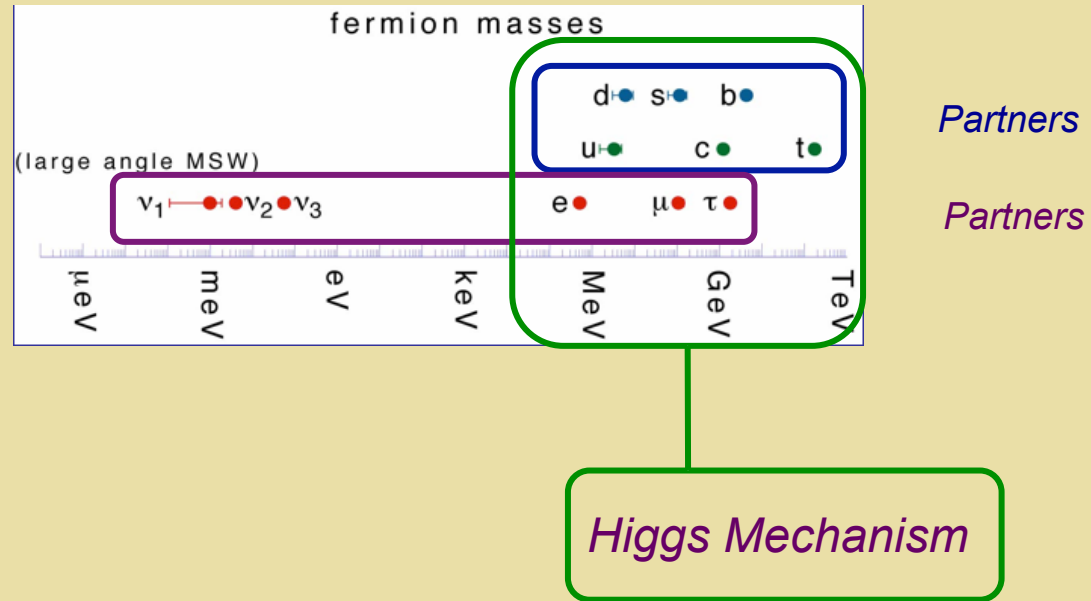
Neutrino Masses



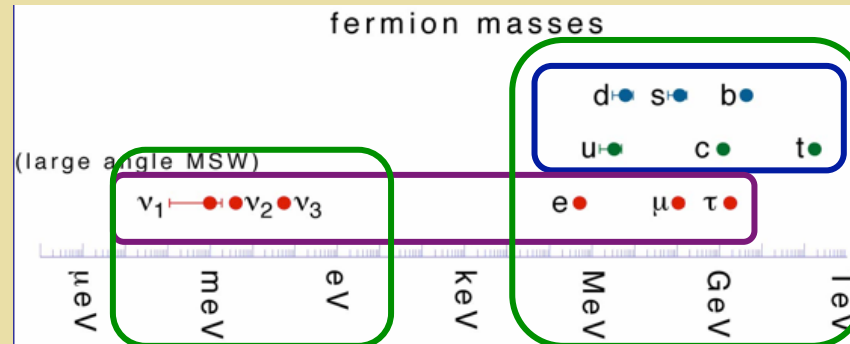
Partners

Partners

Neutrino Masses



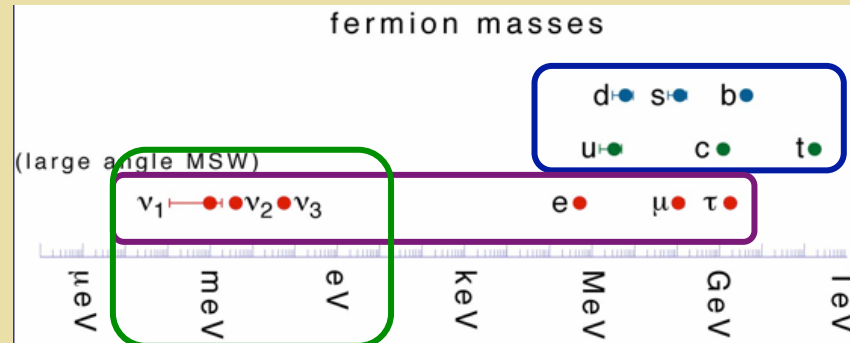
Neutrino Masses



Something else ?

Higgs Mechanism

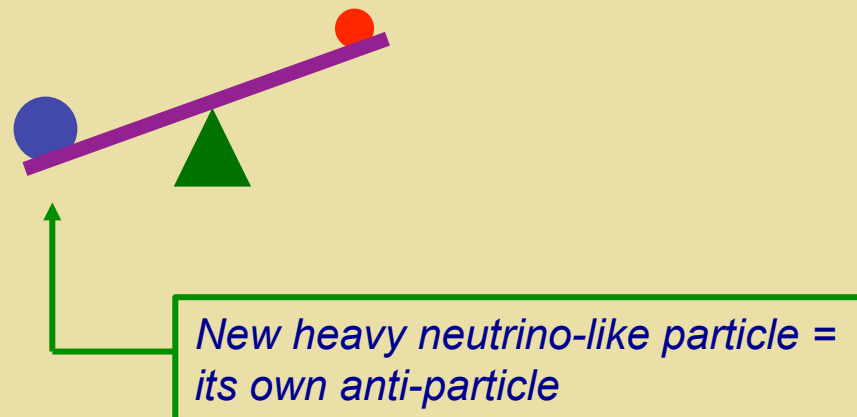
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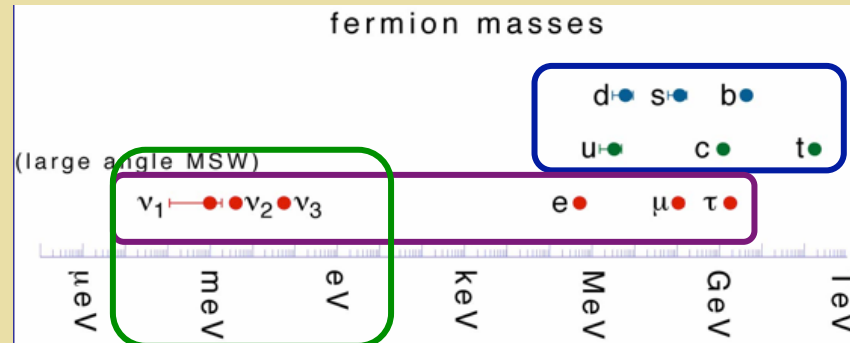
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“See saw mechanism”



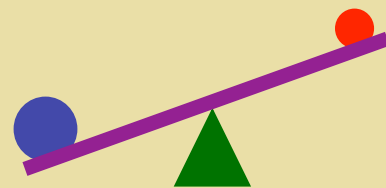
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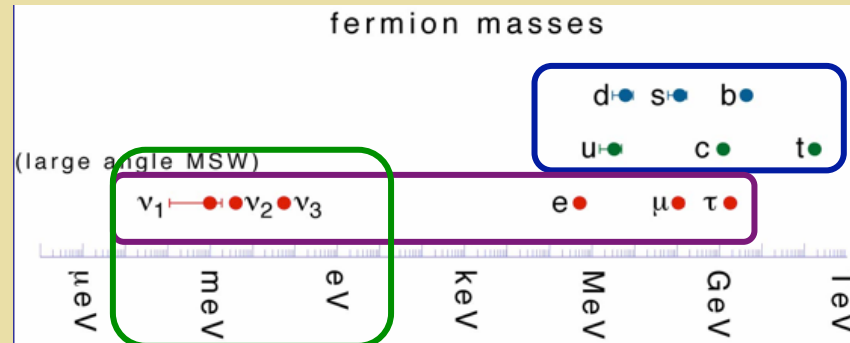
Physical state masses

$$m_1 \approx \frac{m_D^2}{M_N} \quad \sim eV$$

$$m_2 \approx M_N \quad \sim 10^{12} - 10^{15} \text{ GeV}$$

New heavy neutrino-like particle =
its own anti-particle

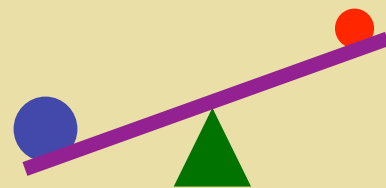
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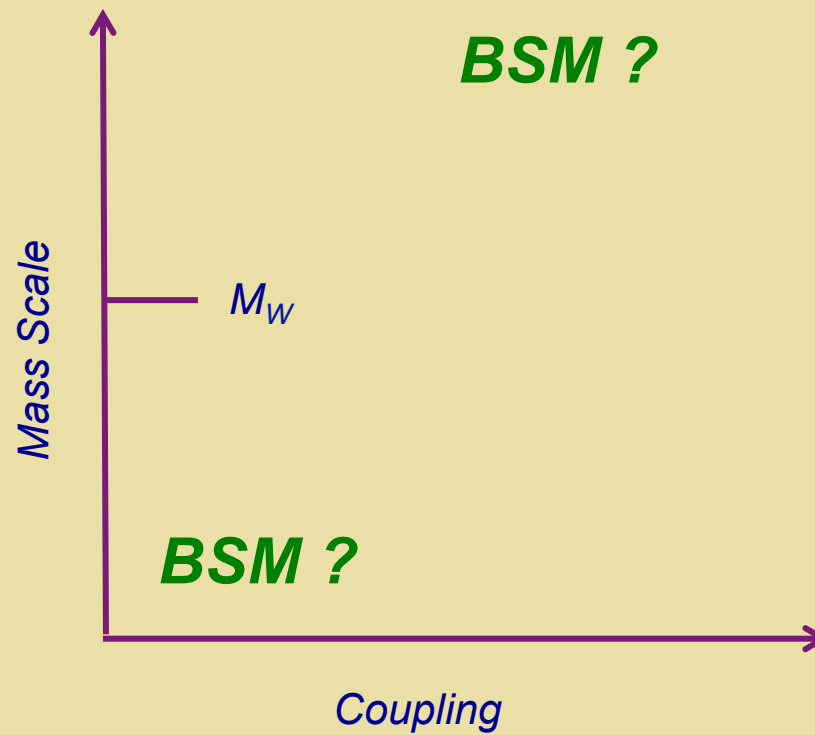


“Leptogenesis”

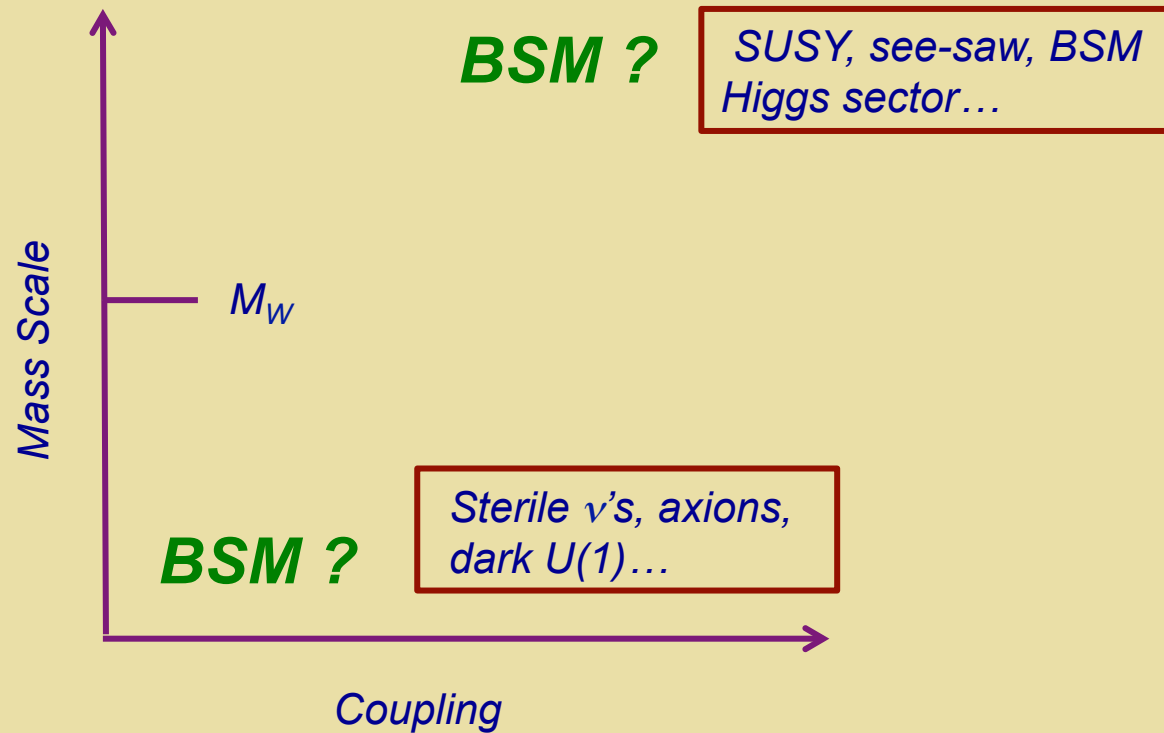
Heavy neutrino decays in early universe generate baryon asym

New heavy neutrino-like particle = its own anti-particle

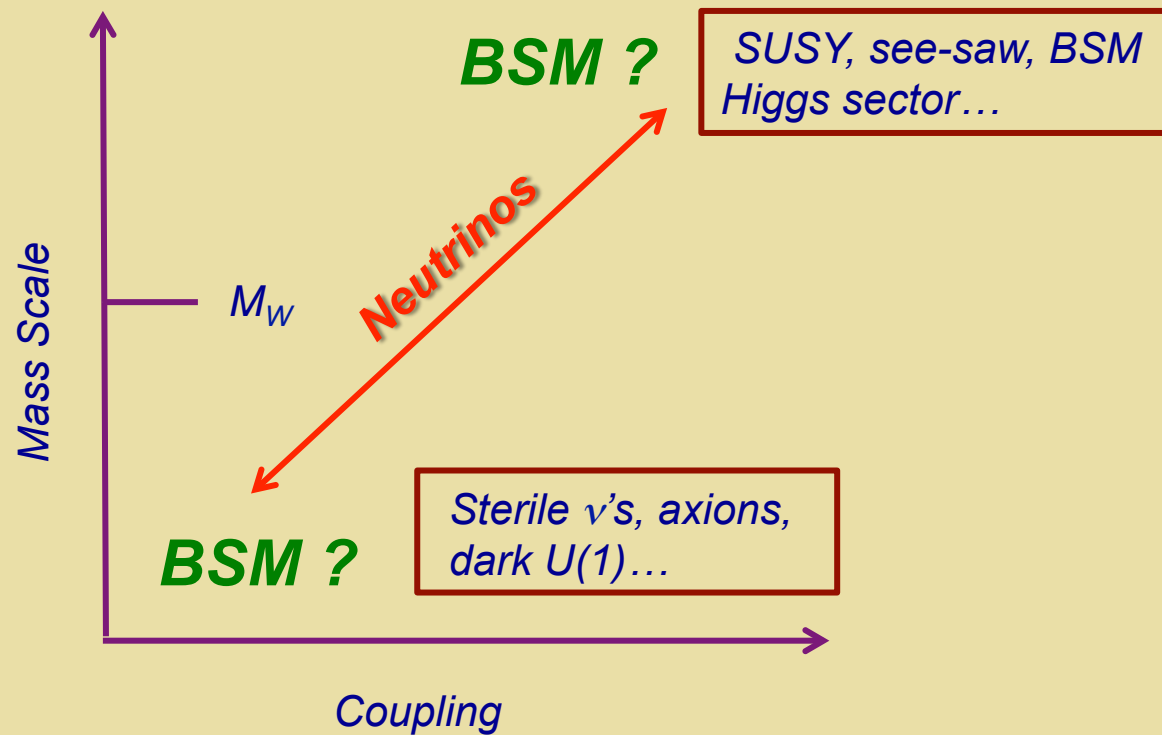
BSM Physics: Where Does it Live ?



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II. $0\nu\beta\beta$ -Decay: General Considerations

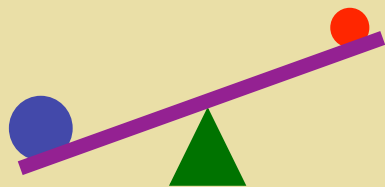
What Questions Does It Address ?

- *Is the neutrino its own antiparticle ?*
- *Why is there more matter than antimatter ?*
- *Why are neutrino masses so small?*

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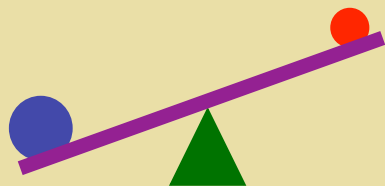
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- *Why are neutrino masses so small?*

“See saw mechanism”



“Leptogenesis”

$$\nu = \bar{\nu}$$

Heavy neutrino decays in early universe generate baryon asym

New heavy neutrino-like particle = its own anti-particle

Neutrinos and the Origin of Matter

- *Heavy neutrinos decay out of equilibrium in early universe*
- *Majorana neutrinos can decay to particles and antiparticles*
- *Rates can be slightly different (CP violation)*

$$\Gamma(N \rightarrow \ell H) \neq \Gamma(N \rightarrow \bar{\ell} H^*)$$

- *Resulting excess of leptons over anti-leptons partially converted into excess of quarks over anti-quarks by Standard Model sphalerons*

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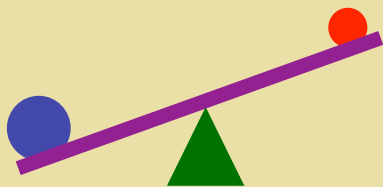
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Physical state masses

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III. Neutrino Mass Models

- *Type I see-saw* “ ν SM”, “ ν MSSM”
- *Type II see-saw* LRSM
- *Type III see-saw* GUTs
- *Inverse see-saw* LRSM
- *Radiative* MSSM

+ combinations & many other examples

$0\nu\beta\beta$ -Decay: LNV? Mass Term?

$$\mathcal{L}_{\text{mass}} = y\bar{L}\tilde{H}\nu_R + \text{h.c.}$$

Dirac

$$\mathcal{L}_{\text{mass}} = \frac{y}{\Lambda}\bar{L}^c H H^T L + \text{h.c.}$$

Majorana

Neutrino Mass Models

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$0\nu\beta\beta$ -Decay: Type I See-Saw

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Dirac

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Majorana

One generation: SM + one N_R

$$\mathcal{L}_{\text{mass}} = y\bar{L}\tilde{H}N_R + \text{h.c.} + M_N\bar{N}_R^C N_R$$



$$\mathcal{L}_{\text{mass}} = \left(\bar{\nu}_L \quad \bar{N}_R^C \right) \begin{pmatrix} 0 & m_D \\ m_D & M_N \end{pmatrix} \begin{pmatrix} \nu_L \\ N_R \end{pmatrix}$$

$0\nu\beta\beta$ -Decay: Type I See-Saw

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Lepton number violating

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Eigenvalues

$$m_1 \approx \frac{m_D^2}{M_N}$$

$$m_2 \approx M_N$$

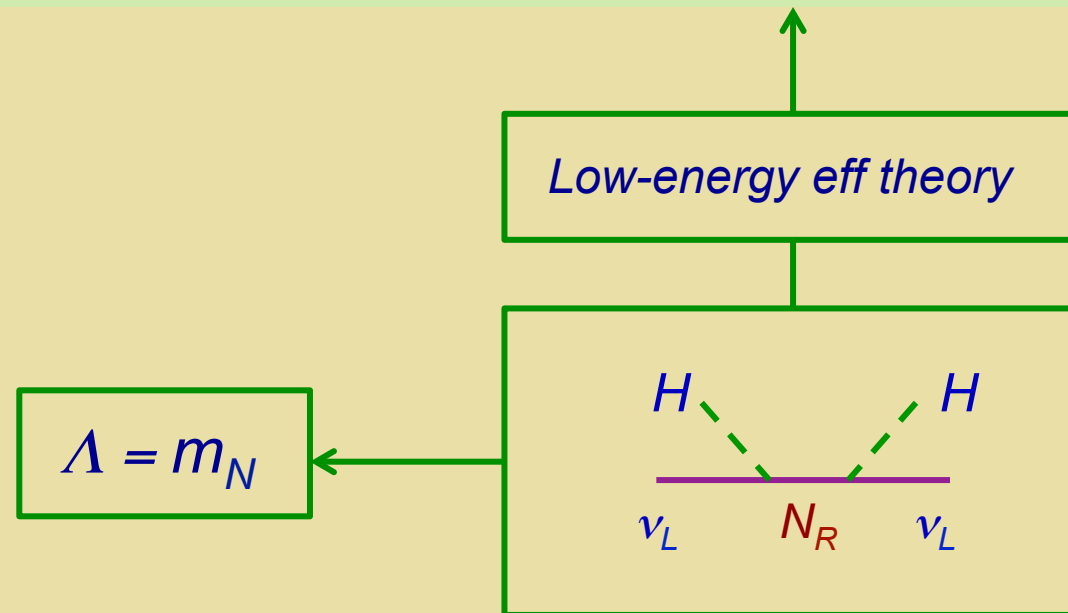
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Majorana

“ ν MSM”

ν MSM
Spin-1/2 fermions

Quarks	Left	u	c	t	Spin-1 bosons	g
	Right	d	s	b		γ
	Right	ν_1	ν_2	ν_3		Z^0
Leptons	Left	e	μ	τ	Force carriers	W^\pm
	Right					
	Right					

Spin-0 Higgs boson: H

Ann. Rev. Nucl. Part. Sci. 59, 191 (2009)

P. Mermoud

N_1 mass \sim keV
 \rightarrow dark matter

$N_{2,3}$ mass \sim GeV
 \rightarrow seesaw
 \rightarrow leptogenesis

“ ν MSSM”

The Standard Model of Particle Interactions

Three Generations of Matter

Leptons	I	II	III	Force Carriers	
	u	c	t		γ
	d	s	b		g
	ν_e	ν_μ	ν_τ		Z
	e	μ	τ	W	

The Minimal Supersymmetric Extension of the Standard Model (MSSM)

Sleptons	I	II	III	Gauginos	
	\tilde{u}	\tilde{c}	\tilde{t}		$\tilde{\gamma}$
	\tilde{d}	\tilde{s}	\tilde{b}		\tilde{g}
	$\tilde{\nu}_e$	$\tilde{\nu}_\mu$	$\tilde{\nu}_\tau$		\tilde{Z}
	\tilde{e}	$\tilde{\mu}$	$\tilde{\tau}$	\tilde{W}	

$$+ (N_R, \tilde{N}_R)$$

Neutrino Mass Models

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+ combinations & many other examples

$0\nu\beta\beta$ -Decay: Type II See-Saw

$$\mathcal{L}_{\text{mass}} = y\bar{L}\tilde{H}\nu_R + \text{h.c.}$$

Dirac

$$\mathcal{L}_{\text{mass}} = \frac{y}{\Lambda}\bar{L}^c H H^T L + \text{h.c.}$$

Majorana

Introduce “Complex Triplet”: $\Delta_L \sim (1, 3, 2)$

$$\Delta_L = \begin{pmatrix} \Delta^+\sqrt{2} & \Delta^+ \\ \Delta^0 & -\Delta^+\sqrt{2} \end{pmatrix}$$

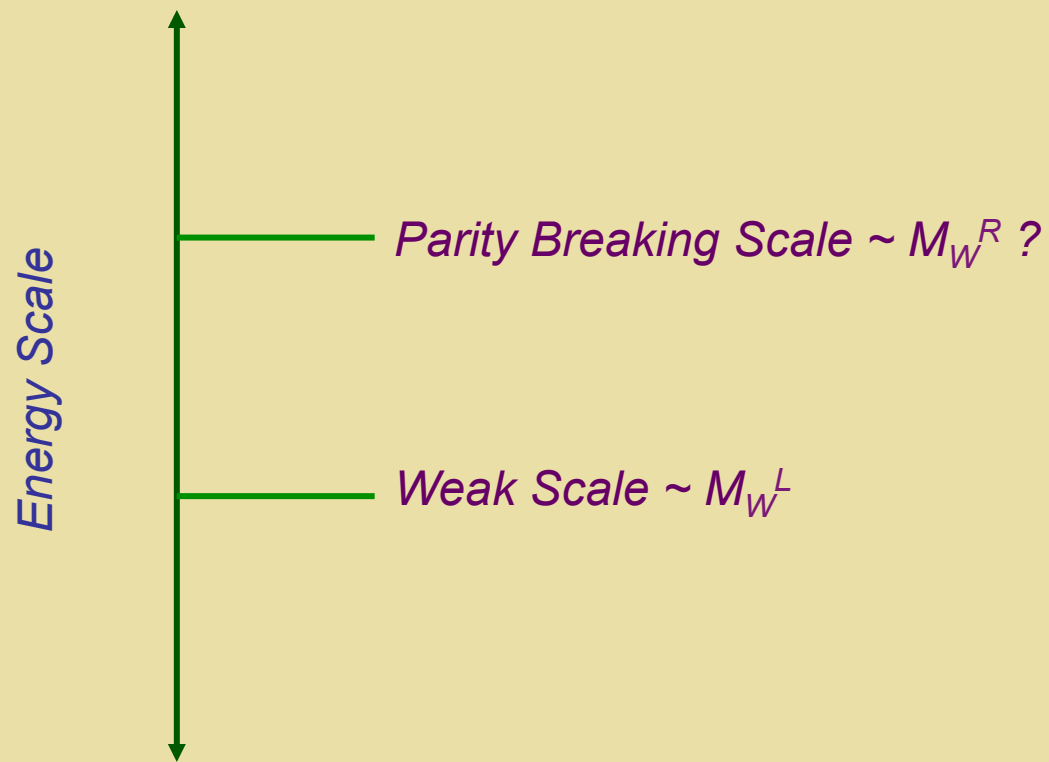
Δ^0 vev \rightarrow Majorana m_ν

$$\mathcal{L} = \frac{g}{2} h_{ij} [\bar{L}^c \varepsilon \Delta_L L^j] + \text{h.c.}$$

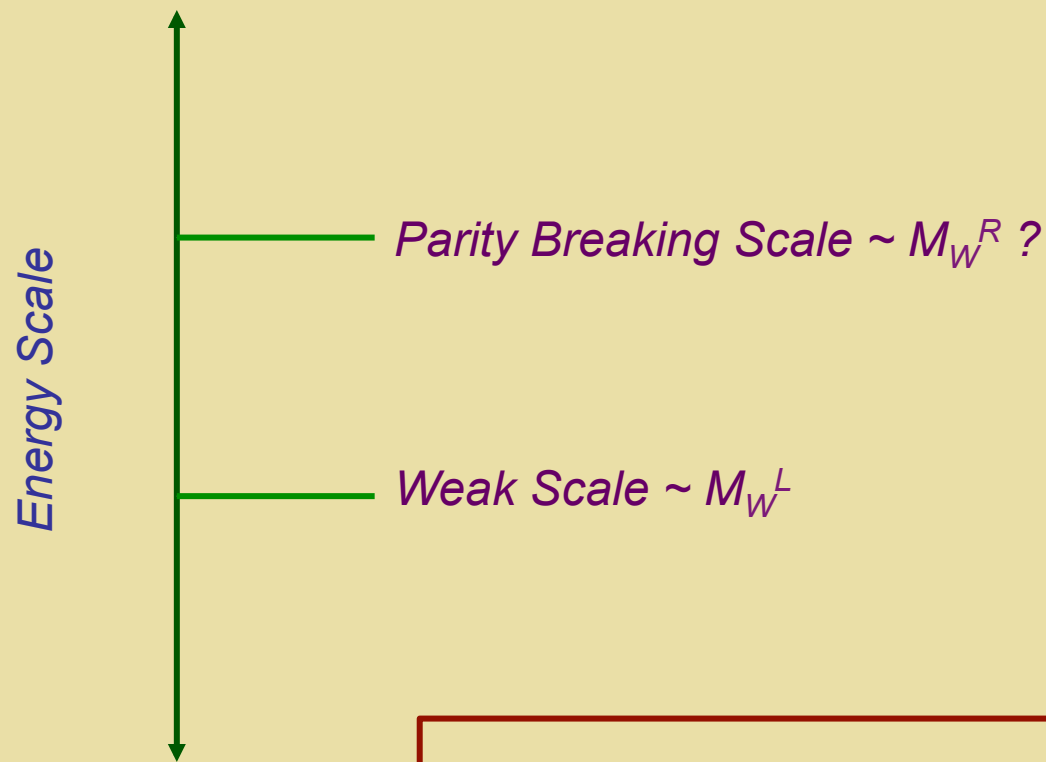
Lepton number violating

Left-Right Symmetric Model

BSM Mass Scale

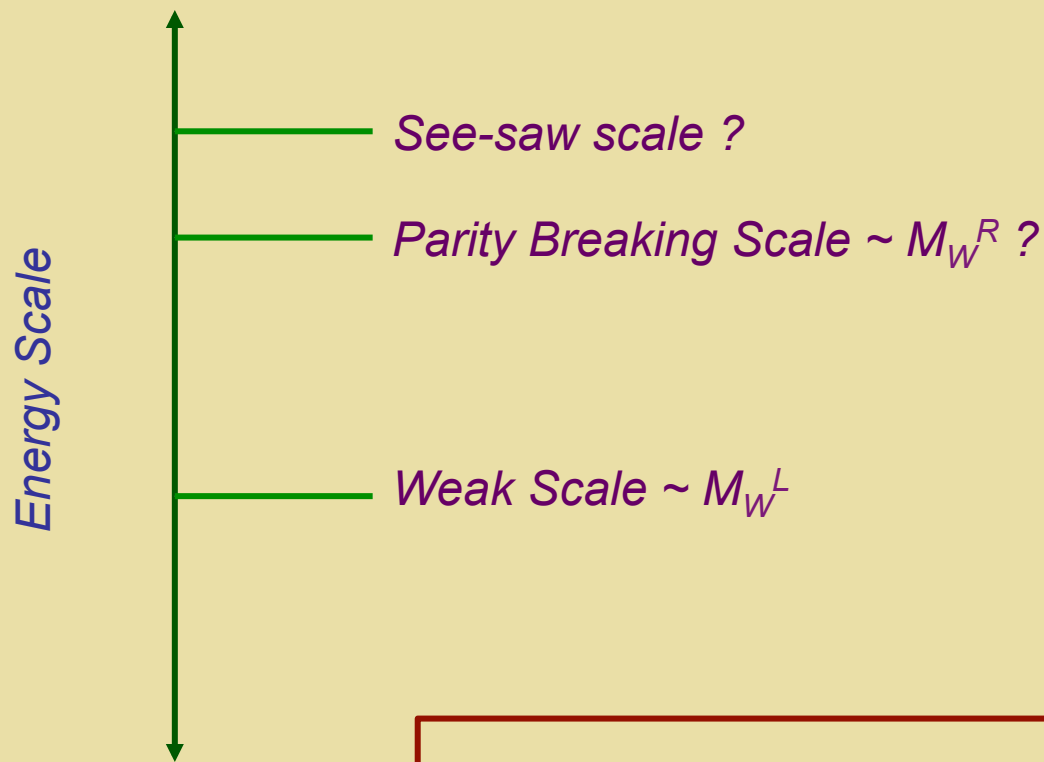


Left-Right Symmetric Model



$$SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

Left-Right Symmetric Model



$$SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

Left-Right Symmetric Model

Gauge boson mass eigenstates

$$\begin{aligned} W_1^+ &= \cos \xi W_L^+ + \sin \xi e^{-i\alpha} W_R^+ \\ W_2^+ &= -\sin \xi e^{i\alpha} W_L^+ + \cos \xi W_R^+ \end{aligned}$$

CKM Matrices for LH & RH sectors: quarks

$$\begin{aligned} u_{Li}^I &= (S_u)_{ij} u_{Lj}^{\text{mass}} \\ u_{Ri}^I &= (T_u)_{ij} u_{Rj}^{\text{mass}} \\ d_{Li}^I &= (S_d)_{ij} d_{Lj}^{\text{mass}} \\ d_{Ri}^I &= (T_d)_{ij} d_{Rj}^{\text{mass}} \end{aligned}$$

$$V_{\text{CKM}}^L = S_u^\dagger S_d$$

$$V_{\text{CKM}}^R = T_u^\dagger T_d$$

Left-Right Symmetric Model

Gauge boson mass eigenstates

$$\begin{aligned} W_1^+ &= \cos \xi W_L^+ + \sin \xi e^{-i\alpha} W_R^+ \\ W_2^+ &= -\sin \xi e^{i\alpha} W_L^+ + \cos \xi W_R^+ \end{aligned}$$

PMNS Matrices for LH & RH sectors: leptons

$$\begin{aligned} \nu_{Li}^I &= (S_\nu)_{ij} \nu_{Lj}^{\text{diag}} \\ N_{Ri}^I &= (T_N)_{ij} N_{Rj}^{\text{diag}} \\ \ell_{Li}^I &= (S_\ell)_{ij} \ell_{Lj}^{\text{diag}} \\ \ell_{Ri}^I &= (T_\ell)_{ij} \ell_{Rj}^{\text{diag}} \end{aligned}$$

$$V_{\text{PMNS}}^L = S_\nu^\dagger S_\ell$$

Left-Right Symmetric Model

Two sources of m_ν :

$$\mathcal{L} = \frac{g}{2} h_{ij} [\bar{L}^{Ci} \varepsilon \Delta_L L^j] + (L \leftrightarrow R) + \text{h.c.}$$

Type I see-saw

Type II see-saw

$$\mathcal{L}_{\text{mass}} = \left(\bar{\nu}_L \quad \bar{N}_R^C \right) \begin{pmatrix} 0 & m_D \\ m_D & M_N \end{pmatrix} \begin{pmatrix} \nu_L \\ N_R \end{pmatrix} + m_L \bar{\nu}_L^C \nu_L$$

$$m_N \sim g h_R \langle \Delta_R^0 \rangle$$

$$m_L \sim g h_L \langle \Delta_L^0 \rangle$$

Neutrino Mass Models

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- *Inverse see-saw* LRSM
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+ combinations & many other examples

$0\nu\beta\beta$ -Decay: Type III See-Saw

$$\mathcal{L}_{\text{mass}} = y \bar{L} \tilde{H} \nu_R + \text{h.c.}$$

Dirac

$$\mathcal{L}_{\text{mass}} = \frac{y}{\Lambda} \bar{L}^c H H^T L + \text{h.c.}$$

Majorana

Introduce “Fermionic Triplet”: $\Delta_L \sim (1, 3, 0)$

$$- \mathcal{L}_v^{\text{III}} = Y_v \ell_L \rho_L H + M_\rho \text{Tr} \rho_L^2 + \text{h.c.}$$

Like Type I but $N_R \rightarrow \rho_L$

See P. Fileviez Perez,
1501.01886

Neutrino Mass Models

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- *Inverse see-saw* LRSM
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+ *combinations & many other examples*

$0\nu\beta\beta$ -Decay: Inverse See-Saw

$$\mathcal{L}_{\text{mass}} = y \bar{L} \tilde{H} \nu_R + \text{h.c.}$$

Dirac

$$\mathcal{L}_{\text{mass}} = \frac{y}{\Lambda} \bar{L}^c H H^T L + \text{h.c.}$$

Majorana

Introduce “singlet” Majorana neutrino

$$\mathcal{L}_{\text{mass}} = \left(\bar{\nu}_L \quad \bar{N}_R \quad \bar{N}_S^C \right) \begin{pmatrix} 0 & m_D^L & 0 \\ m_D^L & 0 & M_D^R \\ 0 & M_D^R & \mu \end{pmatrix} \begin{pmatrix} \nu_L \\ N_R \\ N_S \end{pmatrix}$$

Singlet Majorana mass

$$m_\nu \sim m_D^L (M_D^R)^{-1} \mu (M_D^R)^{-1} m_D^L$$

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+ *combinations & many other examples*

$0\nu\beta\beta$ -Decay: Type II See-Saw

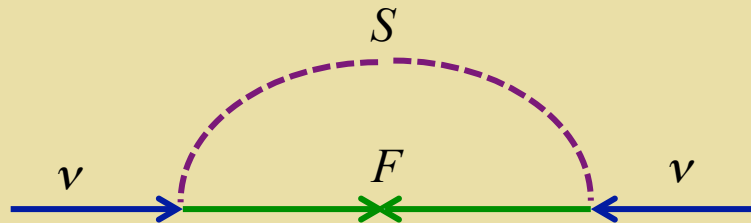
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Majorana

Introduce new scalars (S) & Majorana fermions (F): “mediators”



Attach Higgs lines as appropriate to get Weinberg operator

Recent mini-review: H. Sugiyama, 1505.01738

$0\nu\beta\beta$ -Decay: Type II See-Saw

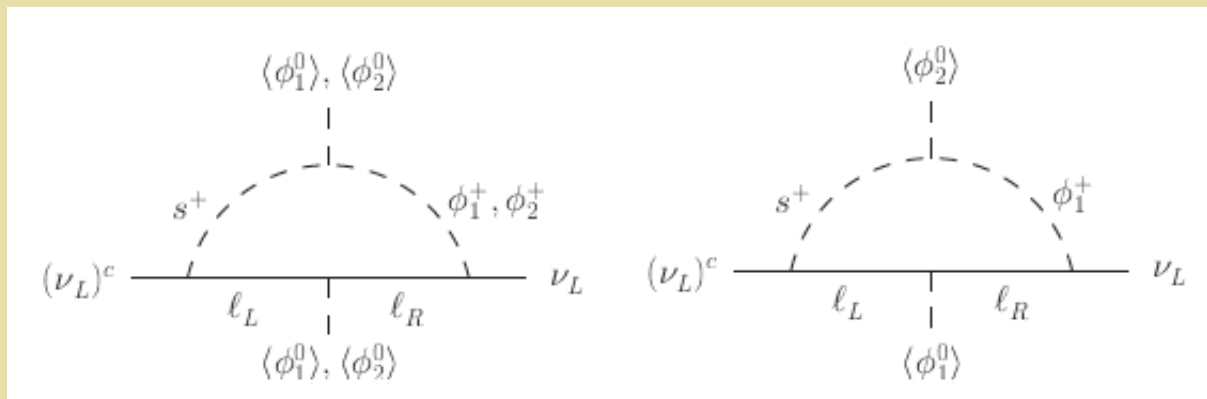
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“Zee Model”

Recent mini-review: H. Sugiyama, 1505.01738

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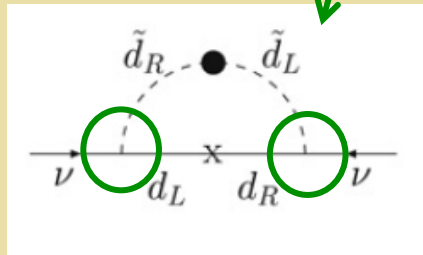
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Majorana

SUSY with “R parity” violation $P_R = (-1)^{2S+3(B-L)}$

“Superpotential”

$$W_{\Delta L=1} = \frac{1}{2}\lambda_{ijk}L_i L_j \bar{e}_k + \lambda'_{ijk}L_i Q_j \bar{d}_k + \mu'_i L_i H_u,$$



IV. Implications for $0\nu\beta\beta$ -Decay

$0\nu\beta\beta$ -Decay: LNV? Mass Term?

$$\mathcal{L}_{\text{mass}} = y\bar{L}\tilde{H}\nu_R + \text{h.c.}$$

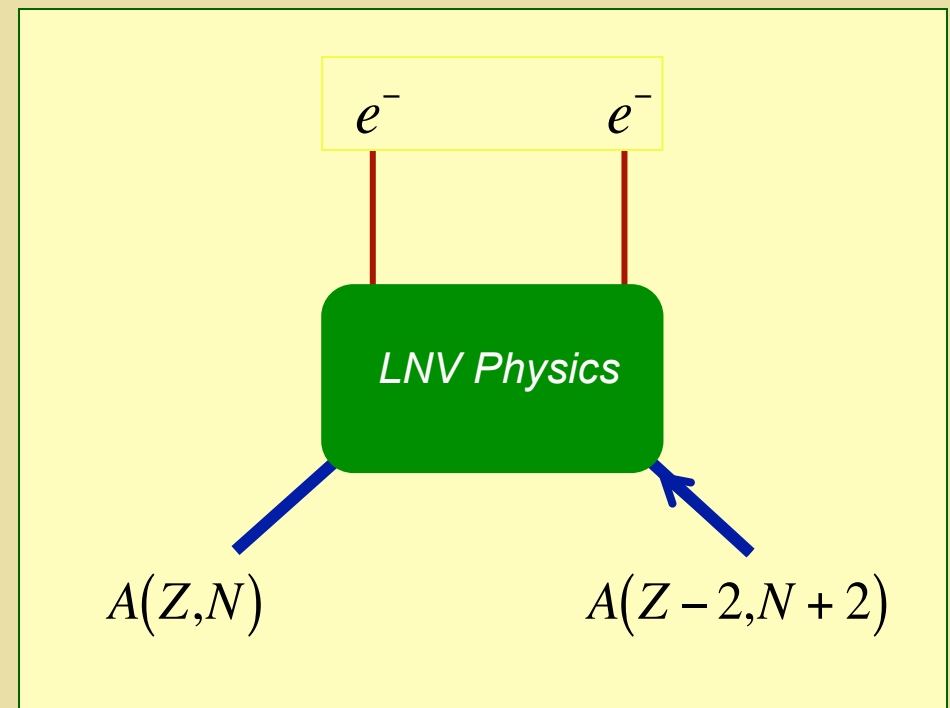
Dirac

$$\mathcal{L}_{\text{mass}} = \frac{y}{\Lambda}\bar{L}^c H H^T L + \text{h.c.}$$

Majorana

Impact of observation

- *Total lepton number not conserved at classical level*
- *New mass scale in nature, Λ*
- *Key ingredient for standard baryogenesis via leptogenesis*



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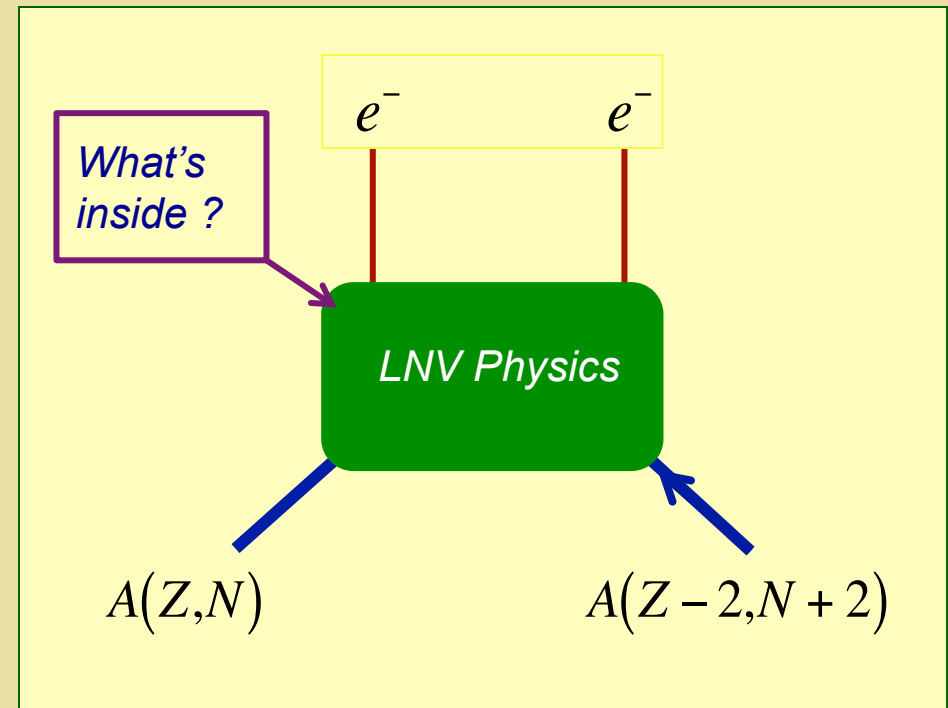
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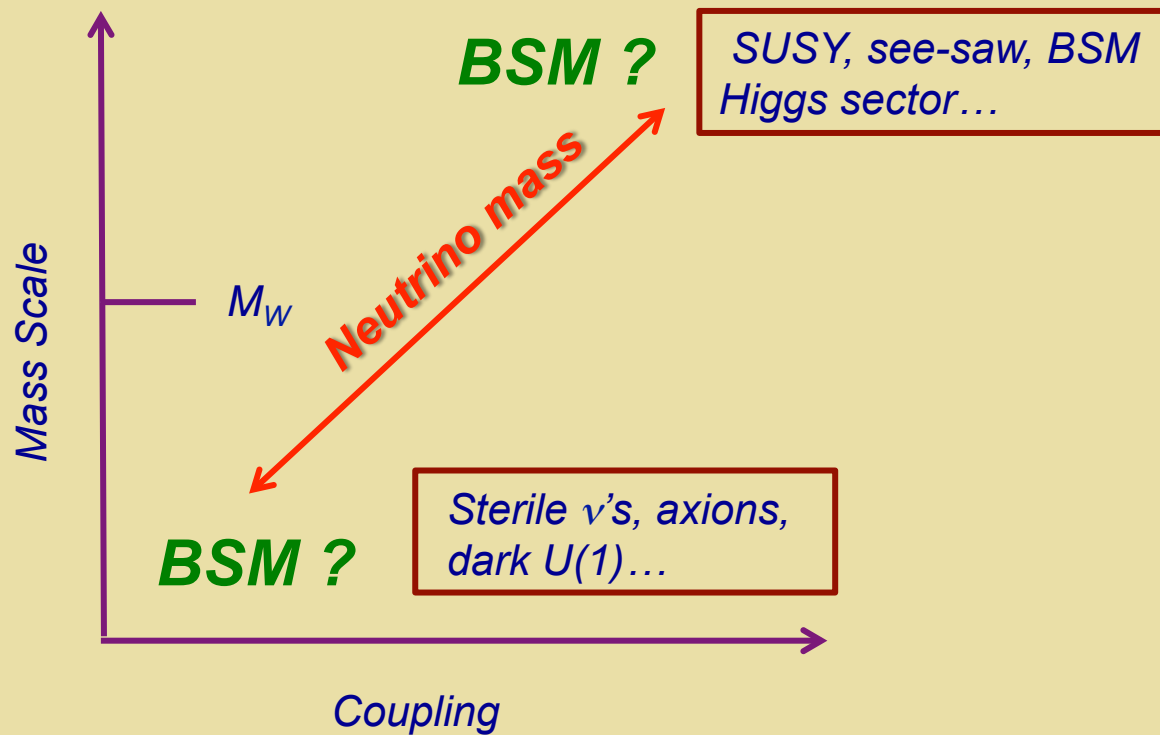
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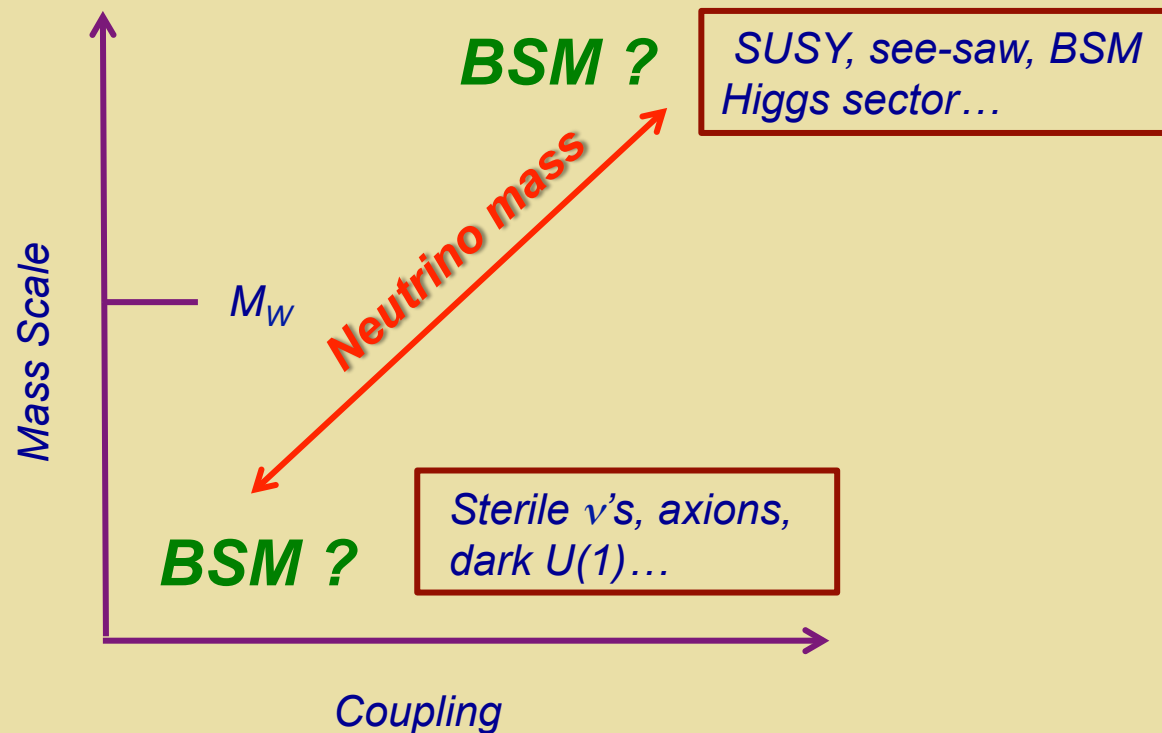
- Total lepton number not conserved at classical level
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- Key ingredient for standard baryogenesis via leptogenesis



BSM Physics: Where Does it Live ?



BSM Physics: Where Does it Live ?



Is the mass scale associated with m_ν far above M_W ? Near M_W ? Well below M_W ?

LVN Mass Scale & $0\nu\beta\beta$ -Decay



- *3 light neutrinos only: source of neutrino mass at the very high see-saw scale*
- *3 light neutrinos with TeV scale source of neutrino mass*
- *> 3 light neutrinos*

LVN Mass Scale & $0\nu\beta\beta$ -Decay



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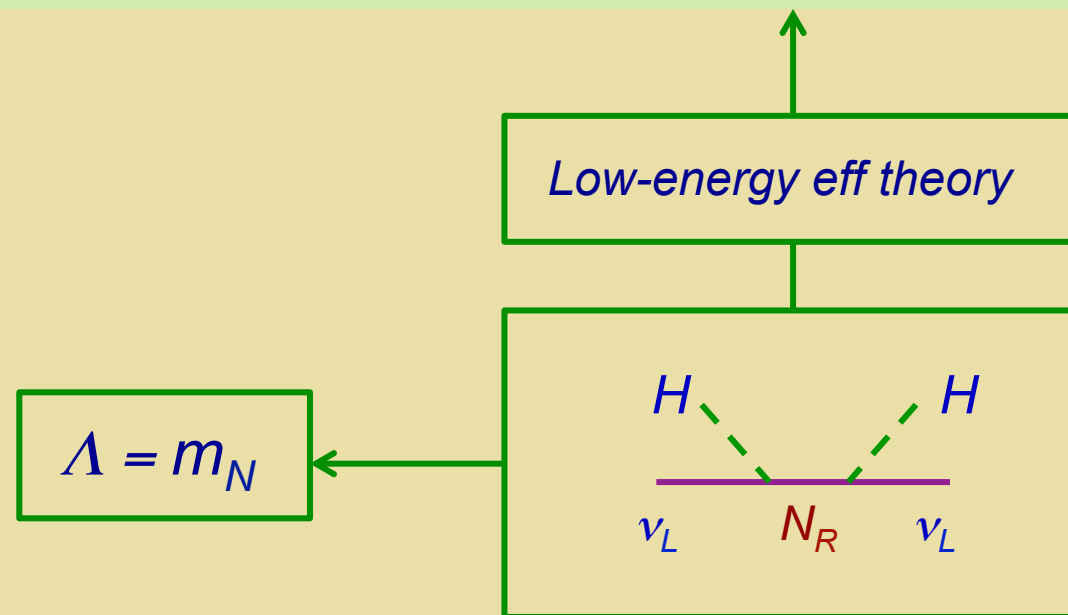
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Majorana



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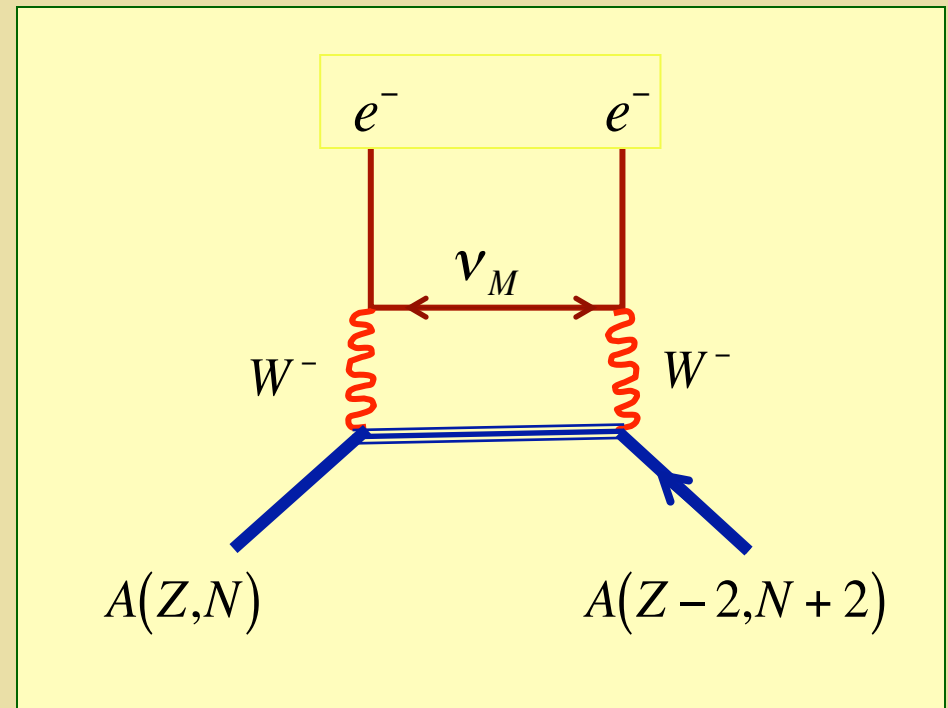
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Majorana

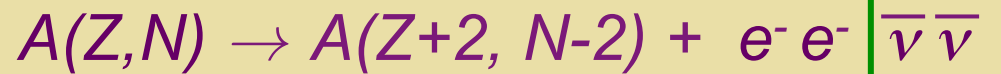
“Standard” Mechanism

- Light Majorana mass generated at the conventional see-saw scale: $\Lambda \sim 10^{12} - 10^{15}$ GeV
- 3 light Majorana neutrinos mediate decay process



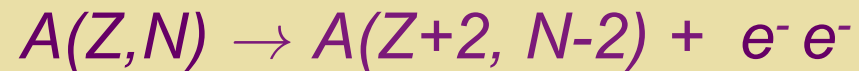
Three Light Neutrinos: What Do We Know ?

2ν DBD:



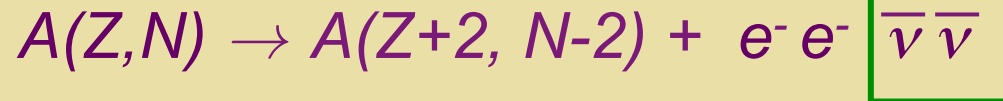
If own antiparticle, can be emitted then absorbed during decay

0ν DBD:



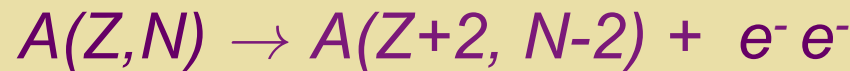
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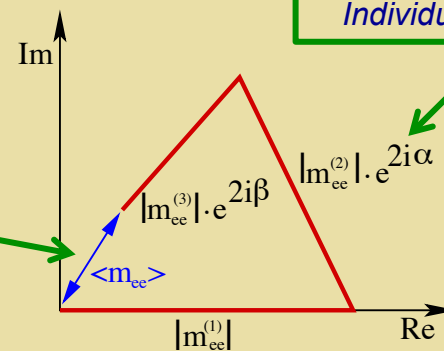


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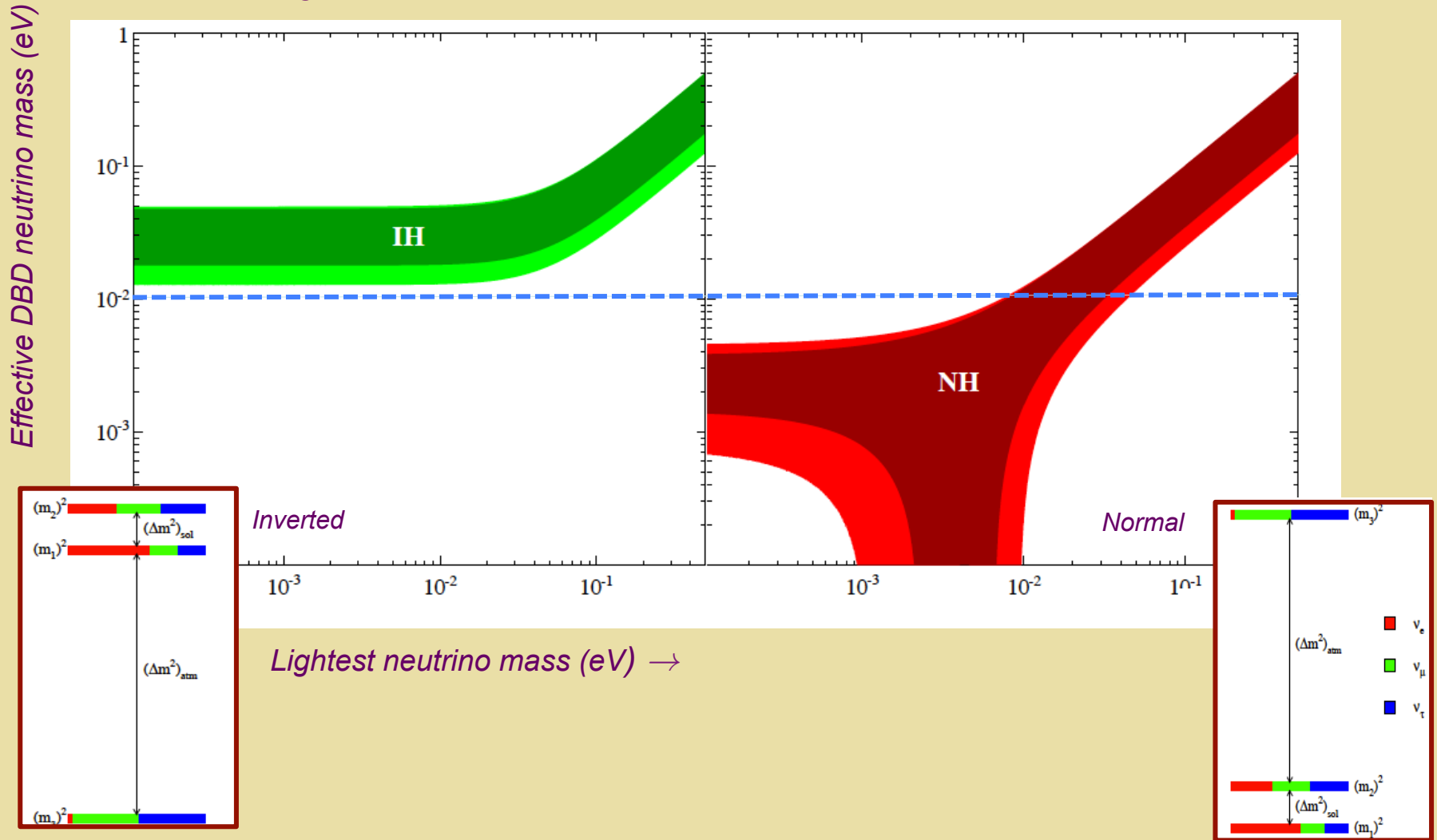


All three light neutrinos participate \rightarrow
Rate governed by an **effective mass**



Why Might A “Ton-Scale” Exp’t See It?

Three active light neutrinos



LN_V Mass Scale & $0\nu\beta\beta$ -Decay



- *3 light neutrinos only: source of neutrino mass at the very high see-saw scale*
- *3 light neutrinos with TeV scale source of neutrino mass*
- *> 3 light neutrinos*

Two parameters: Effective coupling & effective heavy particle mass

$0\nu\beta\beta$ -Decay: LNV? Mass Term?

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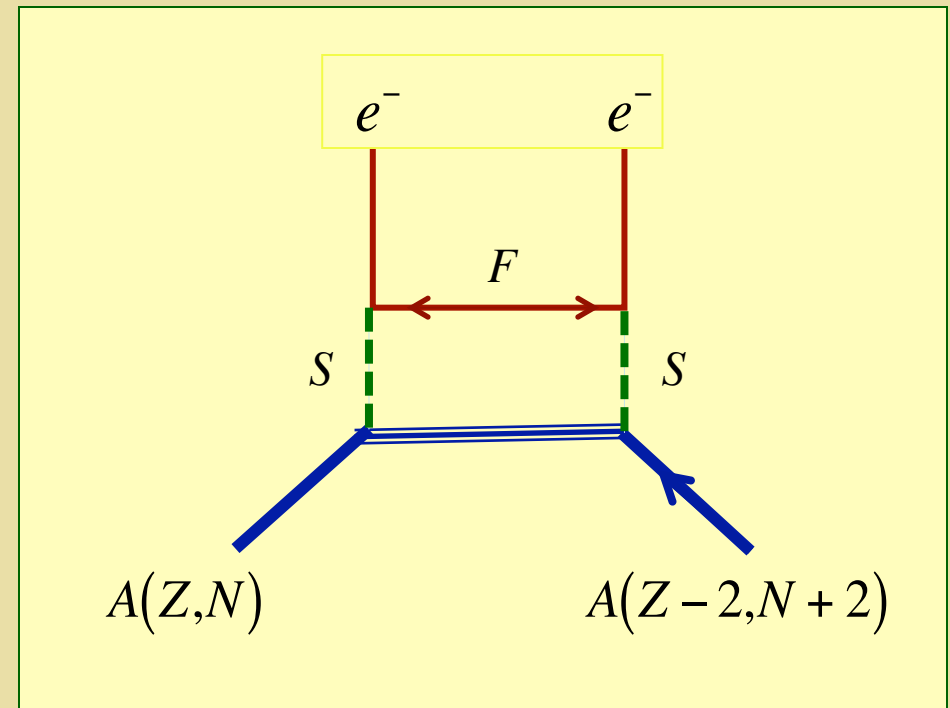
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Majorana

TeV LNV Mechanism

- Majorana mass generated at the TeV scale
- Low-scale see-saw
- Radiative m_ν
- $m_{\text{MIN}} \ll 0.01 \text{ eV}$ but $0\nu\beta\beta$ -signal accessible with tonne-scale exp'ts due to heavy Majorana particle exchange



$0\nu\beta\beta$ -Decay: LNV? Mass Term?

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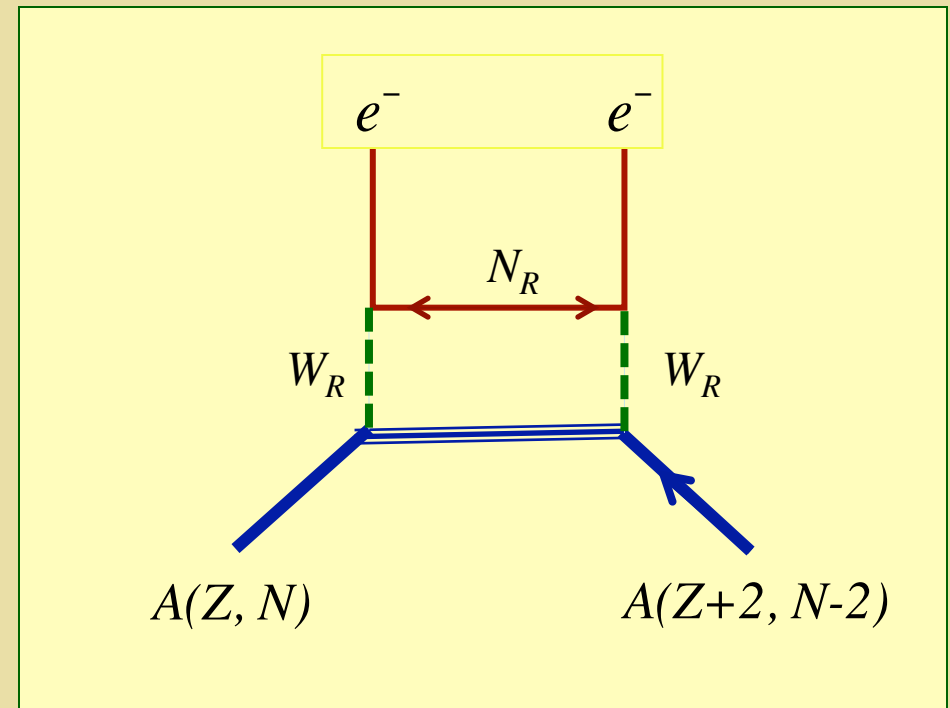
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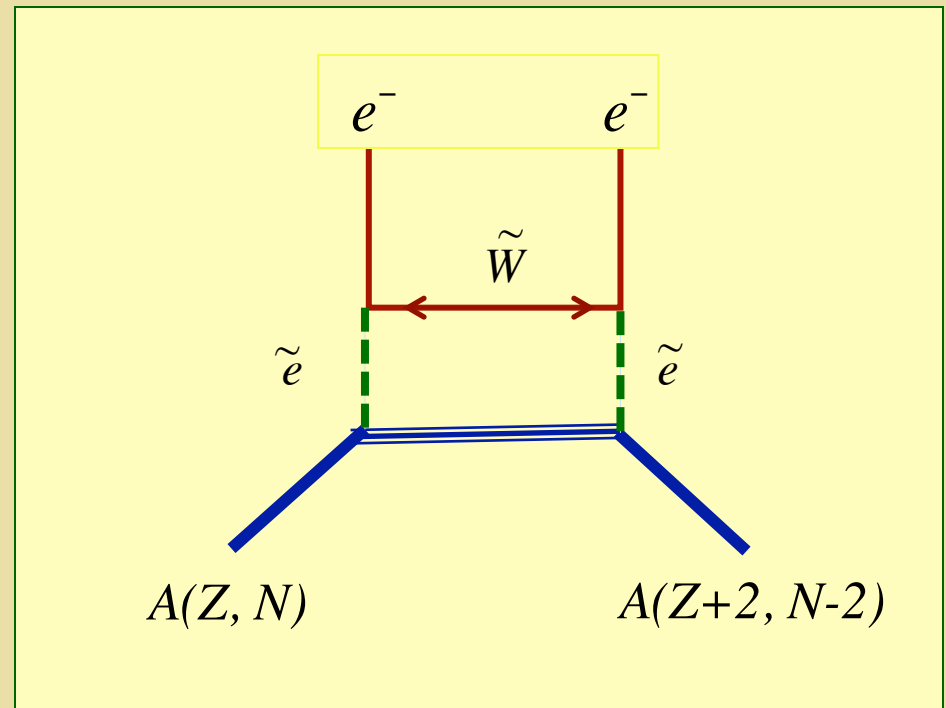
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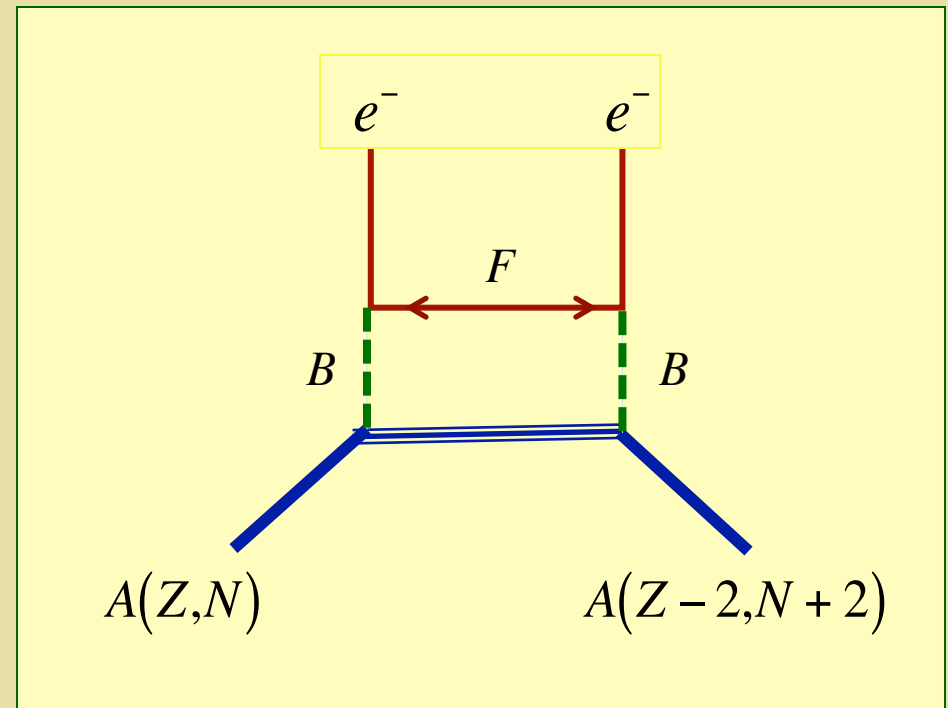
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Majorana

TeV LNV Mechanism

$$\frac{A_H}{A_L} \sim \frac{M_W^4 \bar{k}^2}{\Lambda^5 m_{\beta\beta}}$$

$O(1)$ for $\Lambda \sim 1 \text{ TeV}$



$0\nu\beta\beta$ -Decay: TeV Scale LNV

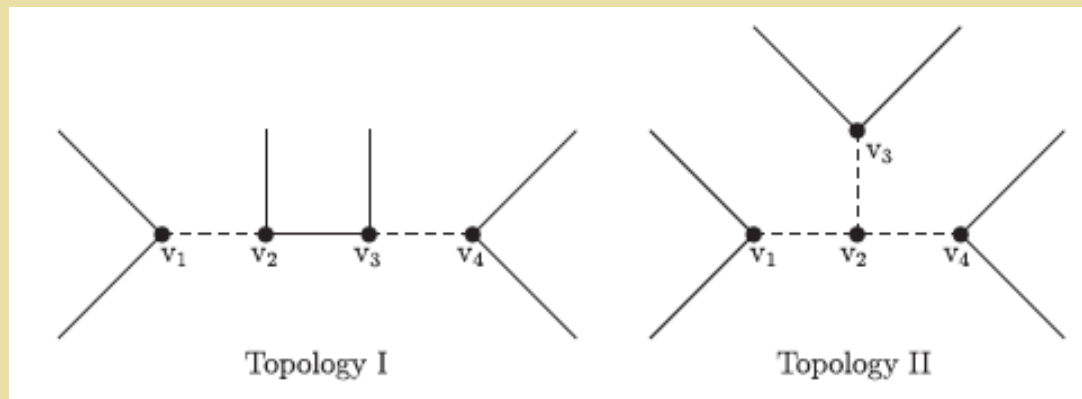
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Majorana

General Classification: Helo et al, PRD 88.011901, 88.073011



$0\nu\beta\beta$ -Decay: TeV Scale LNV

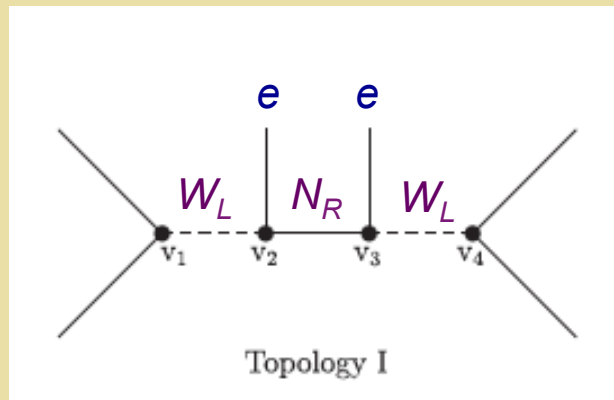
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ν SM: Type I See-Saw

Mass: standard see-saw but TeV scale

$0\nu\beta\beta$ -Decay: TeV Scale LNV

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Dirac

$$\mathcal{L}_{\text{mass}} = \frac{y}{\Lambda} \bar{L}^c H H^T L + \text{h.c.}$$

Majorana

Light + heavy Majorana ν contributions: Single heavy flavor

$$U_{e1}^2 \frac{m_1}{p^2} + V_{e1}^2 \frac{M_1}{p^2 - M_1^2}$$

Type I see-saw: $M_{11} = 0$

$$U_{e1}^2 m_1 + V_{e1}^2 M_1 = 0$$

Mitra et al, 2012

$$U_{e1}^2 \frac{m_1}{p^2} \times \frac{M_1^2}{M_1^2 - p^2}$$

*Since $p^2 < 0 \rightarrow$
Amplitude reduction !*

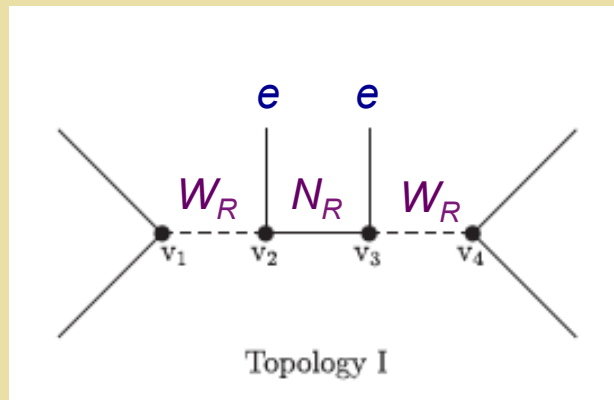
$0\nu\beta\beta$ -Decay: TeV Scale LNV

$$\mathcal{L}_{\text{mass}} = y \bar{L} \tilde{H} \nu_R^{N_R} + \text{h.c.}$$

Dirac

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Majorana

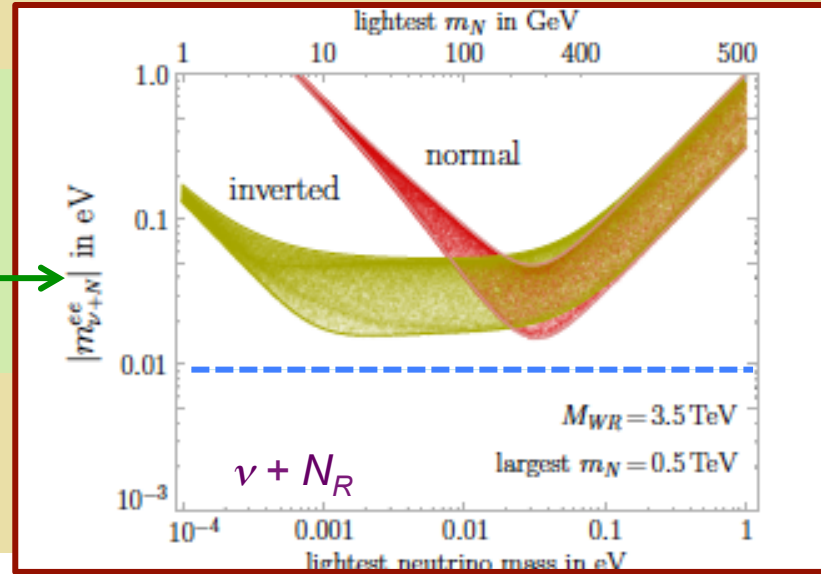
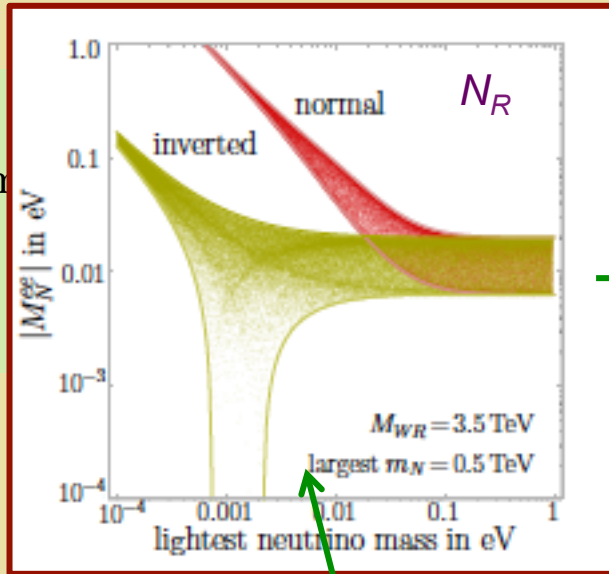


LRSM: Type I See-Saw

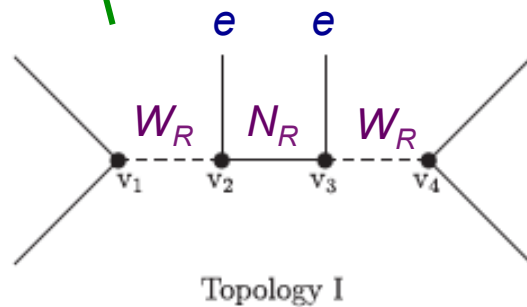
Mass: standard see-saw but TeV scale

$0\nu\beta\beta$ -Decay: TeV Scale LNV

\mathcal{L}_n



C.



LRSM: Type I See-Saw

Mass: standard see-saw but TeV scale

$0\nu\beta\beta$ -Decay: TeV Scale LNV

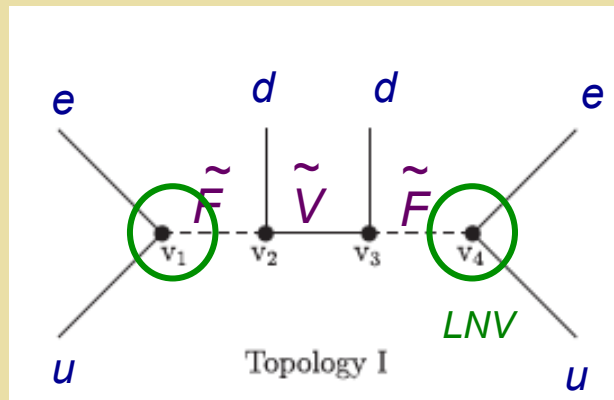
$$\mathcal{L}_{\text{mass}} = y\bar{L}\tilde{H}\nu_R + \text{h.c.}$$

Dirac

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Majorana

General Classification: Helo et al, PRD 88.011901, 88.073011



SUSY: R Parity-Violation

Sfermion \tilde{q}, \tilde{l}

Gaugino \tilde{g}, χ *Majorana*

$$W_{\Delta L=1} = \frac{1}{2}\lambda_{ijk}L_i L_j \bar{e}_k + \lambda'_{ijk}L_i Q_j \bar{d}_k + \mu'_i L_i H_u,$$

$0\nu\beta\beta$ -Decay: TeV Scale LNV

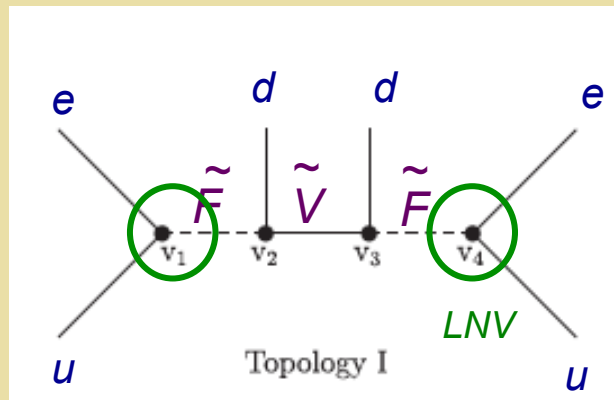
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Majorana

General Classification: Helo et al, PRD 88.011901, 88.073011



SUSY: R Parity-Violation

$$\lambda'_{111} \leq 2 \times 10^{-4} \left(\frac{m_{\tilde{q}}}{100 \text{ GeV}}\right)^2 \left(\frac{m_{\tilde{g}}}{100 \text{ GeV}}\right)^{1/2}$$

$$W_{\Delta L=1} = \frac{1}{2}\lambda_{ijk}L_i L_j \bar{e}_k + \lambda'_{ijk}L_i Q_j \bar{d}_k + \mu'_i L_i H_u,$$

$0\nu\beta\beta$ -Decay: TeV Scale LNV

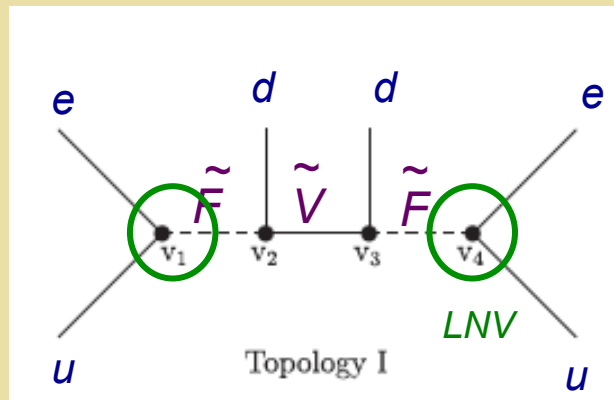
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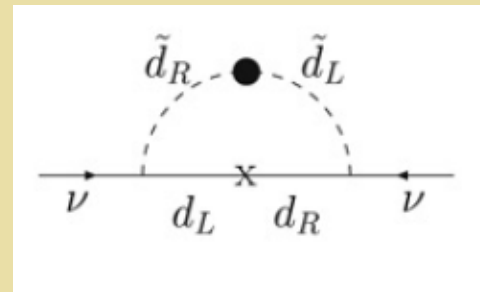
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Majorana

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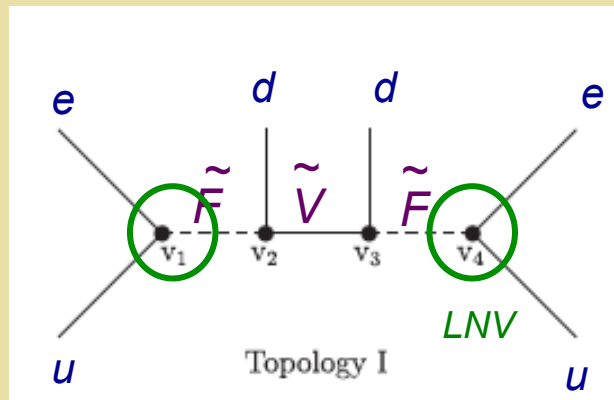
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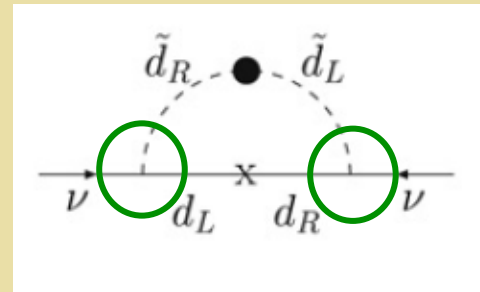
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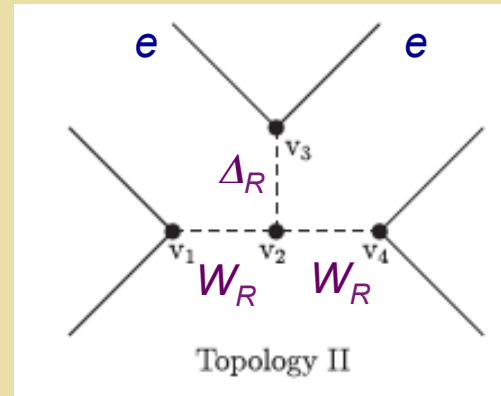
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Majorana

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LRSM: Type II See-Saw

$$\mathcal{L} = \frac{g}{2}h_{ij} [\bar{L}^{C_i}\varepsilon\Delta_L L^j] + (L \leftrightarrow R) + \text{h.c.}$$



$0\nu\beta\beta$ -Decay: TeV Scale LNV

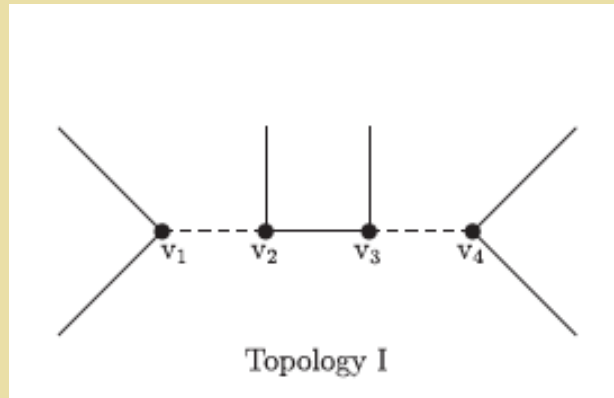
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Dirac

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Majorana

General Classification: Helo et al, PRD 88.011901, 88.073011



Scalar Leptoquarks

Mass: like RPV SUSY (loop)

NLDBD: need Majorana fermion

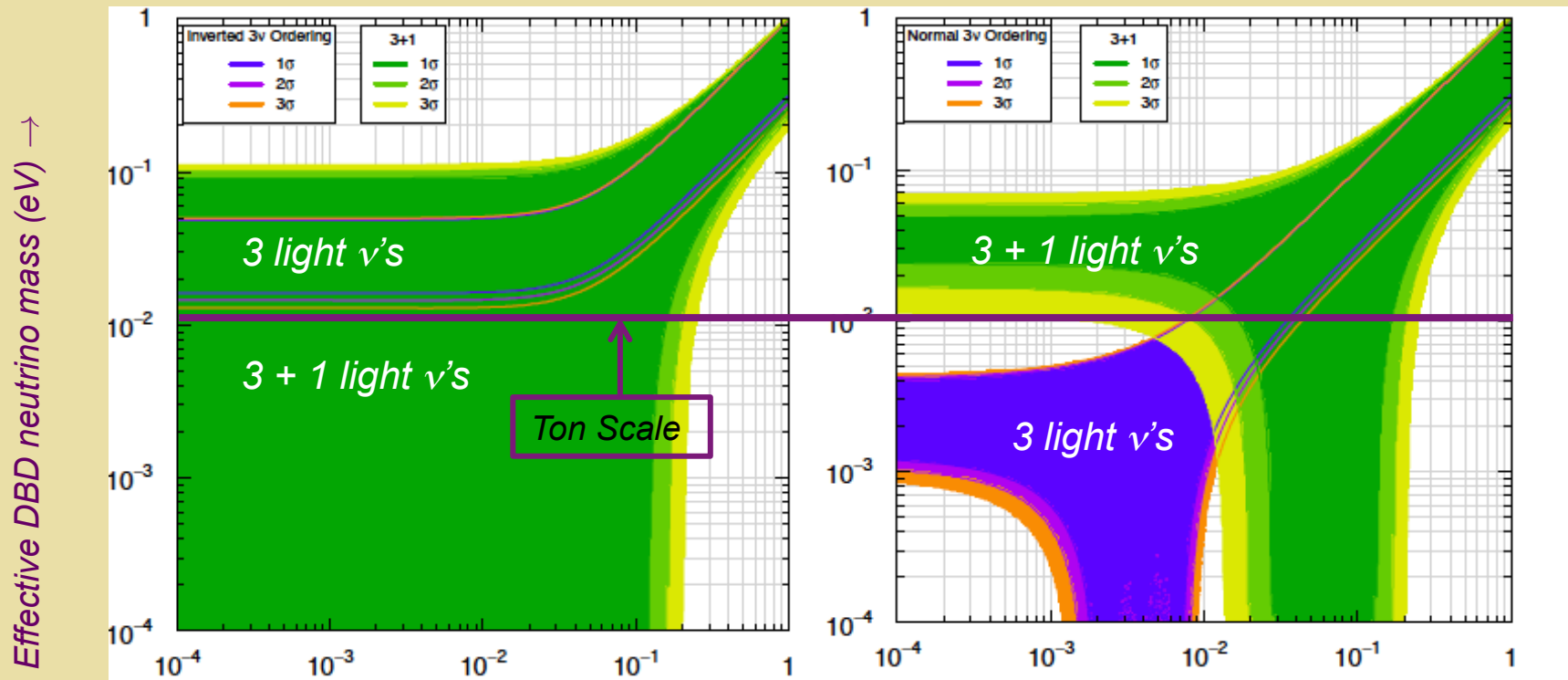
$$\mathcal{L}_{F=0} = h_{1/2}^L \bar{u}_R \ell_L S_{1/2}^L + h_{1/2}^R \bar{q}_L e_R S_{1/2}^R + \tilde{h}_{1/2}^L \bar{d}_R \ell_L \tilde{S}_{1/2}^L$$

LVN Mass Scale & $0\nu\beta\beta$ -Decay



- *3 light neutrinos only: source of neutrino mass at the very high see-saw scale*
- *3 light neutrinos with TeV scale source of neutrino mass*
- *> 3 light neutrinos*

LN ν Mass Scale & $0\nu\beta\beta$ -Decay



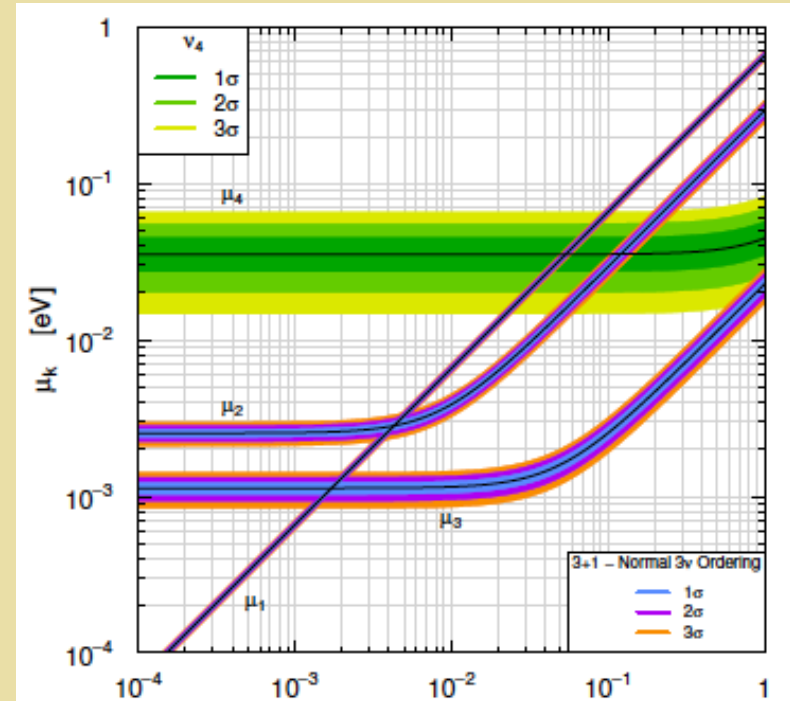
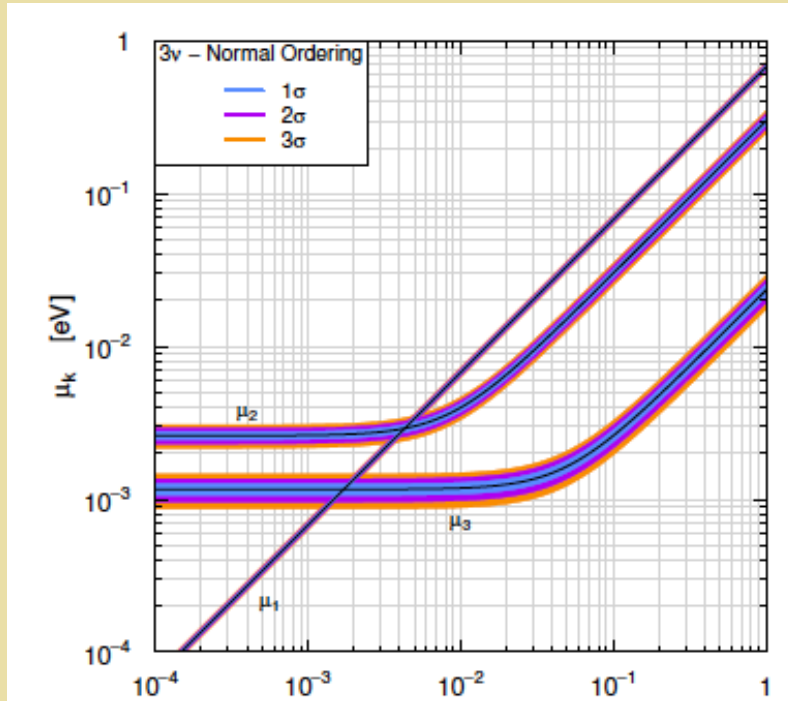
Lightest neutrino mass (eV) →

Sterile Neutrinos & $0\nu\beta\beta$ -Decay

3 active light neutrinos

3+1 active light neutrinos

Effective DBD neutrino mass (eV)



Lightest neutrino mass (eV) \rightarrow

Lightest neutrino mass (eV) \rightarrow

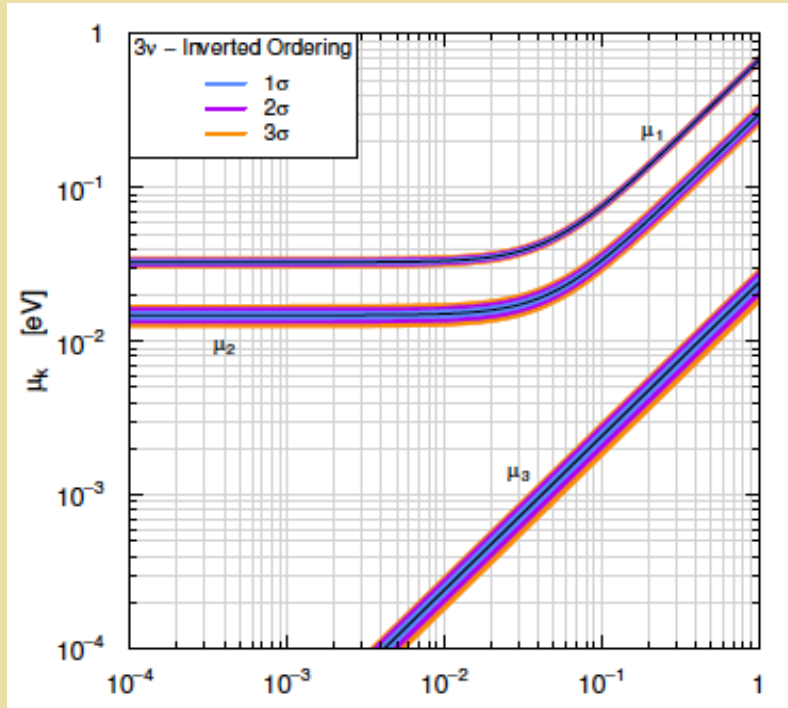
$$|m_{\beta\beta}| = |\mu_1 + \mu_2 e^{i\alpha_2} + \mu_3 e^{i\alpha_3}|$$

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Sterile Neutrinos & $0\nu\beta\beta$ -Decay

3 active light neutrinos

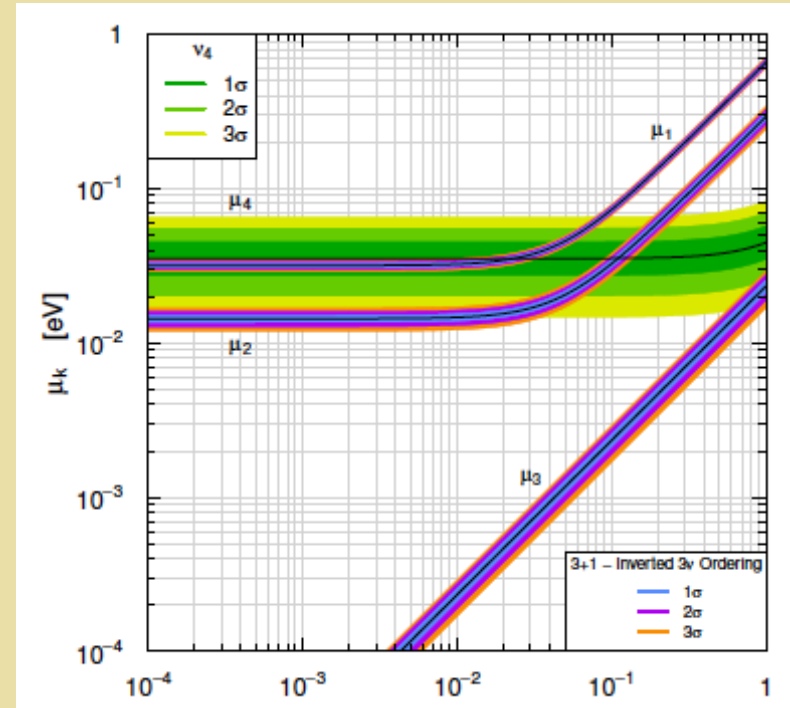
Effective DBD neutrino mass (eV)



Lightest neutrino mass (eV) →

$$|m_{\beta\beta}| = |\mu_1 + \mu_2 e^{i\alpha_2} + \mu_3 e^{i\alpha_3}|$$

3+1 active light neutrinos



Lightest neutrino mass (eV) →

$$|m_{\beta\beta}| = |\mu_1 + \mu_2 e^{i\alpha_2} + \mu_3 e^{i\alpha_3} + \mu_4 e^{i\alpha_4}|$$

$0\nu\beta\beta$ -Decay: Rate & Mass Dependence

$$\mathcal{L}_{\text{mass}} = y \bar{L} \tilde{H} \nu_R^{N_R} + \text{h.c.}$$

Dirac

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Majorana

Light ν exchange

$$\frac{1}{T_{1/2}} = G^{0\nu}(E, Z) |M_{0\nu}| |\langle m_{\beta\beta} \rangle|^2$$

Quadratic dependence on $m_{\beta\beta}$

Heavy particle exchange

$$\begin{aligned} \frac{1}{T_{1/2}} = & G_{01} \left(\frac{\text{TeV}}{m_e} \right)^2 \left(\frac{\Lambda_H}{\text{TeV}} \right)^4 \left(\frac{1}{18} \right) \left(\frac{v}{\text{TeV}} \right)^8 \\ & \times \left(\frac{1}{g_A \cos \theta_C} \right)^4 |M_0|^2 \left[\frac{C_{\text{eff}}^2}{(\Lambda/\text{TeV})^{10}} \right], \end{aligned}$$

Scales as $1 / M^{10}$

Lecture II Summary

- *Origin of neutrino mass is a key open problem in fundamental interaction physics*
- *There exist a wide array of well-motivated models that address it with sensitivities to a variety of BSM mass scales*
- *These scenarios may also address other key open problems, such as the origin of the matter-antimatter asymmetry*
- *The corresponding implications for $0\nu\beta\beta$ -decay are rich and go well beyond the simplest “standard mechanism” expectations*