



$$\sin^2 \theta_W = 0.238$$
$$\theta_W = 29.2^\circ$$

Future PVES Experiment New, high precision measurement of the weak mixing angle

Frank Maas

(Helmholtz Institute Mainz,
Institute for Nuclear Physics,
PRISMA cluster of excellence)

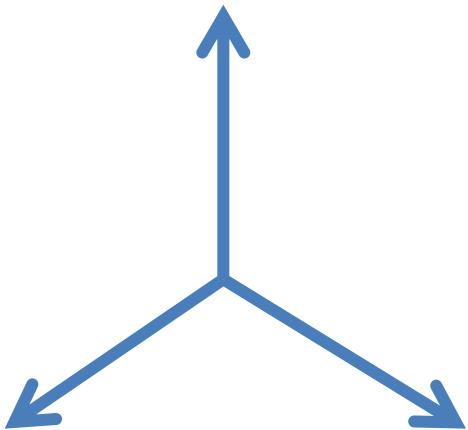
Johannes Gutenberg University Mainz

“The Electroweak Box Workshop”, Amherst Center for Fundamental Physics
September 4-28-30, 2017



Search for New Physics: Various Methods

High Energy (LHC)

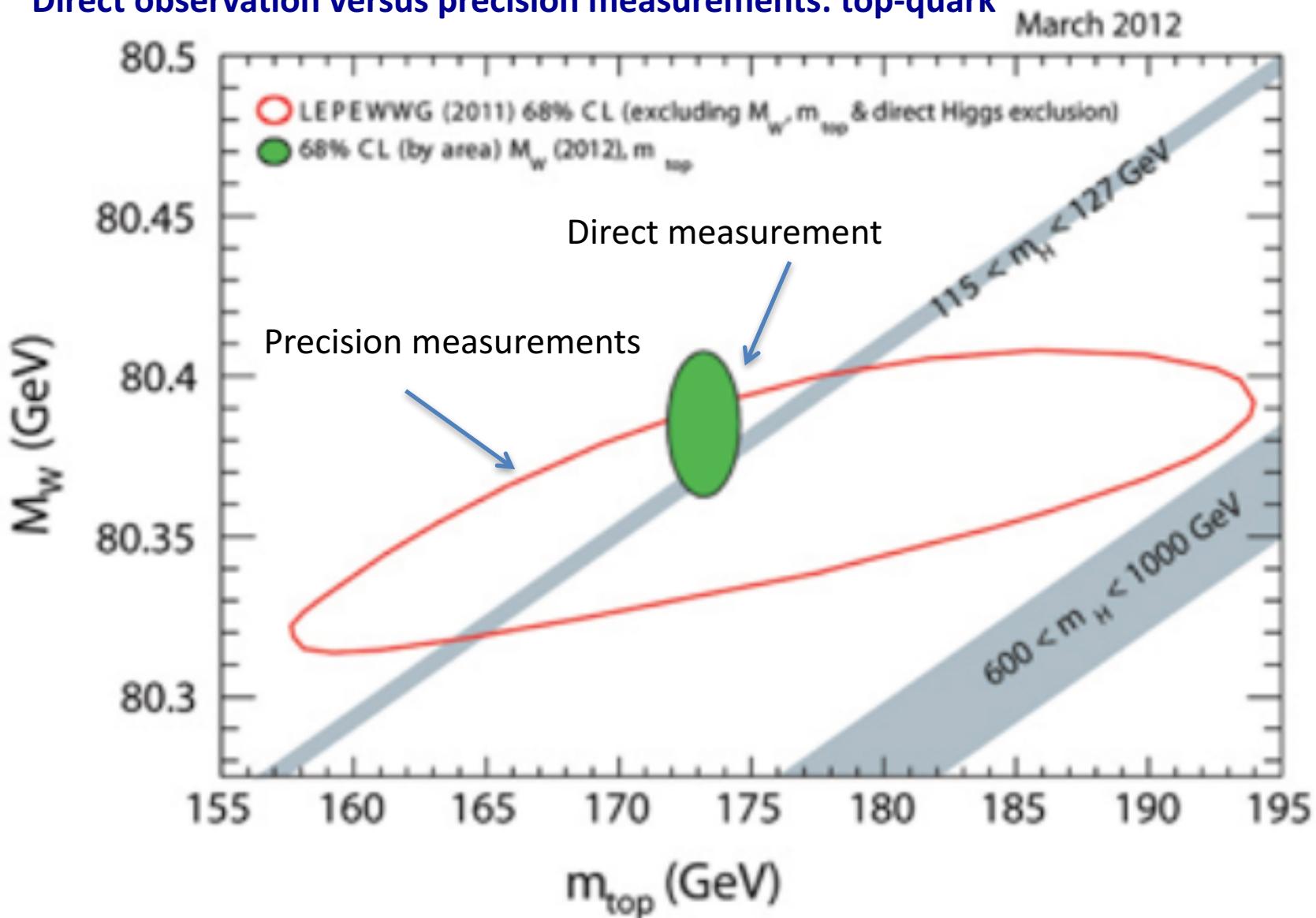


High Intensity
(B-decays)

High Precision
 $((g-2)_\mu, \text{EDM}, \sin^2 \theta_W, \dots)$
(at low energy)

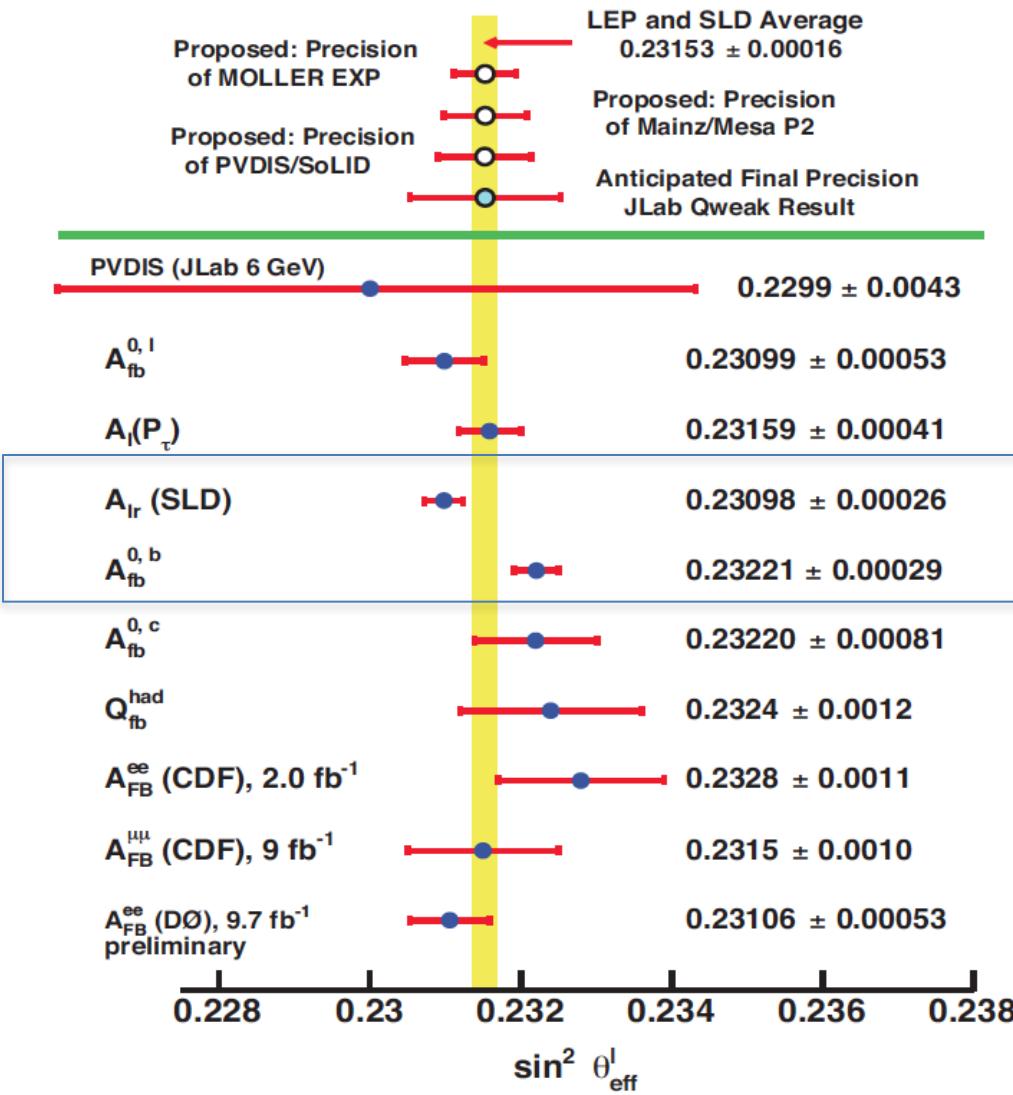


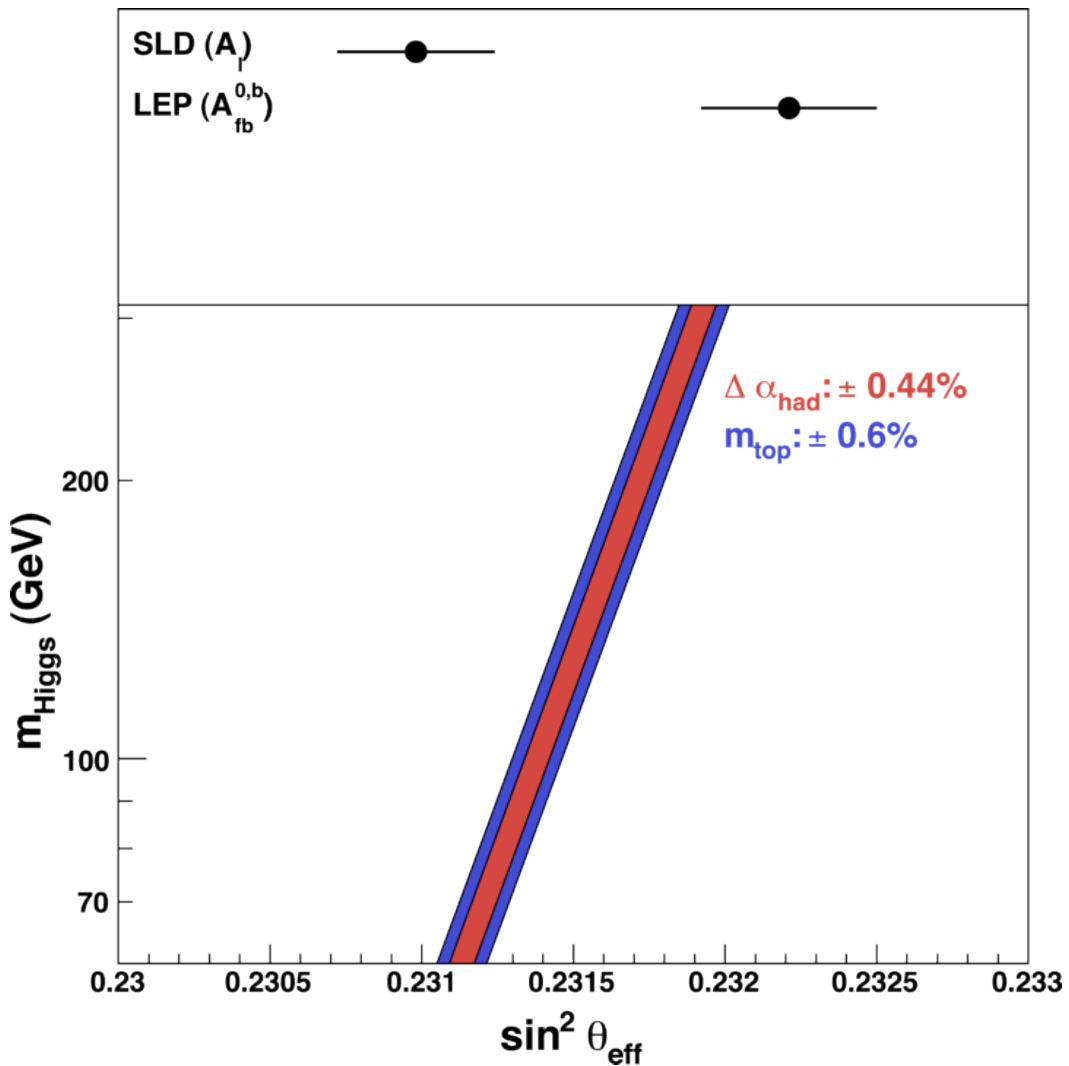
Direct observation versus precision measurements: top-quark

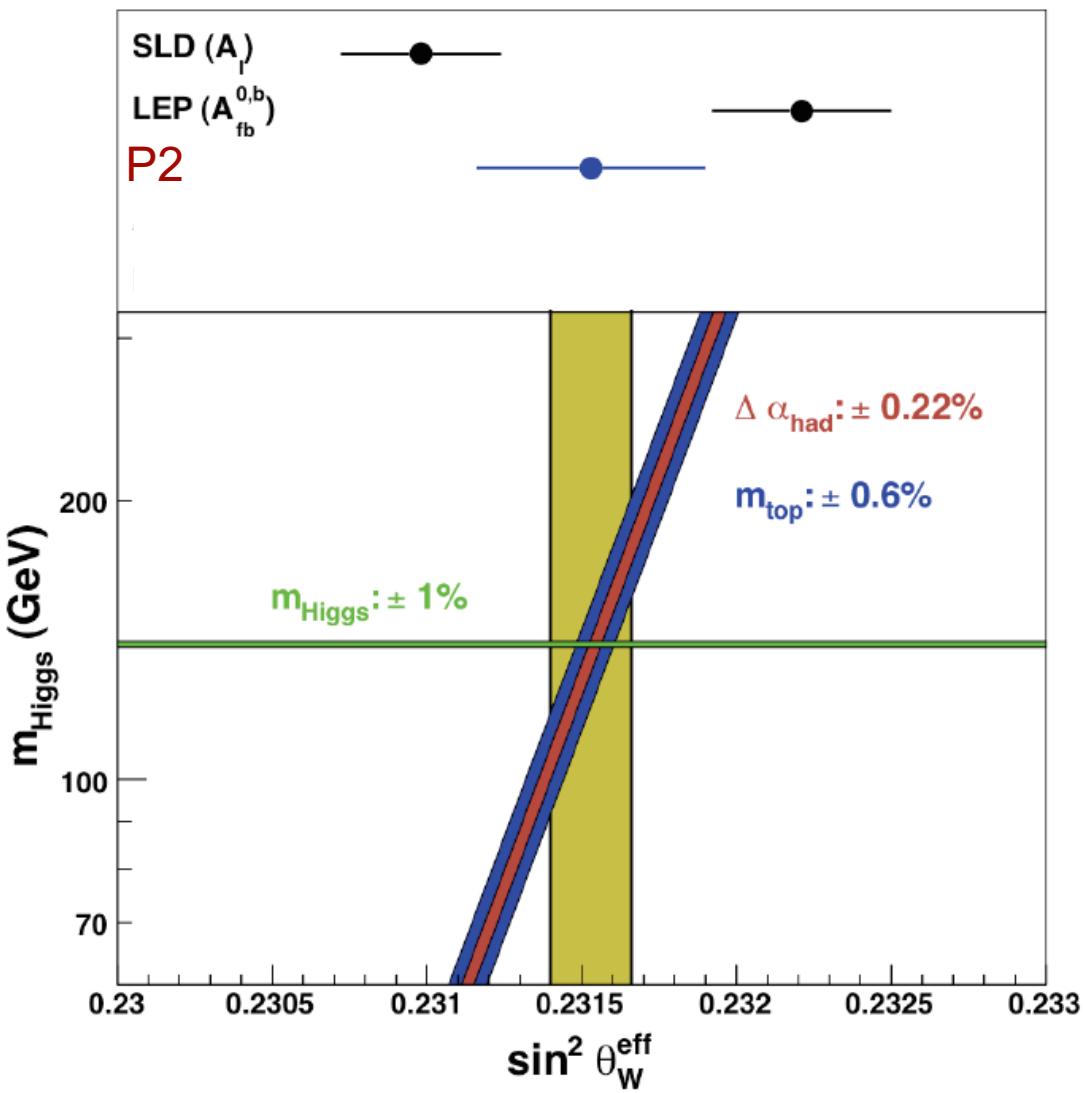




Summary: Measurements of $\sin^2 \theta_{W(\text{effective})}^l$



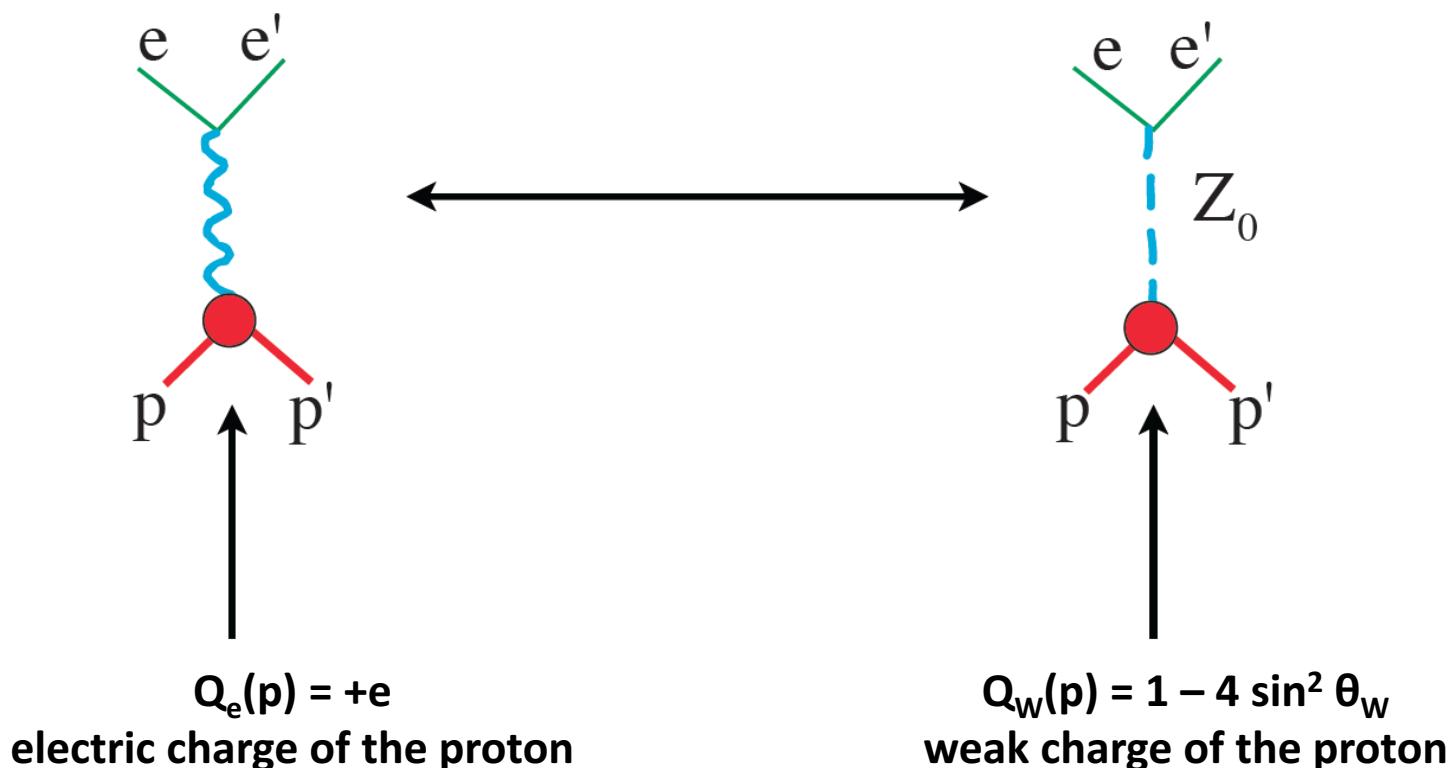






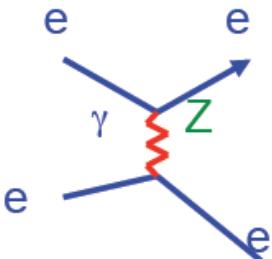
The role of the weak mixing angle

The **relative strength** between the weak and electromagnetic interaction is determined by the **weak mixing angle**: $\sin^2(\theta_W)$



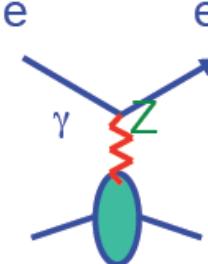
$\sin^2 \theta_W$: a **central parameter** of the standard model

Møller Scattering



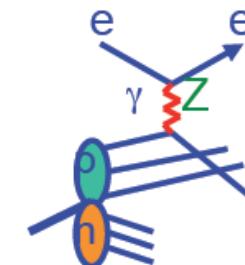
- Purely Leptonic

Q-Weak (JLab) P2 (Mainz/MESA)



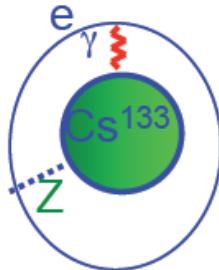
- Coherent quarks in p
- in operation now
- $2(2C_{1u} + C_{1d})$

e-DIS



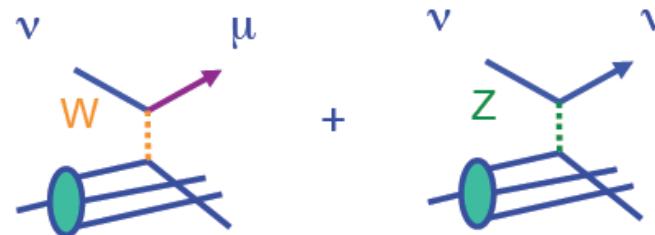
- Isoscaler quark scattering
- $(2C_{1u} - C_{1d}) + Y(2C_{2u} - C_{2d})$

Atomic Parity Violation



- Coherent quarks in entire nucleus
- Nuclear structure uncertainties
- $-376 C_{1u} - 422 C_{1d}$

Neutrino Scattering



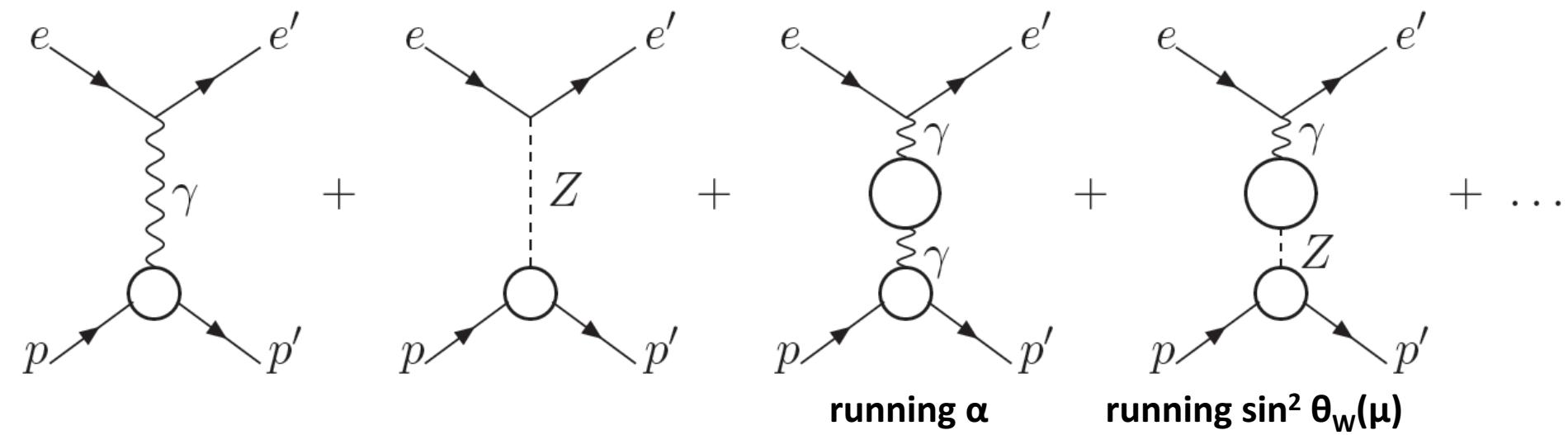
- Quark scattering (from nucleus)
- Weak charged and neutral current difference



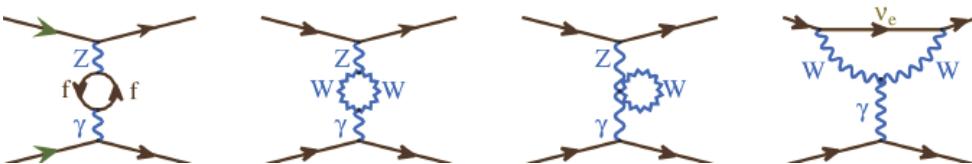
„running“ $\sin^2 \theta_{\text{eff}}$ or $\sin^2 \theta_W(\mu)$

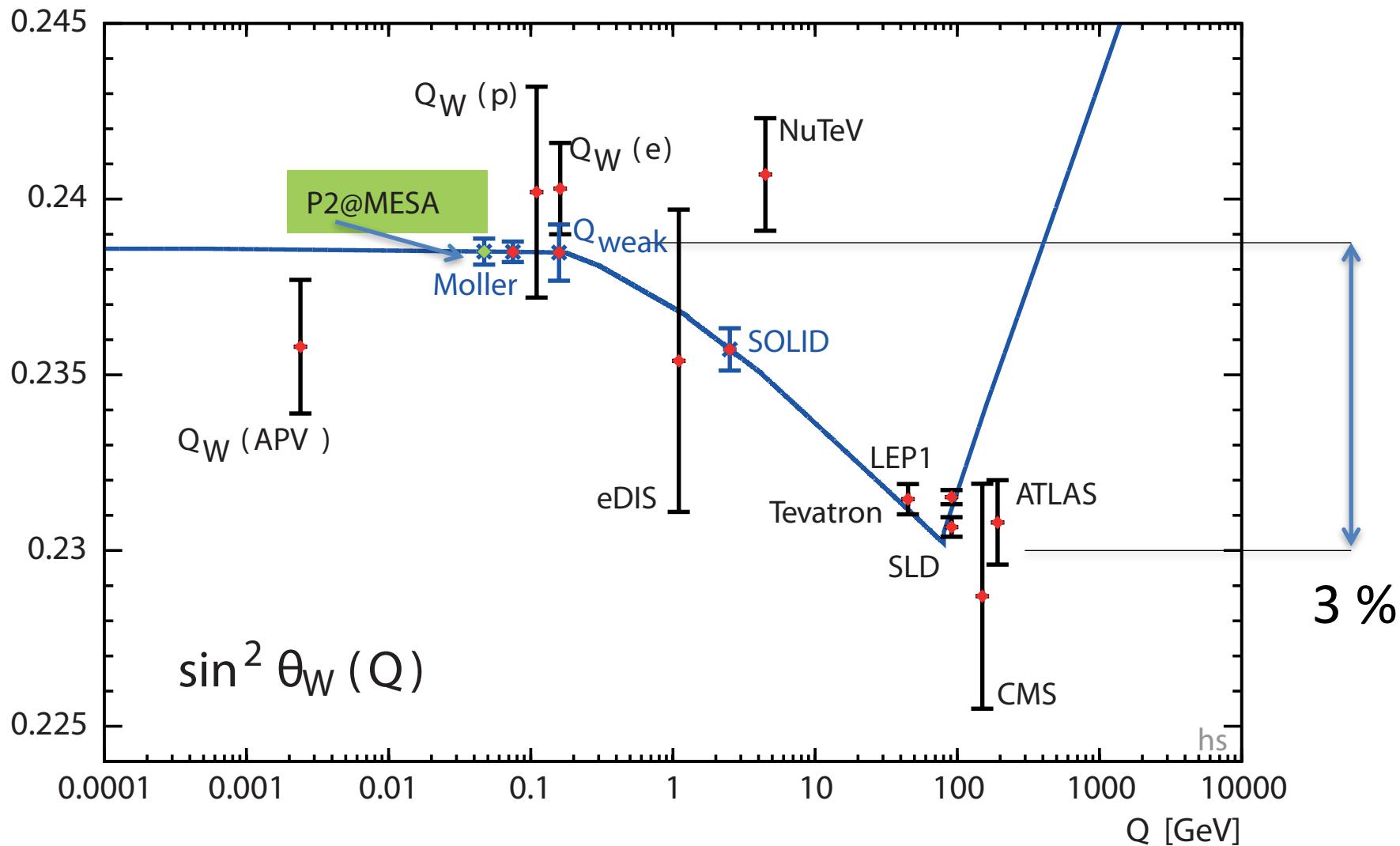


Precision measurements and quantum corrections:



Universal quantum corrections: can be absorbed into a
scale dependent, „running“ $\sin^2 \theta_{\text{eff}}$ or $\sin^2 \theta_W(\mu)$



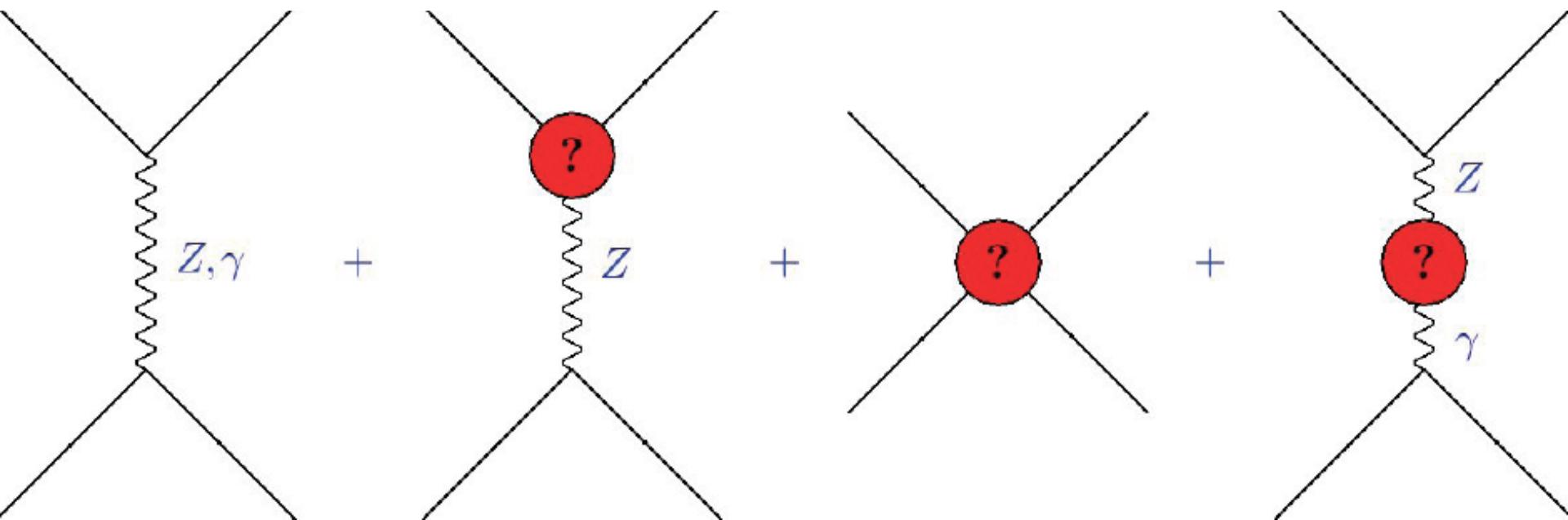




Sensitivity to new physics beyond the Standard Model



Sensitivity to new physics beyond the Standard Model



Extra Z

Mixing with
Dark photon or
Dark Z

Contact interaction

New
Fermions

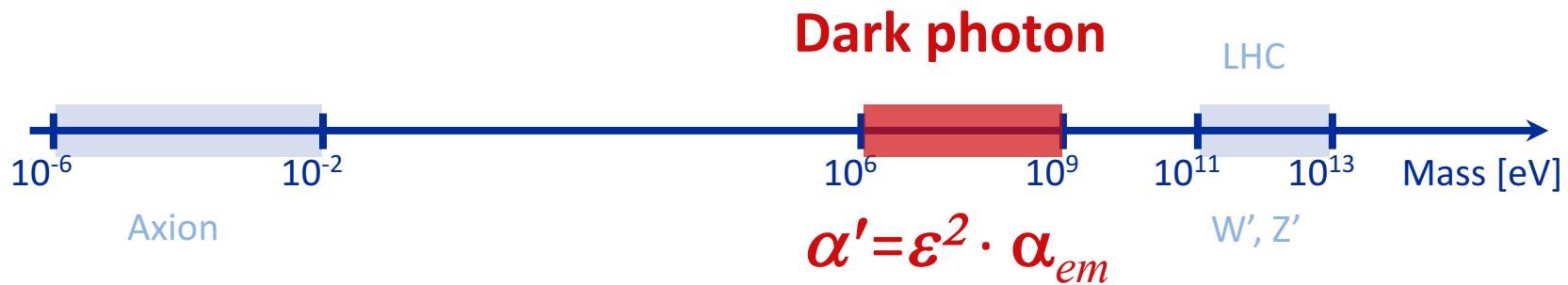


Dark Photon, Z-Boson



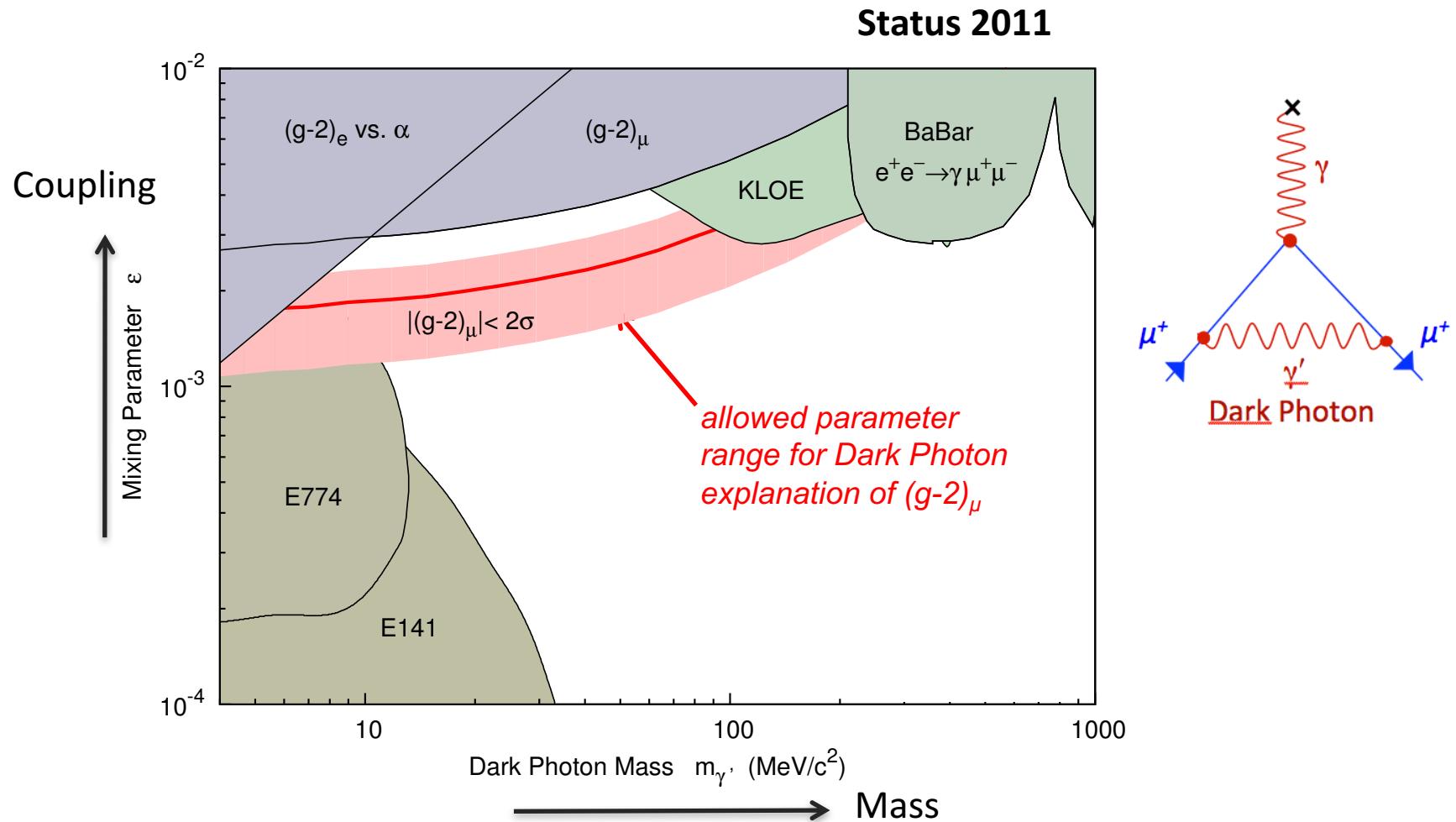
New massive force carrier of extra $U(1)_d$ gauge group;
predicted in almost all string compactifications

$$Z = \cos\theta_W W_3 - \sin\theta_W B$$
$$A = \sin\theta_W W_3 + \cos\theta_W B$$



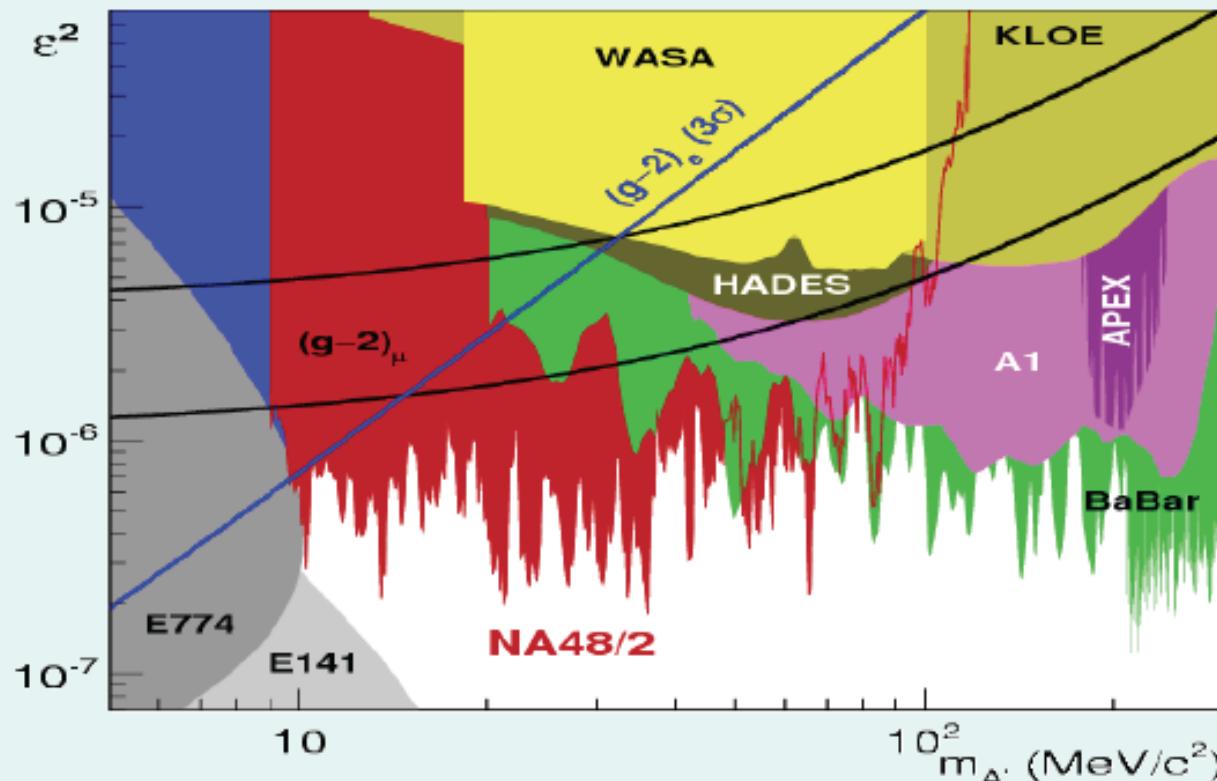
Search for the $O(\text{GeV}/c^2)$ mass scale in a world-wide effort

- Could explain large number of **astrophysical anomalies**
*Arkani-Hamed et al. (2009)
Andreas, Ringwald (2010); Andreas, Niebuhr, Ringwald (2012)*
- Could (have) explained presently seen **deviation of $>3\sigma$** between $(g-2)_\mu$
Standard Model prediction and direct $(g-2)_\mu$ measurement
Pospelov (2008)



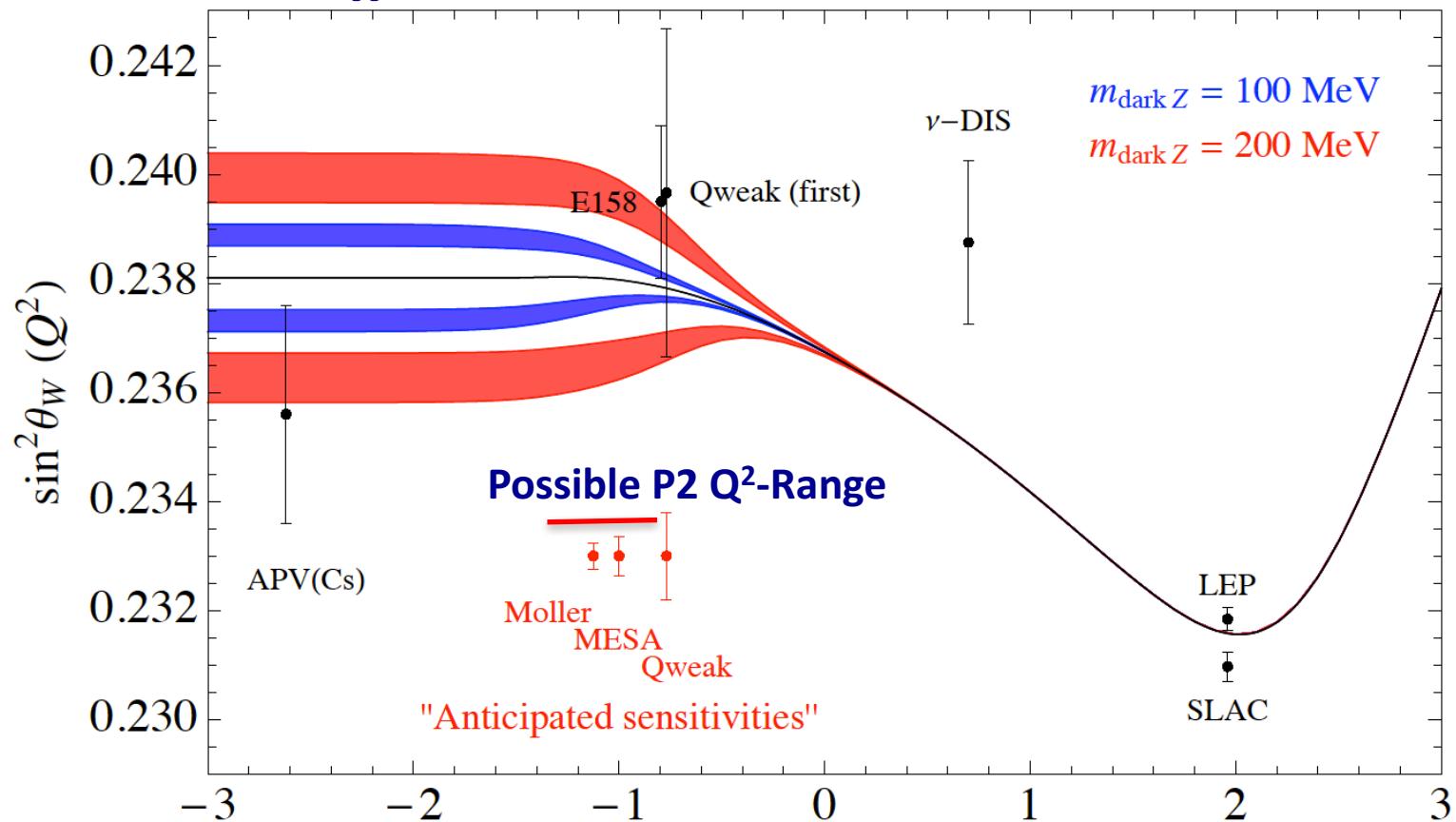


NA48/2 Updated Bounds on Dark Photon
 $g_\mu - 2$ discrepancy solution ruled out
Assumes $\text{BR}(Z_d \rightarrow e^+e^-) \sim 1$





Running $\sin^2 \theta_W$ and Dark Parity Violation



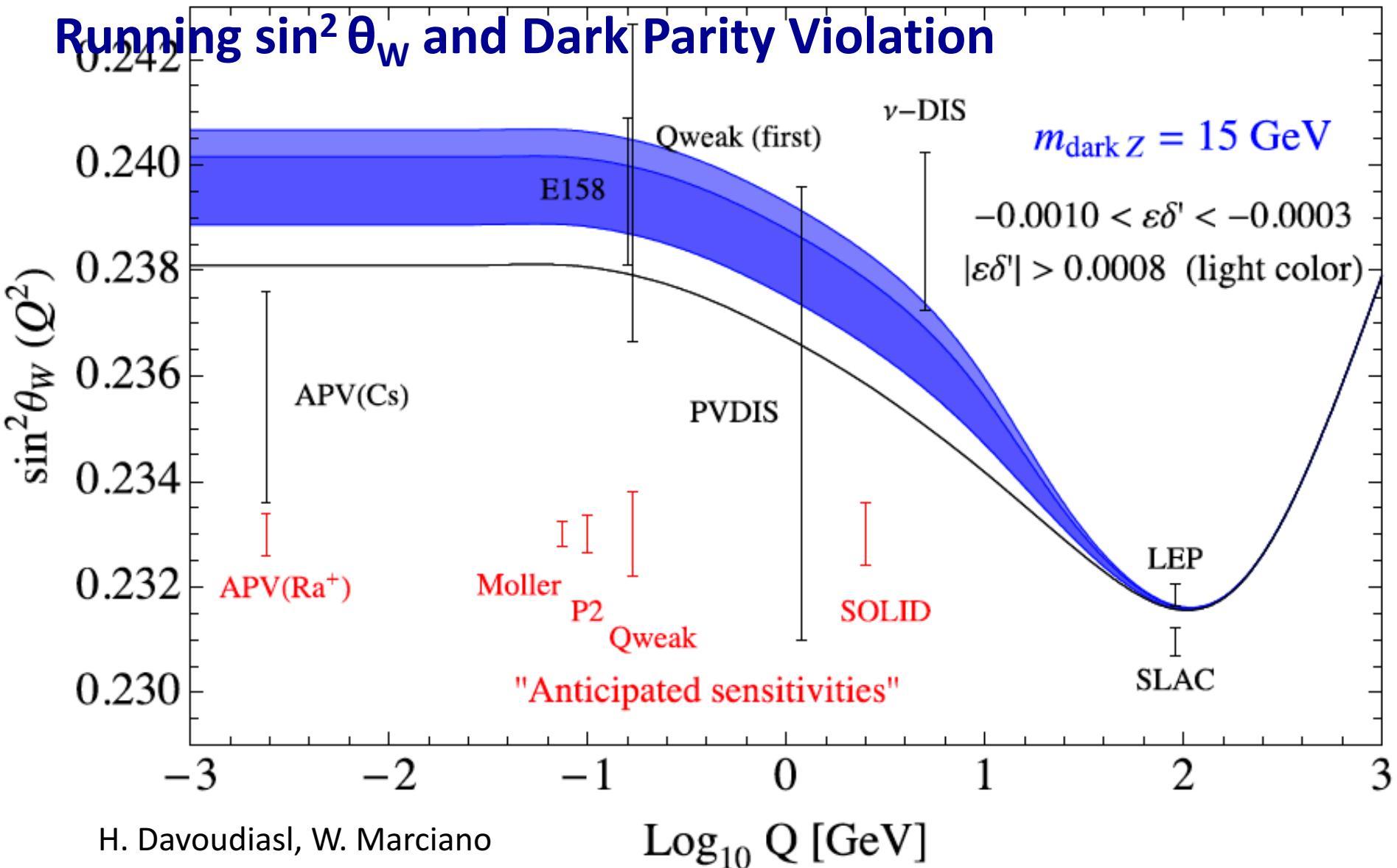
$$Z = \cos \theta_W W_3 - \sin \theta_W B$$
$$A = \sin \theta_W W_3 + \cos \theta_W B$$

 $\log_{10} Q [\text{GeV}]$

Bill Marciano



Running $\sin^2 \theta_W$ and Dark Parity Violation





- Complementary access by weak charges of proton and electron

Weak charge of the proton:

$$Q_W^p = 0.0716$$

A horizontal line with a central dot and two vertical error bars extending to the left and right, labeled ± 0.0029 .

Weak charge of the electron:

$$Q_W^e = -0.0449$$

A horizontal line with a central dot and two vertical error bars extending to the left and right, labeled ± 0.0051 .

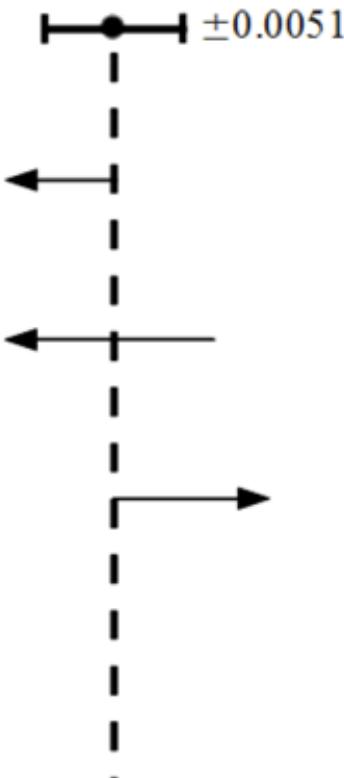
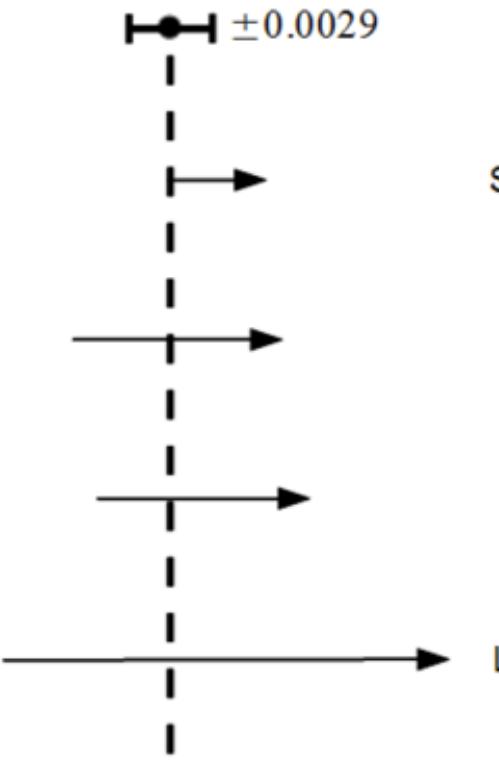
Experiment

SUSY-Loops

$E_6 Z'$

RPV SUSY

Leptoquarks



SM

(Jens Erler, Ramsey-Musolf, 2003)

SM



Weak
Charge
Of
Proton:
Qweak (Jlab),
P2 (MESA)

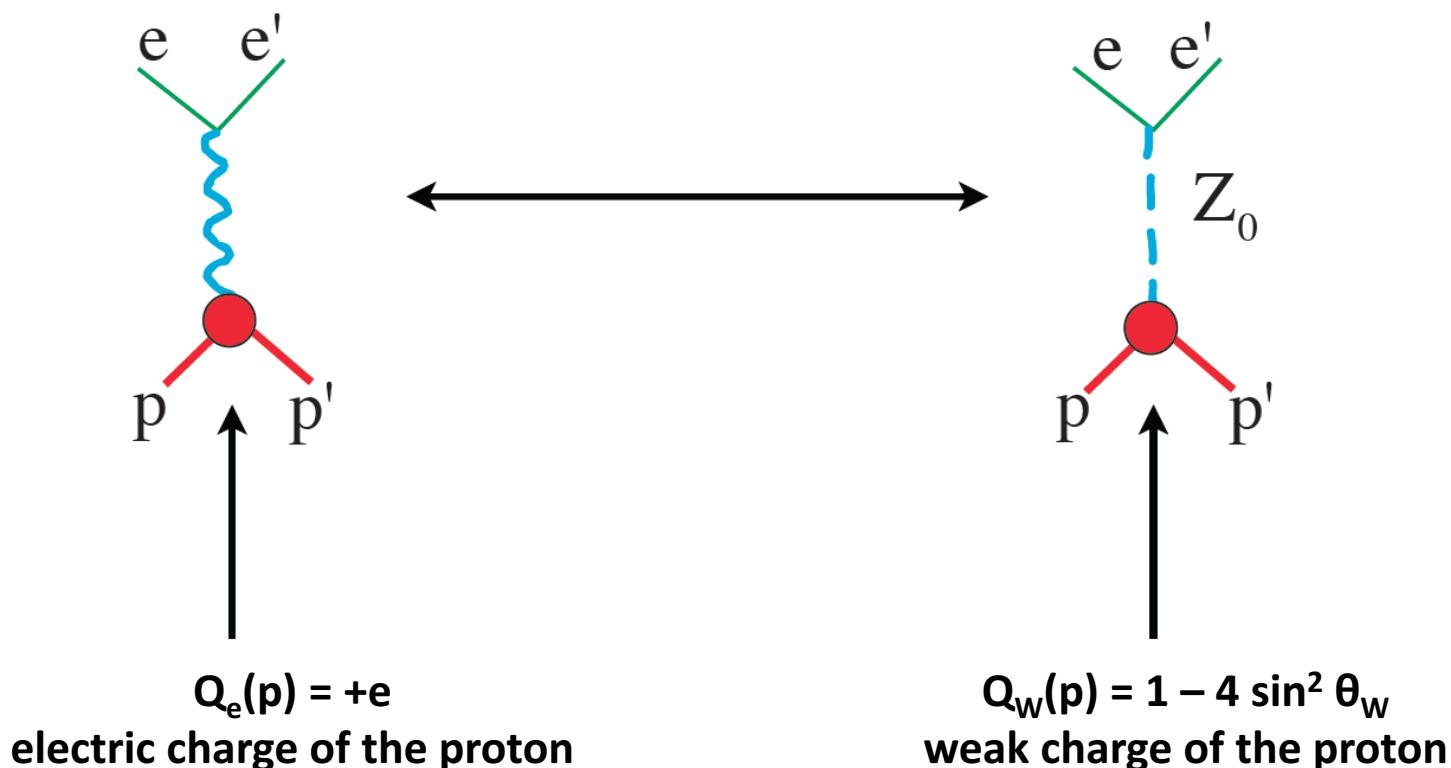
Weak
Charge
Of
Electron:
MOELLER
(JLAB)

Weak
Charge
Of
Quarks:
SOLID
(PVDIS)
(JLAB)



The role of the weak mixing angle

The **relative strength** between the weak and electromagnetic interaction is determined by the **weak mixing angle**: $\sin^2(\theta_W)$



$\sin^2 \theta_W$: a **central parameter** of the standard model



Proton: special case

$$\text{Proton Weak charge: } Q_W(p) = 1 - 4 \sin^2 \theta_W$$

$$\text{Error: } \Delta Q_W(p) = 4 \Delta \sin^2 \theta_W$$

$$\text{Rel. error: } \Delta Q_W(p)/Q_W(p) = 4/((1/\sin^2 \theta_W) - 4) \quad (\Delta \sin^2 \theta_W / \sin^2 \theta_W)$$

$$\text{Rel. error } \Delta \sin^2 \theta_W / \sin^2 \theta_W = ((1/\sin^2 \theta_W) - 4) / 4 \quad \Delta Q_W(p)/Q_W(p)$$

$$\text{Example: } \sin^2 \theta_W (50 \text{ MeV}) = 0.238$$

$$4/((1/\sin^2 \theta_W) - 4) \sim 20$$

$$\Delta Q_W(p)/Q_W(p) = 2\% \quad \text{from Experiment}$$

$$\Delta \sin^2 \theta_W / \sin^2 \theta_W = 0.1 \% \quad \text{same precision as LEP, SLAC}$$

Neutron Weak charge:

$$\Delta Q_W(p)/Q_W(n) = \Delta \sin^2 \theta_W / \sin^2 \theta_W$$

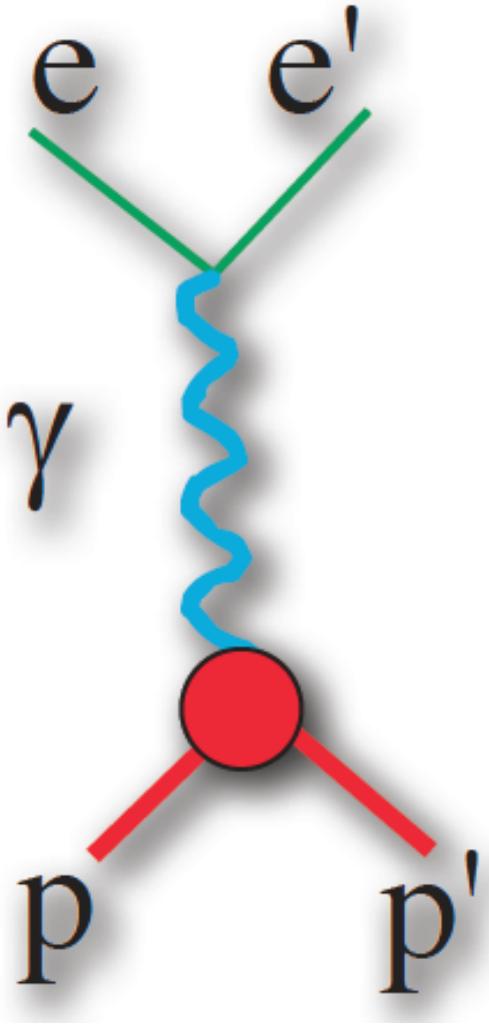


Physics sensitivity from contact interaction (LEP2 convention, $g^2 = 4\pi$)

	precision	$\Delta \sin^2 \bar{\theta}_W(0)$	$\Lambda_{\text{new}} (\text{expected})$
APV Cs	0.58 %	0.0019	32.3 TeV
E158	14 %	0.0013	17.0 TeV
Qweak I	19 %	0.0030	17.0 TeV
Qweak final	4.5 %	0.0008	33 TeV
PVDIS	4.5 %	0.0050	7.6 TeV
SoLID	0.6 %	0.00057	22 TeV
MOLLER	2.3 %	0.00026	39 TeV
P2	2.0 %	0.00036	49 TeV
PVES ^{12}C	0.3 %	0.0007	49 TeV

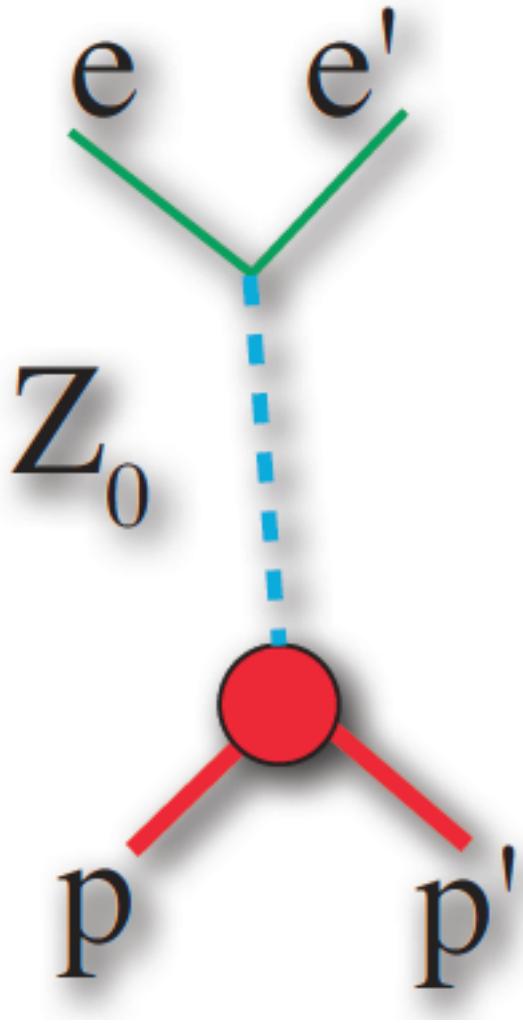


Experimental Method: Parity Violating Electron Scattering



$$\begin{aligned}\sigma &\sim \mathcal{M} \mathcal{M}^* \text{ Phasespace} \\ &\sim (\mathbf{j}_\mu \frac{1}{Q^2} J^\mu)(\mathbf{j}_\mu \frac{1}{Q^2} J^\mu)^*\end{aligned}$$
$$\mathbf{j}_\mu \sim \bar{e} \gamma_\mu e \text{ Vector Current}$$

$$\begin{aligned}J_\gamma^\mu &\sim \left\langle N | q^{\textcolor{red}{u}} \bar{u} \gamma_\mu u + q^{\textcolor{blue}{d}} \bar{d} \gamma_\mu d + q^{\textcolor{green}{s}} \bar{s} \gamma_\mu s | N' \right\rangle \\ &= \overline{\mathcal{P}} [\gamma^\mu \mathbf{F}_1 - i \sigma^{\mu\nu} q_\nu \frac{\kappa_p}{2M_N} \mathbf{F}_2] \mathcal{P}\end{aligned}$$



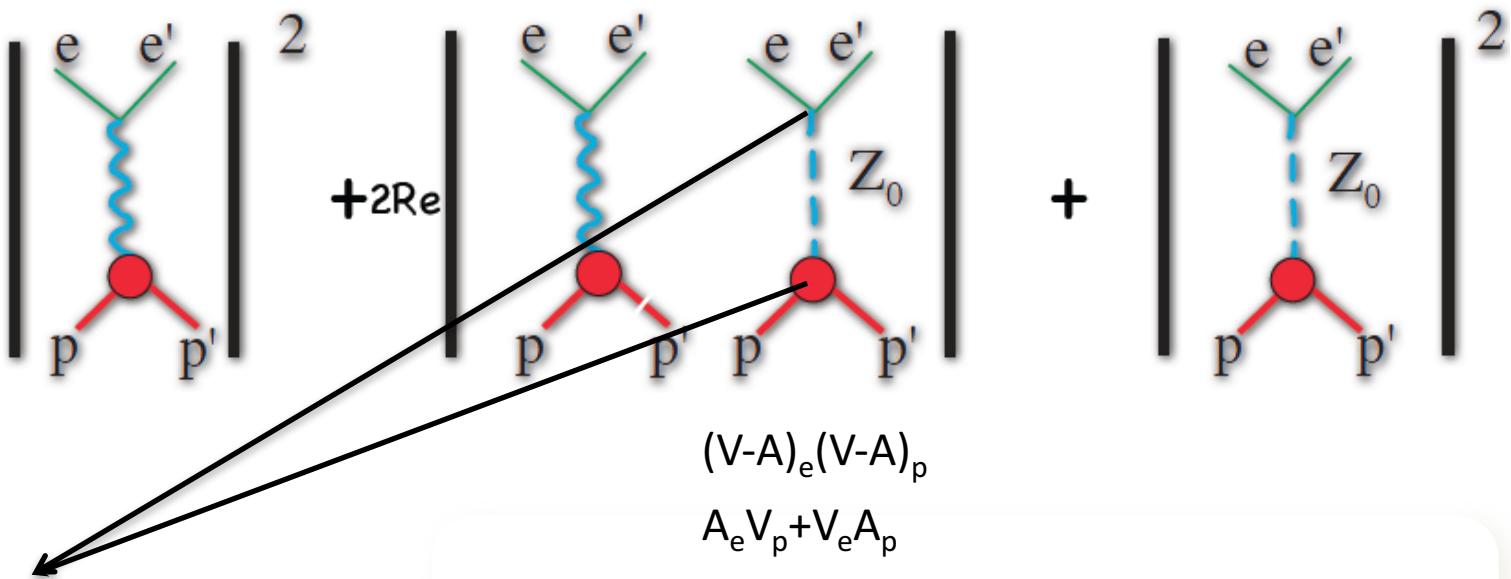
$$\tilde{q}^d V = \tau_3 - 2q^d \sin^2(\theta_W)$$

$$\begin{aligned}\tilde{J}_Z^\mu &\sim \left\langle N | \tilde{q}^{\textcolor{red}{u}} \bar{u} \gamma_\mu u + \tilde{q}^{\textcolor{blue}{d}} \bar{d} \gamma_\mu d + \tilde{q}^{\textcolor{green}{s}} \bar{s} \gamma_\mu s | N' \right\rangle \\ &= \overline{\mathcal{P}} [\gamma^\mu \tilde{F}_1 - i \sigma^{\mu\nu} q_\nu \frac{\kappa_p}{2M_N} \tilde{F}_2] \mathcal{P}\end{aligned}$$

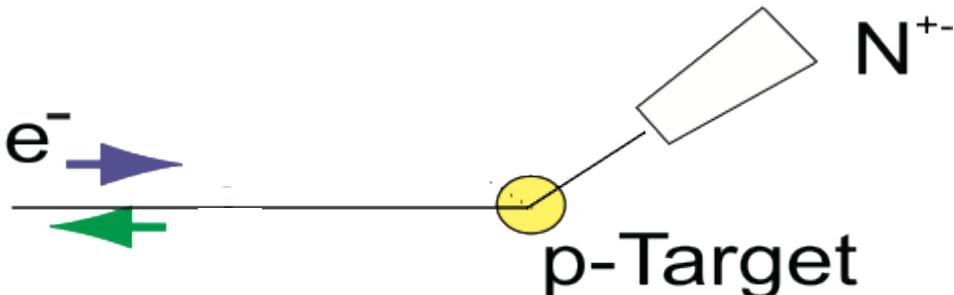


Parity Violating Asymmetry in elastic electron proton scattering

$$\sigma \approx$$



V-A coupling:
parity-violating
cross section asymmetry A_{LR}
longitudinally pol. electrons
unpolarised protons





Parity violating cross section asymmetry

$$A_{LR} = \frac{\sigma(e \uparrow) - \sigma(e \downarrow)}{\sigma(e \uparrow) + \sigma(e \downarrow)} = -\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} (Q_W - F(Q^2))$$

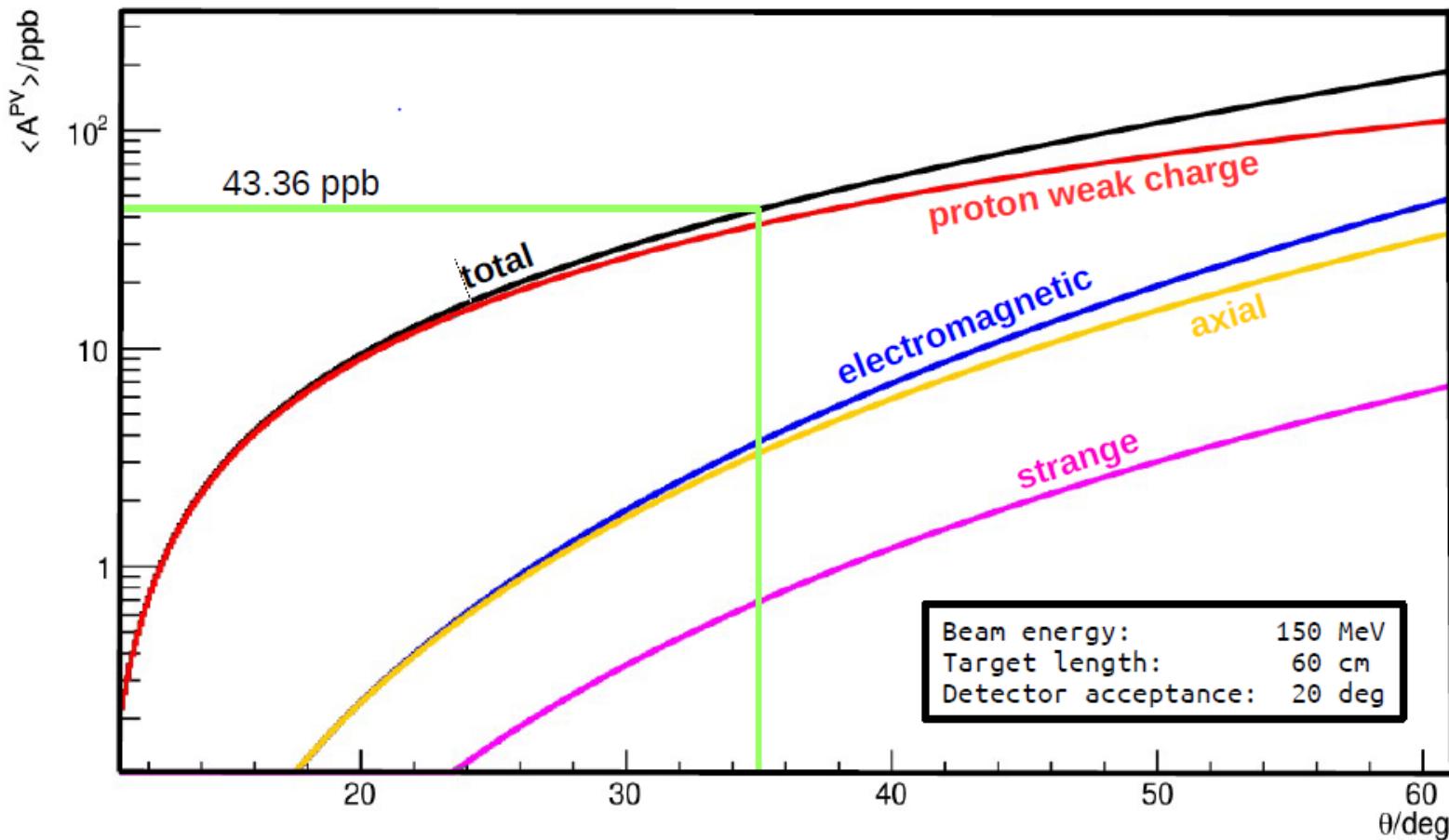
$$Q_W = 1 - 4 \sin^2 \theta_W(\mu)$$

polarisation measurement
hadron structure

$$F(Q^2) = F_{EM}(Q^2) + F_{Axial}(Q^2) + F_{Strange}(Q^2)$$



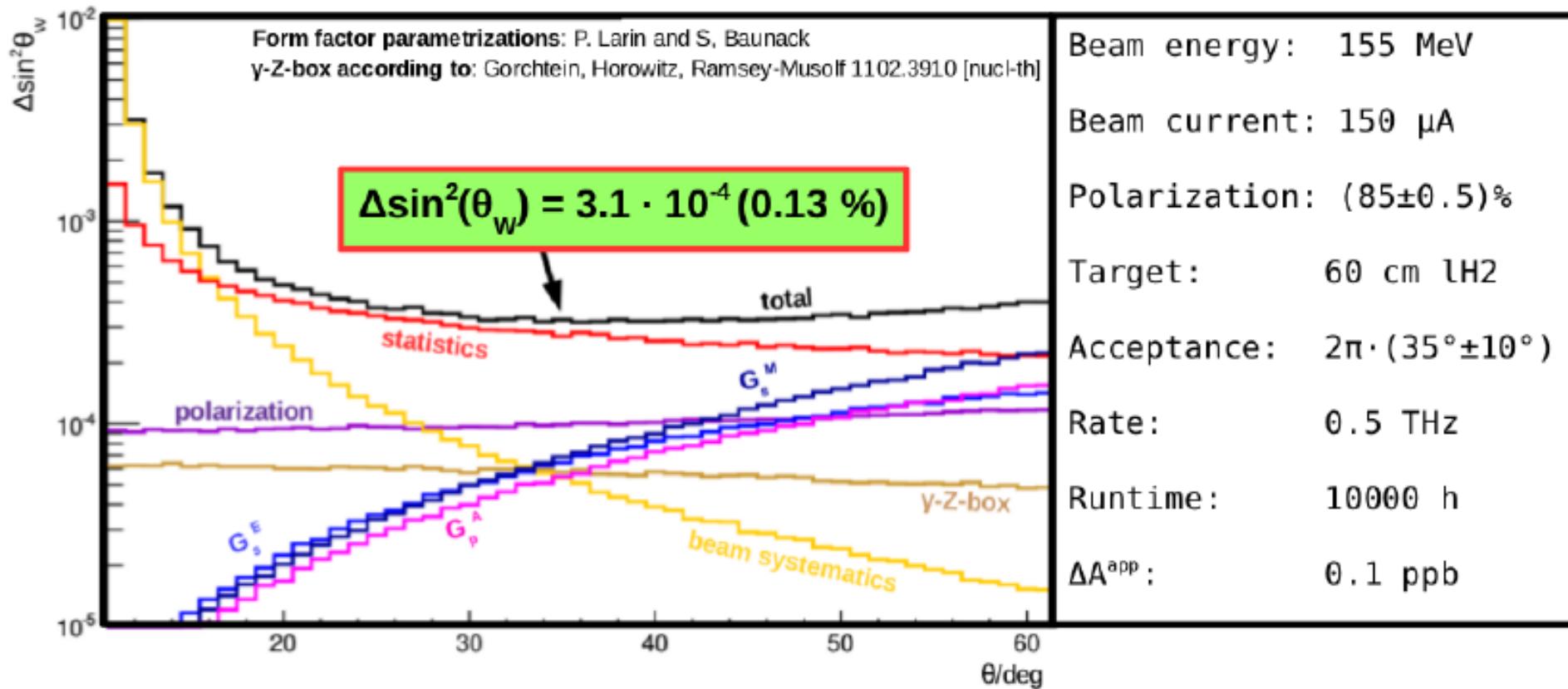
- Contributions to $\Delta \sin^2 \Theta_W$ for 35° central scattering angle, $E=150$ MeV, 10000 h of data taking





JG|U

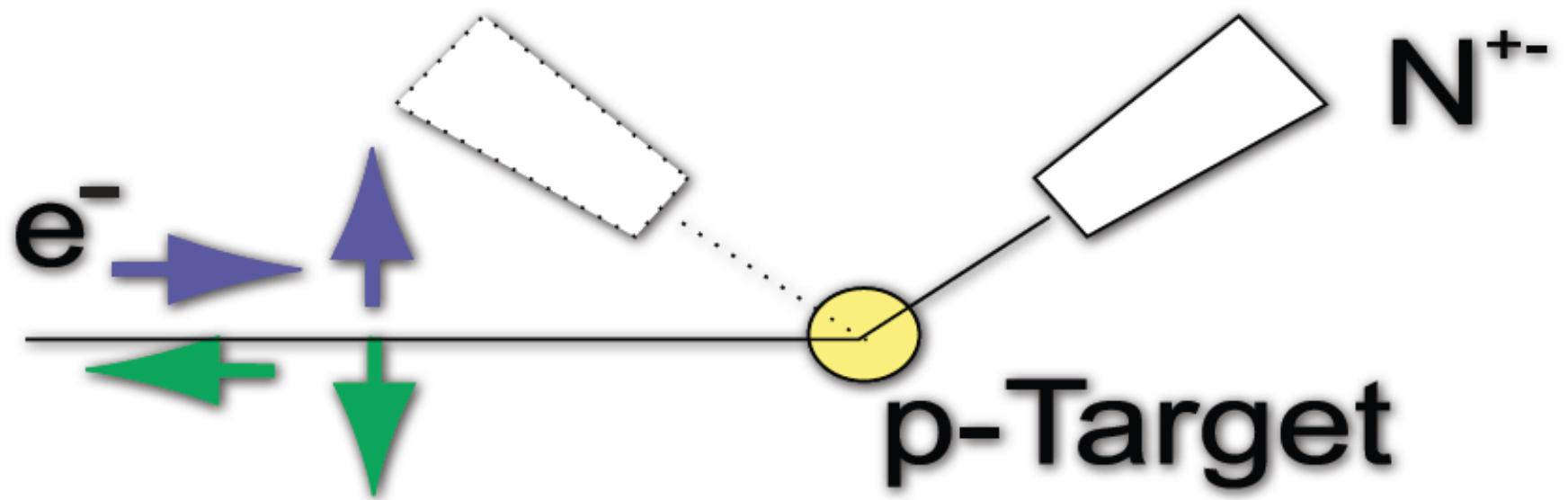
P2-Precision in $\sin^2 \theta_W$



	Total	Statistics	Polarization	Apparative	FF	$\text{Re}(\square_{yzA})$
$\Delta \sin^2(\theta_W)$	3.1e-4 (0.13 %)	2.6e-4 (0.11 %)	9.7e-5 (0.04 %)	7.0e-5 (0.03 %)	1.4e-4 (0.04 %)	6e-5 (0.03 %)
$\Delta A^{exp}/\text{ppb}$	0.44 (1.5 %)	0.38 (1.34 %)	0.14 (0.49 %)	0.10 (0.35 %)	0.11 (0.38 %)	0.09 (0.32 %)



Conceptually very simple experiments



$$A = (N^+ - N^-) / (N^+ + N^-) \quad \Delta A = (N^+ + N^-)^{-1/2} = N^{-1/2}$$

$$A = 20 \times 10^{-9} \quad 2\% \text{ Measurement} \quad N = 6.25 \times 10^{18} \text{ events}$$

Highest rate, measure Q^2 : Large Solid Angle Spectrometers

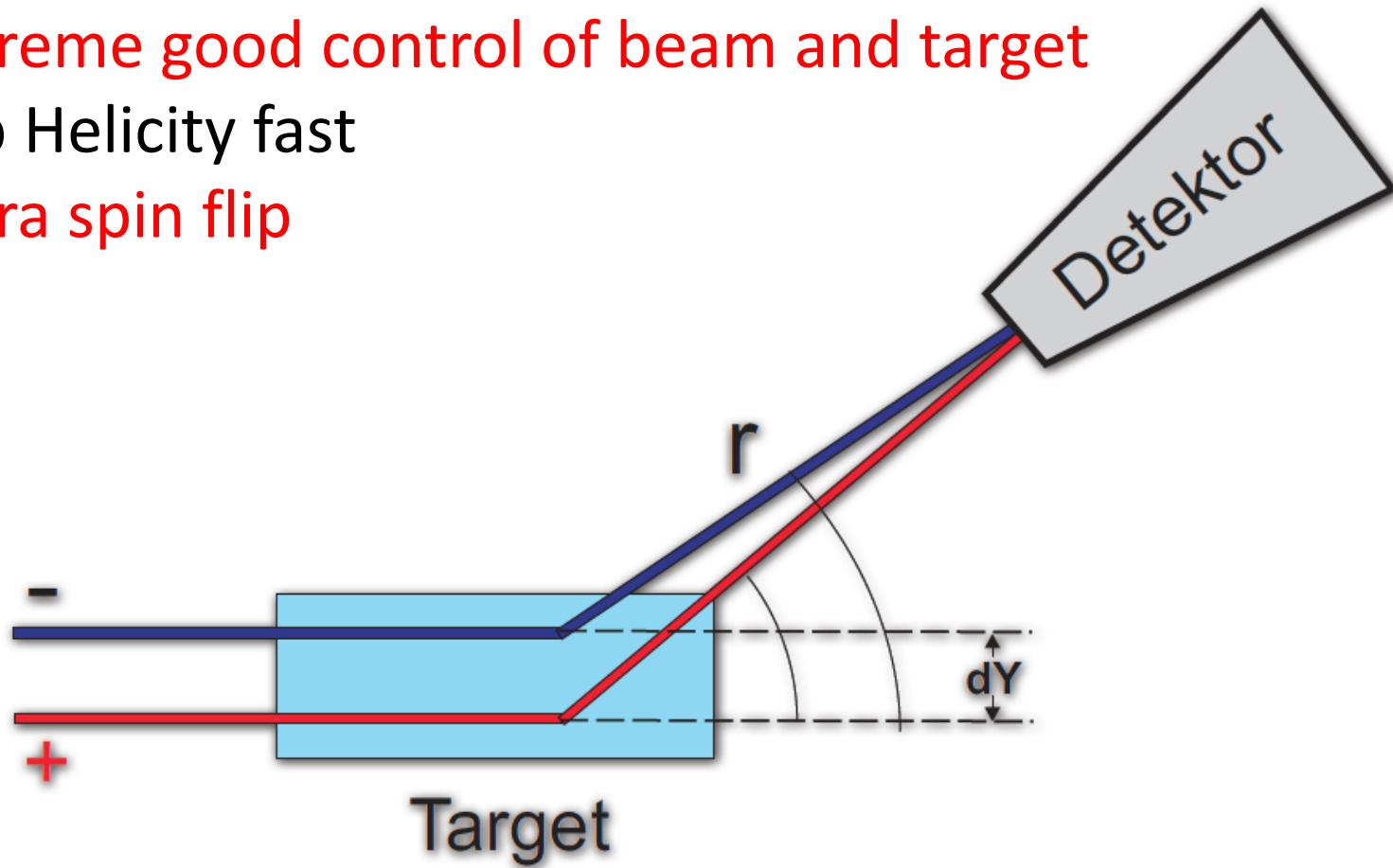


Apparative (false) asymmetries:

Extreme good control of beam and target

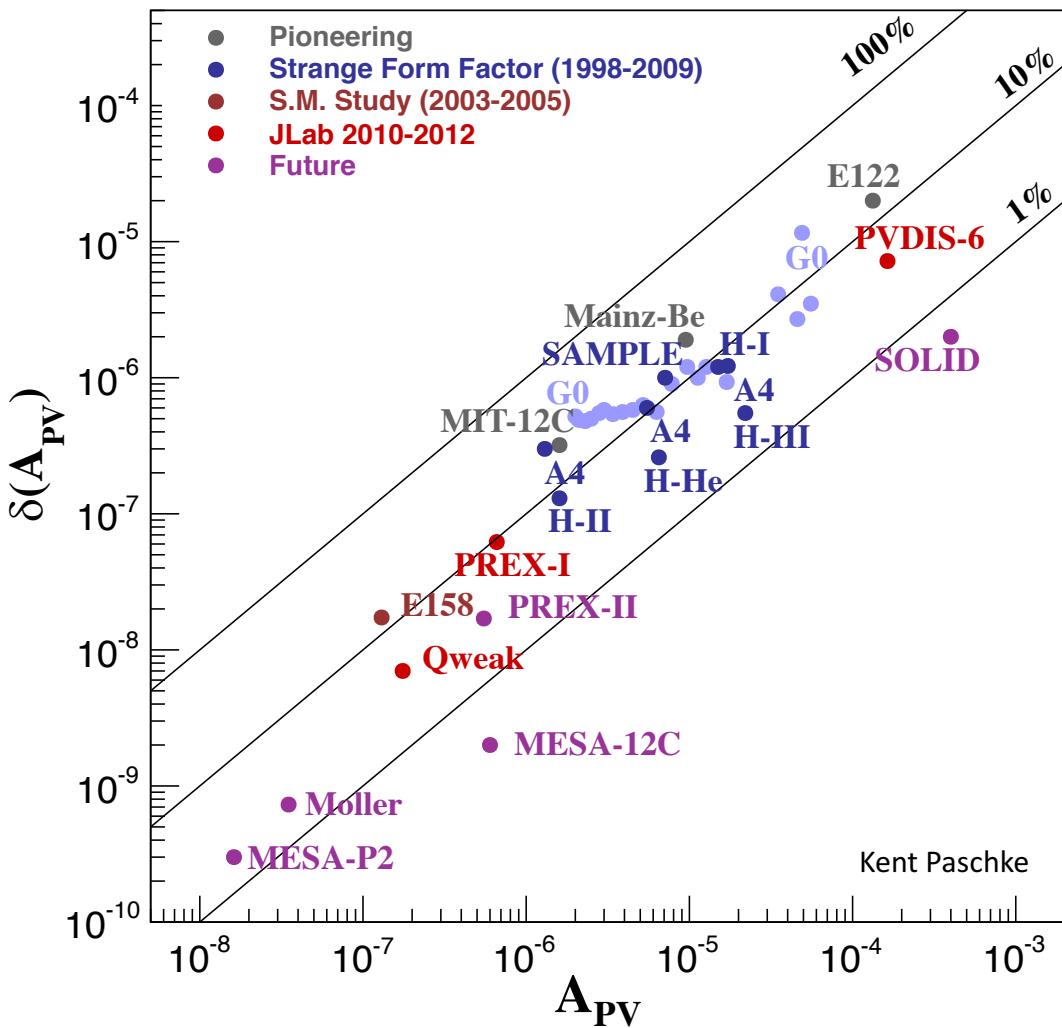
Flip Helicity fast

Extra spin flip



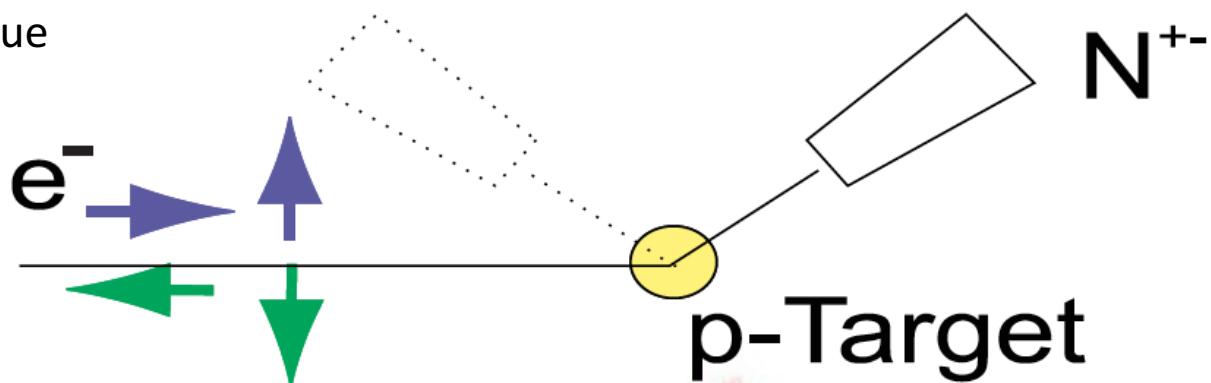


PVeS Experiment Summary





Counting Technique

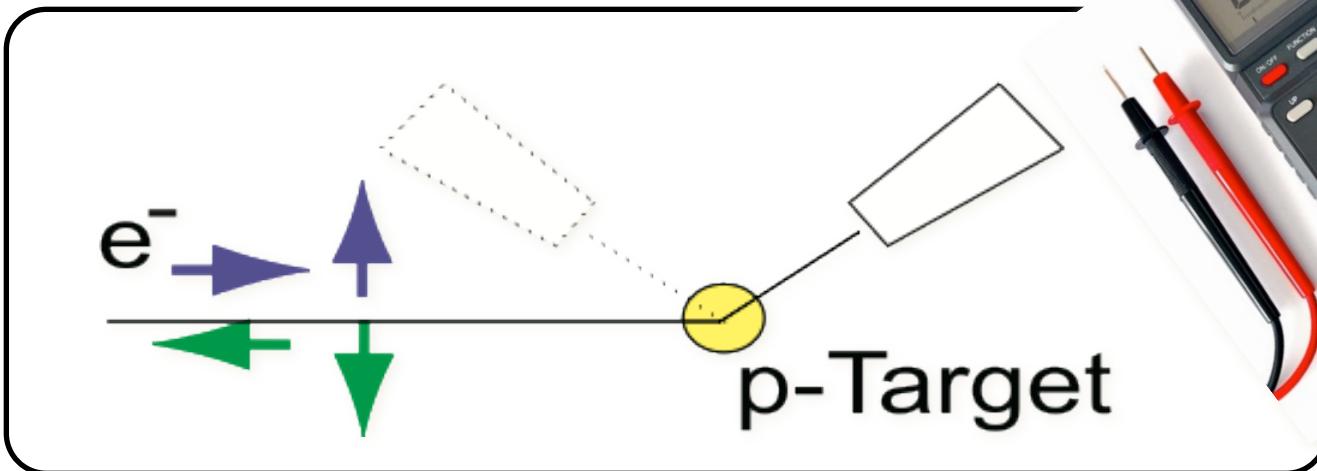


Count scattered electrons:

- pile-up (double count losses)
- Background Asymmetry
- Very Fast Counting (MHz)
- Measure TOF or Energy



Analogue Technique

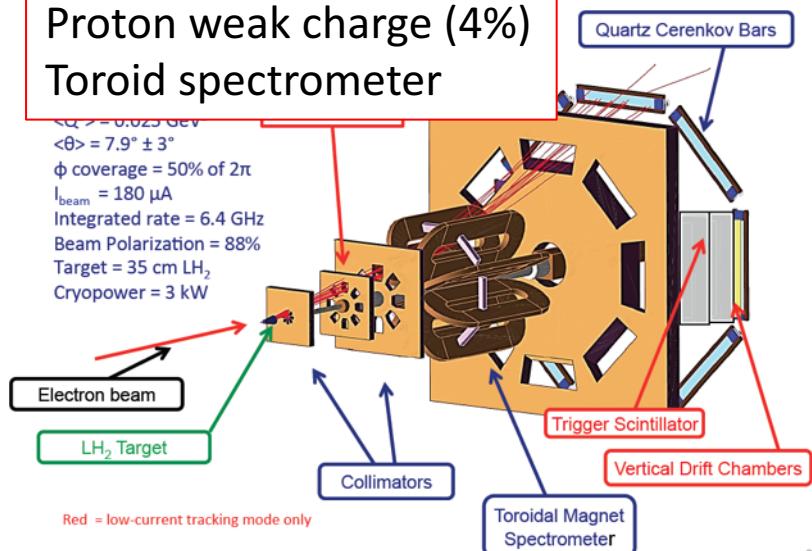


Measure Flux of Scattered electrons:

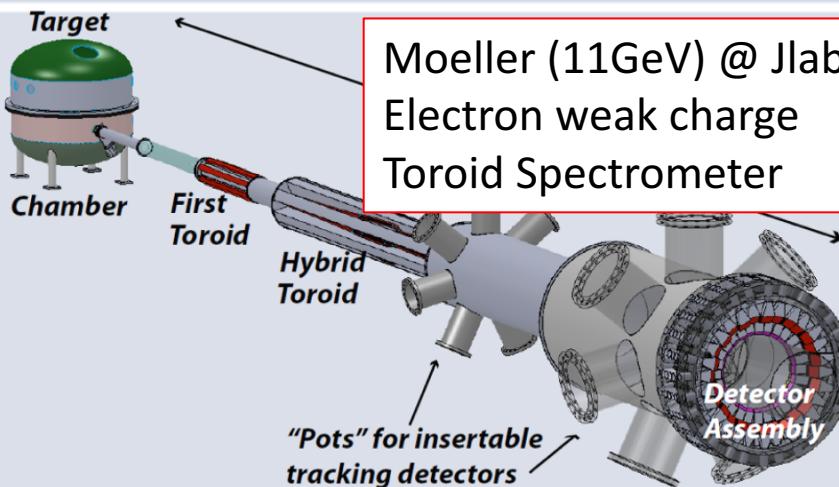
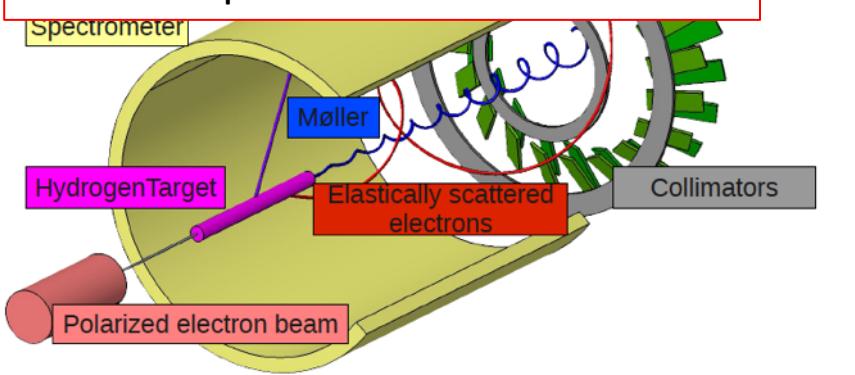
- no pile-up (double count losses)
- sensitive to small electr. fields.
- no separation of phys. process



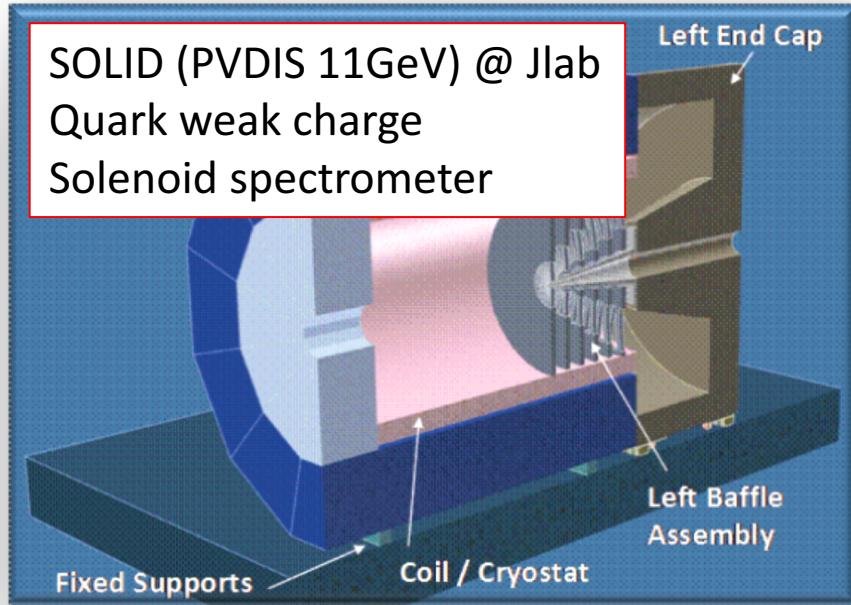
Qweak (1GeV) @ Jlab
Proton weak charge (4%)
Toroid spectrometer



P2@MESA (0.150 GeV) @ Mainz
Proton weak charge (1.7%)
Solenoid spectrometer



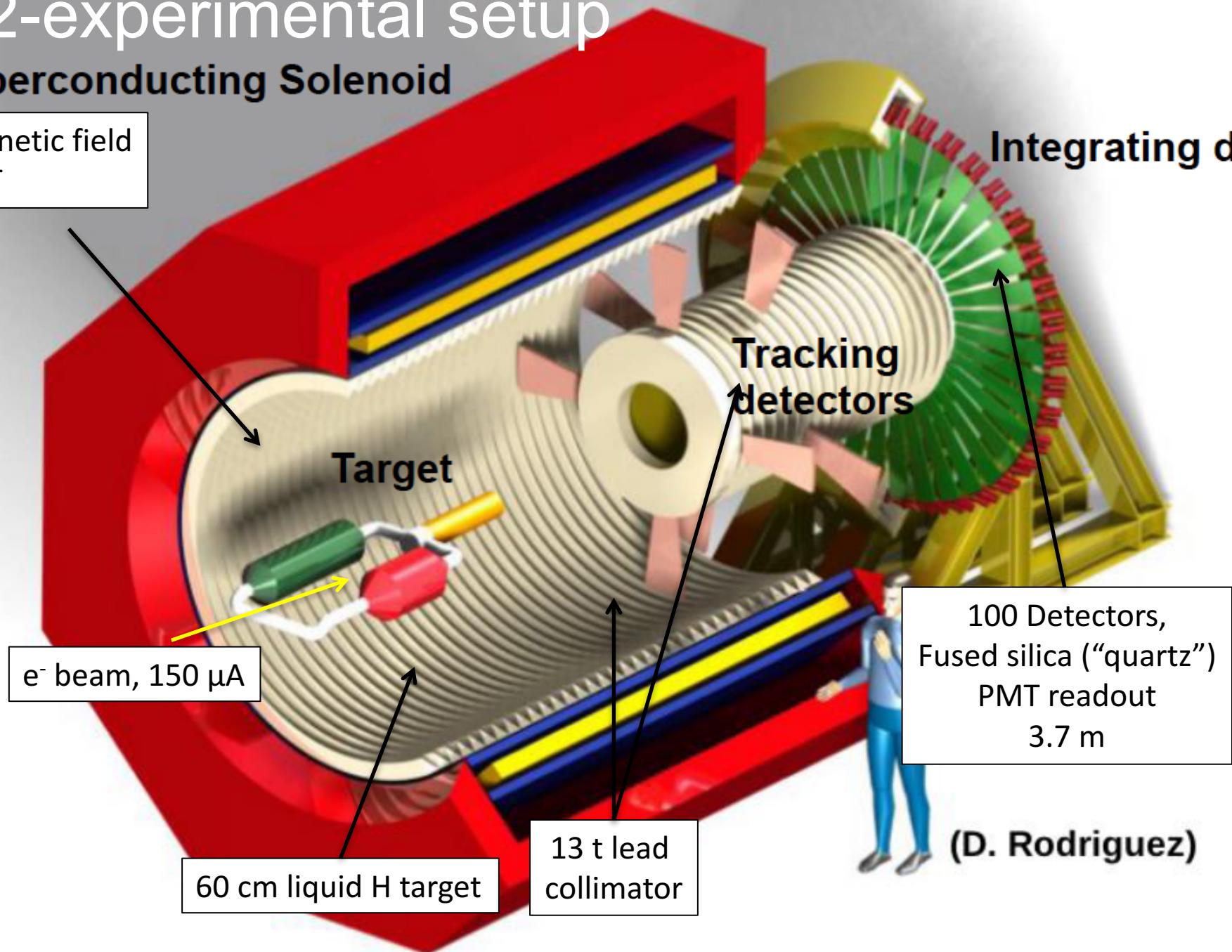
Moeller (11GeV) @ Jlab
Electron weak charge
Toroid Spectrometer



P2-experimental setup

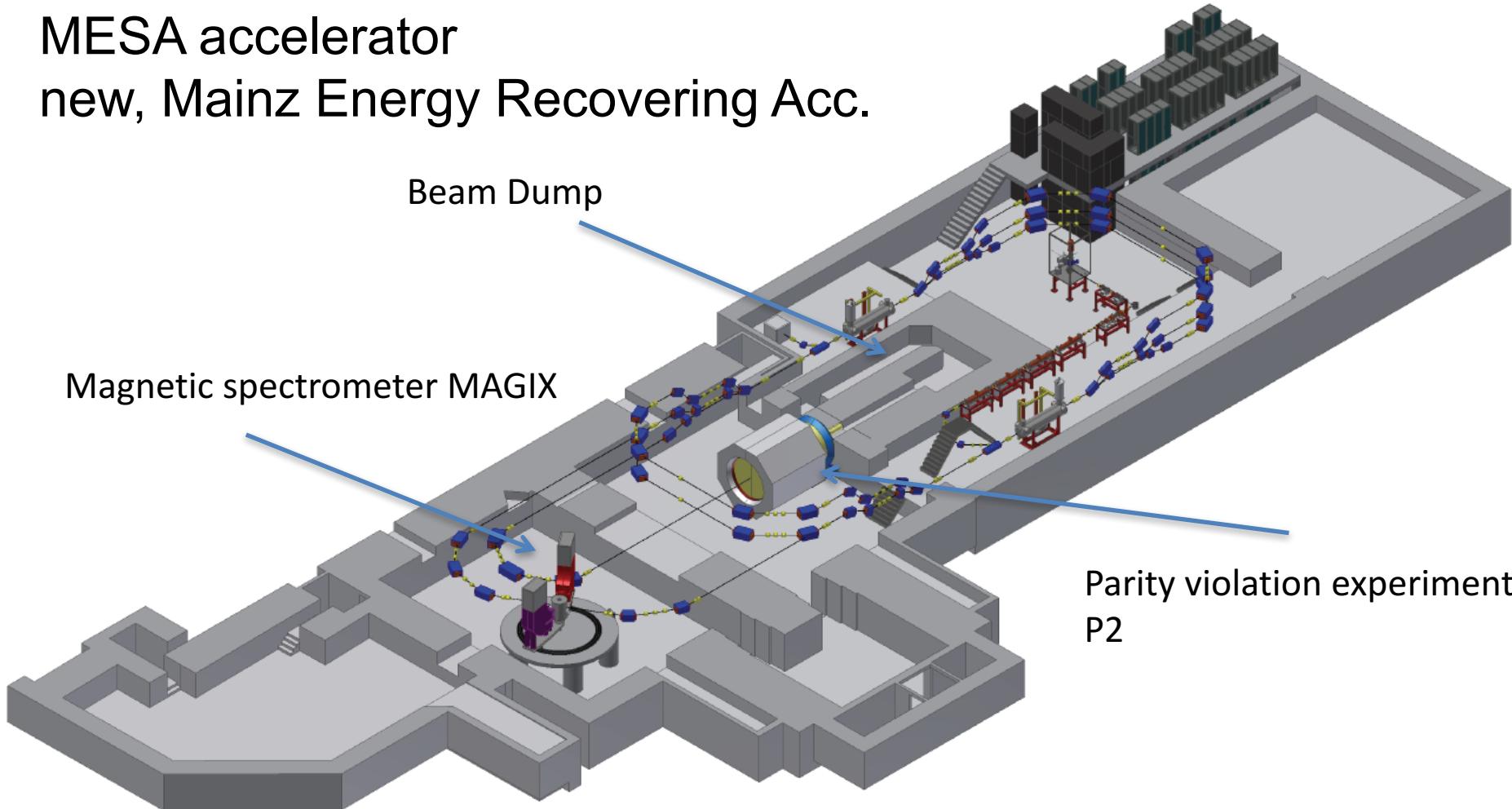
Superconducting Solenoid

Magnetic field
0.6 T





MESA accelerator new, Mainz Energy Recovering Acc.





- Parity violating electron scattering: “Low energy frontier” comprises a sensitive test of the standard model **complementary to LHC**
- Determination of $\sin^2(\theta_w)$ with high precision (same as Z-pole)
- P2-Experiment (proton weak charge) in Mainz under preparation
New MESA energy recovering accelerator at 155 MeV, target precision is 1.7% in Qweak i.e. 0.13% in $\sin^2(\theta_w)$, Sensitivity to new physics up to a scale of 49 TeV
- Much more physics from PV electron scattering
- Together with Moeller@Jlab (electron weak charge) and SOLID@Jlab (quark weak charge) very sensitive test of standard model and possibility to narrow in on Standard Model Extension

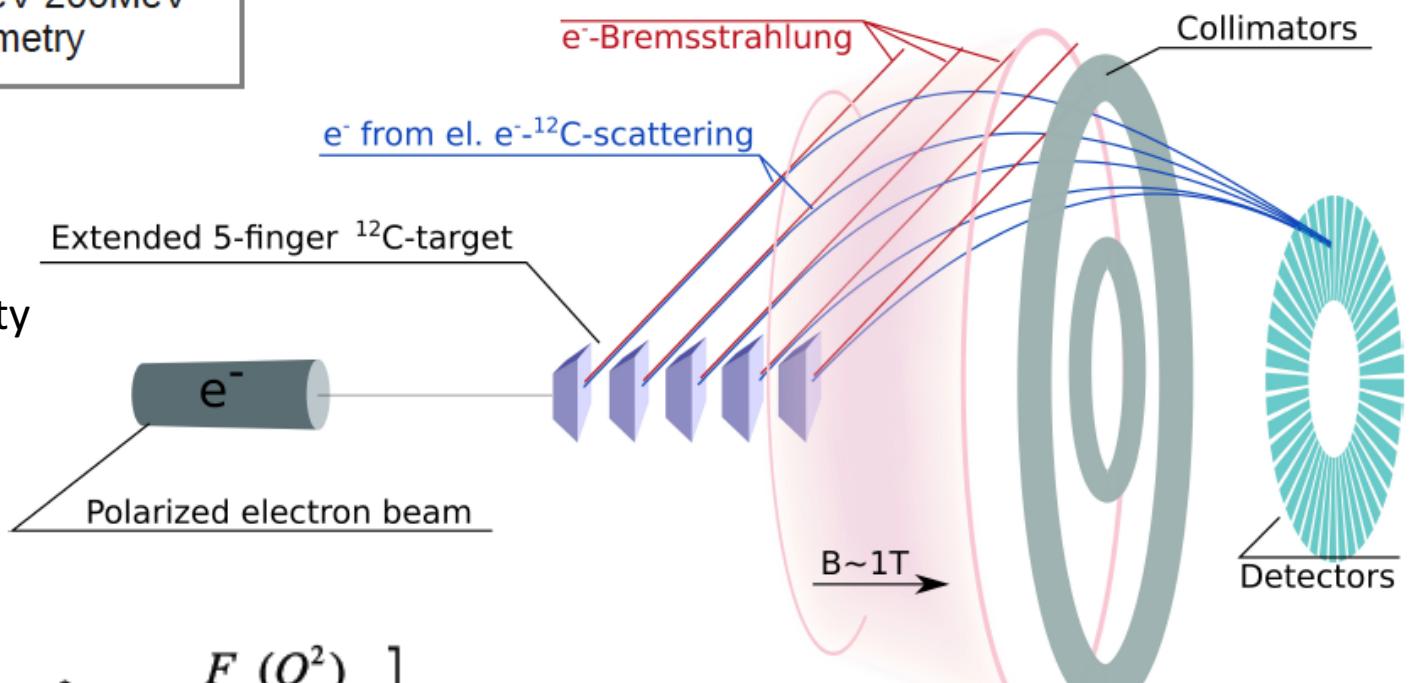


Other Measurements:
Carbon, Lead

EXPERIMENTAL REALIZATION

- MESA:
- 150 μ A
 - 150MeV-200MeV
 - Polarimetry

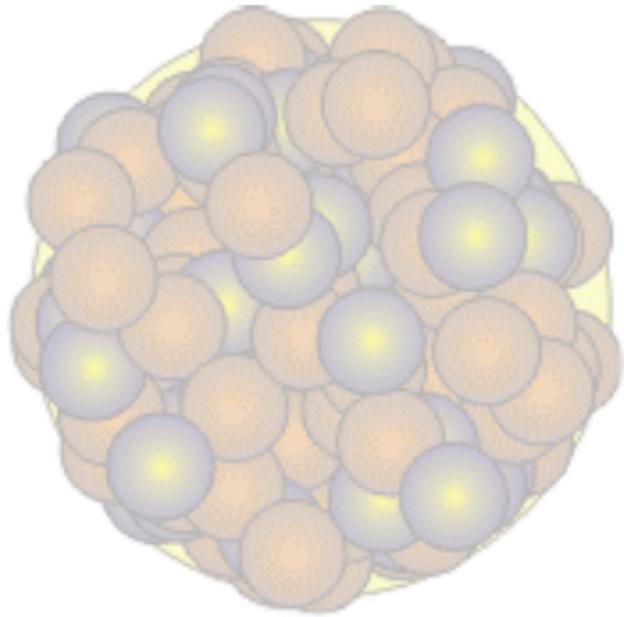
Enhanced sensitivity
To new physics



$$-N = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[\underbrace{\sin^2 \theta_W}_{\approx 0} - \frac{F_n(Q^2)}{F_p(Q^2)} \right]$$

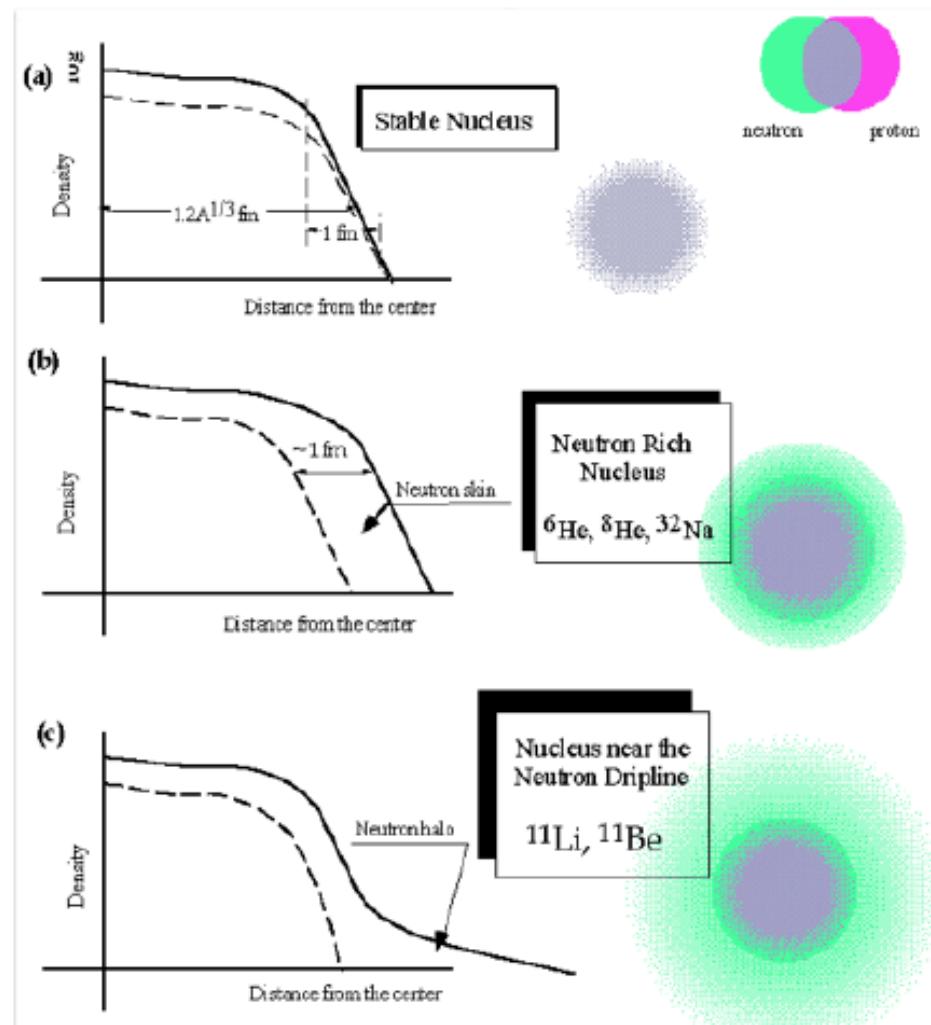
Neutron Skin for beginner

Where do the neutrons go?



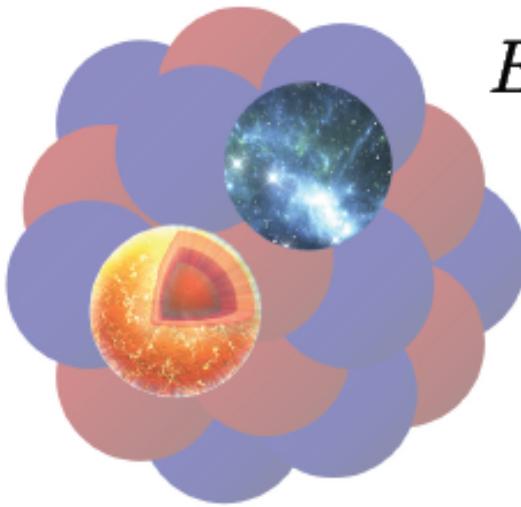
Pressure forces neutrons
out against surface tension

→ EOS



Measurement of neutron distribution in nuclei deceisive for Neutron star properties

WHY?



$$E(\rho, \delta) = E(\rho, 0) + E_{sym}(\rho) \delta^2 + \mathcal{O}(\delta)^4$$

symmetry energy

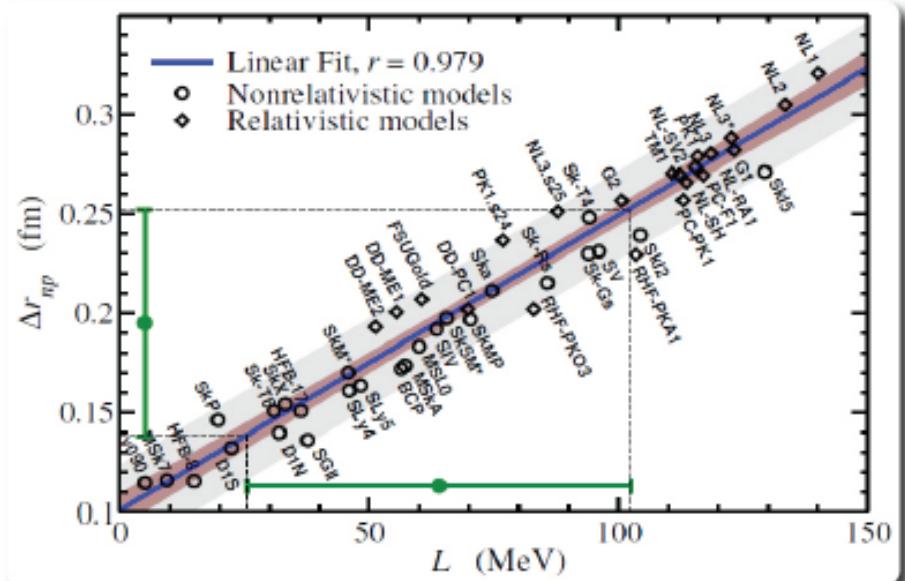
$$E_{sym}(\rho) = \left[S_v + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2 \right] + \dots$$

slope parameter

$$L = 3\rho_0 \frac{\partial E_{sym}(\rho)}{\partial \rho} \Big|_{\rho_0}$$

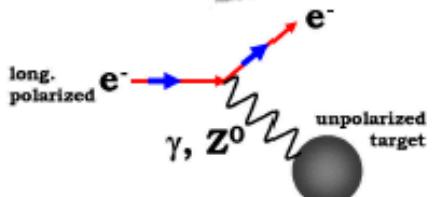
curvature parameter

$$K_{sym} = 9\rho_0^2 \frac{\partial^2 E_{sym}(\rho)}{\partial \rho^2} \Big|_{\rho_0}$$



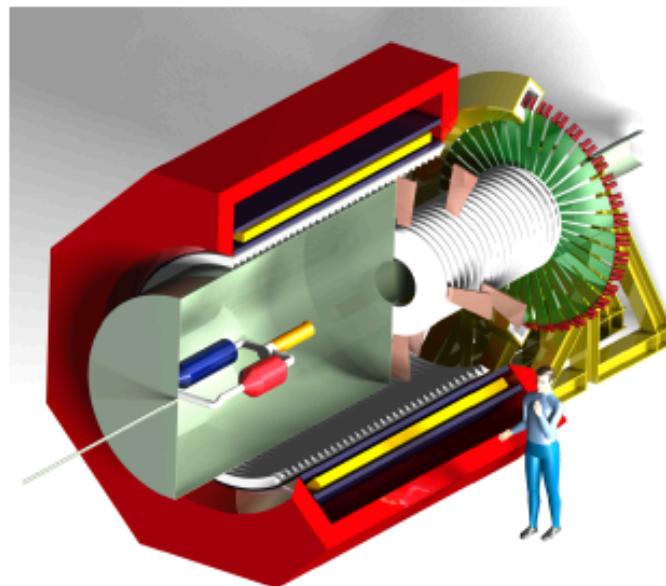
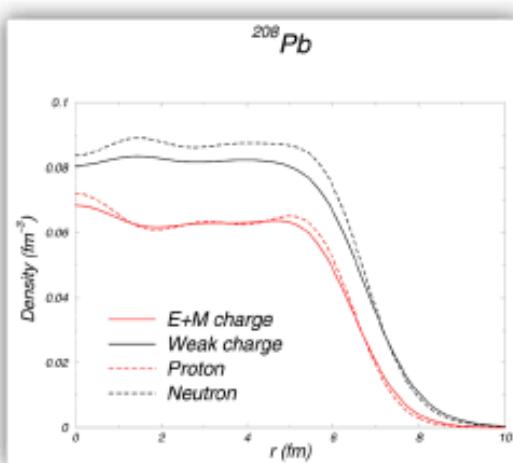
PVES

Enormously Clean ...
Extraordinarily Expensive!

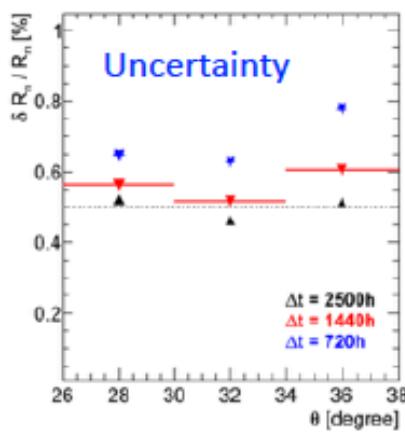
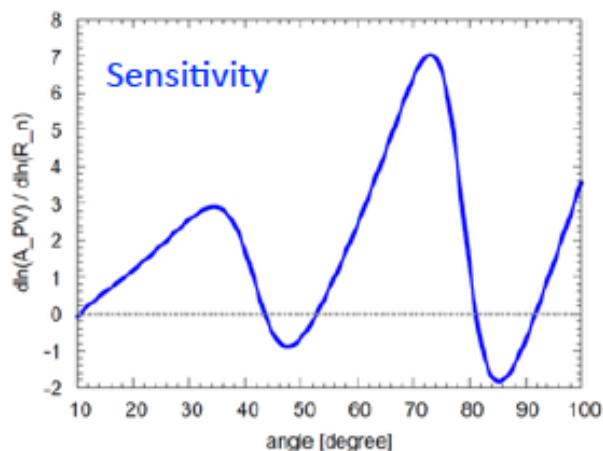


$$A_{PV} = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[1 - 4\sin^2\theta_W - \frac{F_n(Q^2)}{F_p(Q^2)} \right] \approx 0$$

$$F_{n,p}(Q^2) = \frac{1}{4\pi} \int d^3r \ j_0(qr) \rho_{n,p}(r)$$

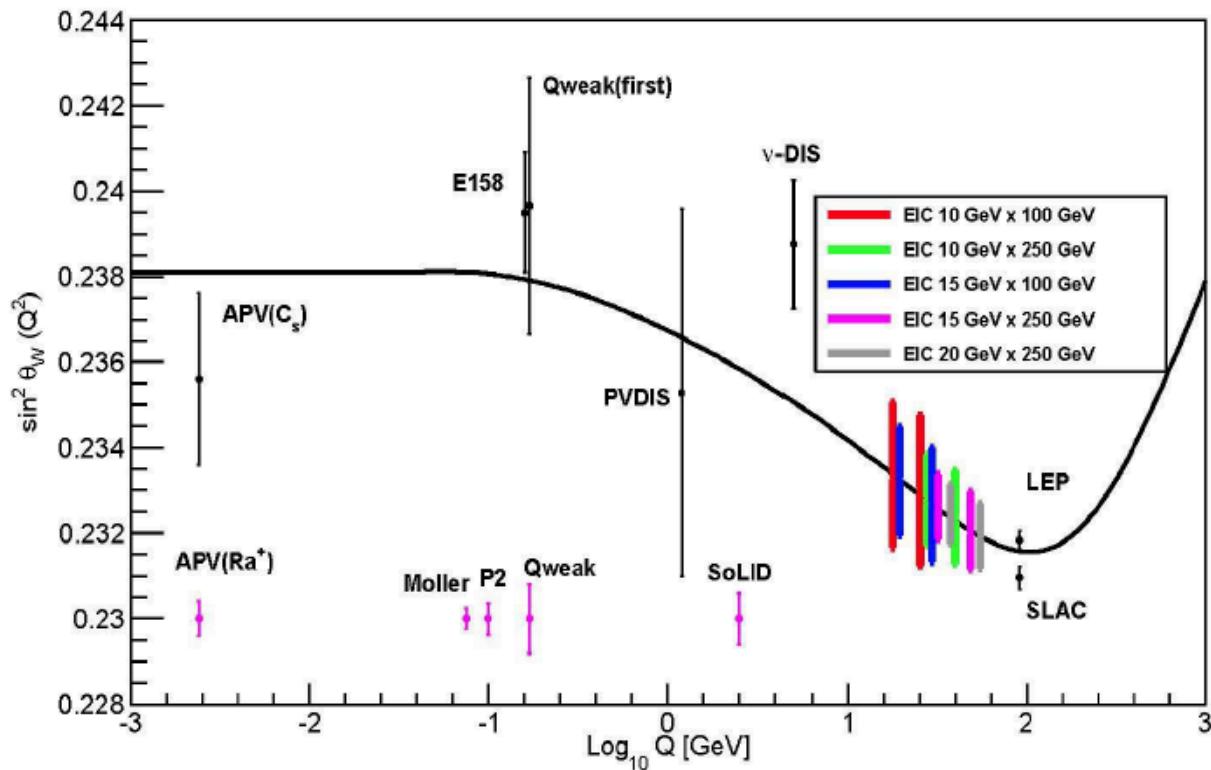


Full azimuthal coverage $\Leftrightarrow 4\times$ stat



Assuming same PREX luminosity:
 $\Delta\theta=4^\circ$: Rate=8.25 GHz, $A_{PV}=0.66$ ppm
1440h $\rightarrow \delta R_n/R_n = 0.5\%$
 (assuming 1% syst. $\delta A_{PV}/A_{PV}$)

World data of $\sin^2 \Theta_w$ including EIC projections



- 200 days of dedicated run
- Can reach similar precision to SoLID measurement
- Interesting Q^2 region never been measured or planned

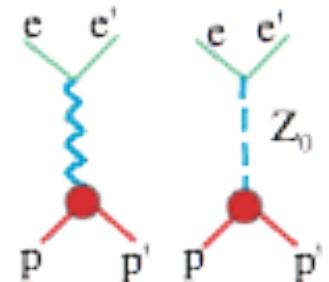


Beam Energy ERL/EB [MeV]	105/155 (105/205)
Operation mode	1300 MHz, c.w.
Elektron-sources	1.) Polarised : NEA GaAsP/GaAs superlattice , 200keV (?) 2.) unpolarised KCsSb, 200keV
Bunch Charge EB/ERL [pC] $7.7\text{pC}=\text{10mA@1300MHz}$	0.15/0.77 (0.15/7.7)
Norm. Emittance EB/ERL [μm]	0.1/<0.5 (0.1/<1)
Spin Polarisation (EB-mode only)	> 0.85
Recirculations	2 (3)
Beampower at Exp. ERL/EB [kW]	100/22.5 (1050/30)
R.f.-Power installed [kW]	140 (180)



Parity violating cross section asymmetry

$$A_{ep} = \left[\frac{G_F Q^2}{4\pi\alpha\sqrt{2}} \right] \frac{\epsilon G_E^\gamma G_E^Z + \tau G_M^\gamma G_M^Z - (1 - 4 \sin^2 \theta_W) \epsilon' G_M^\gamma G_A^Z}{\epsilon (G_E^\gamma)^2 + \tau (G_M^\gamma)^2}$$



$$A_{RL} = \underbrace{A_V + A_A}_{= A_0} + A_S \left\{ \begin{array}{l} A_V = -a\rho'_{eq} \left[(1 - 4 \sin^2 \theta_W) - \frac{\epsilon G_E^p G_E^n + \tau G_M^p G_M^n}{\epsilon (G_E^p)^2 + \tau (G_M^p)^2} \right] \\ A_A = a \frac{(1 - 4 \sin^2 \theta_W) \sqrt{1 - \epsilon^2} \sqrt{\tau(1 + \tau)} G_M^p \tilde{G}_A^p}{\epsilon (G_E^p)^2 + \tau (G_M^p)^2} \\ A_S = a\rho'_{eq} \frac{\epsilon G_E^p G_E^s + \tau G_M^p G_M^s}{\epsilon (G_E^p)^2 + \tau (G_M^p)^2} \end{array} \right.$$

$$a = -G_F q^2 / 4\pi\alpha\sqrt{2}, \quad \tau = -q^2 / 4M_p^2, \quad \epsilon = [1 + 2(1 + \tau) \tan^2 \theta / 2]^{-1}$$



Polarimetry (<0.5%)

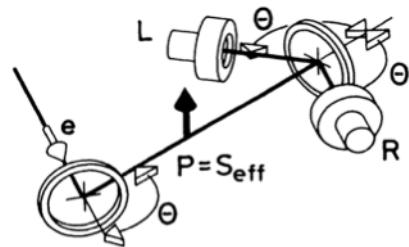


The double scattering Mott polarimeter:

Mott Polarimeter:

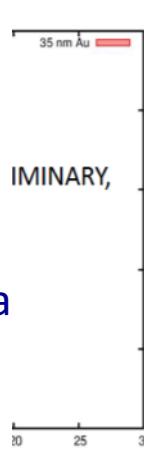
- Measuring left/right asymmetry to calculate spin polarisati
- Analysing power of target foils has to be extrapolated

A. Gellrich and J. Kessler, Phys. Rev. A 43, 204 (1991)



Double Scattering Polarimeter (DSP):

- Analysing power of the targets can be calculated directly from measurements
- Allows for higher precision measurement of spin polarisation
- Invasive polarimetry at the electron source
- Scattering chamber in operation, first double scattering data





Hydro Möller Polarimeter

The promise:(*)

- **Hydro-Möller: Atomic trap with completely electron-spin polarized Hydrogen**
- **Online capability, high accuracy (<0.5%)**
- **Statistical efficiency approaches 0.5% in 2 hours**
(Target: $3 \times 10^{-16} \text{ cm}^{-2}$)
- **Acceptance similar to conventional Möller**

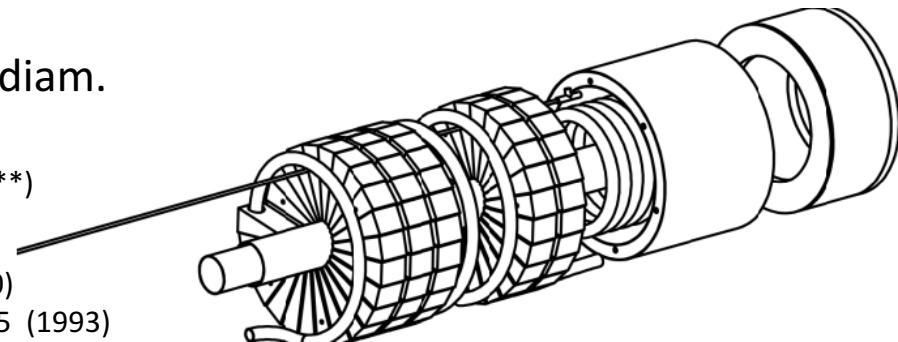
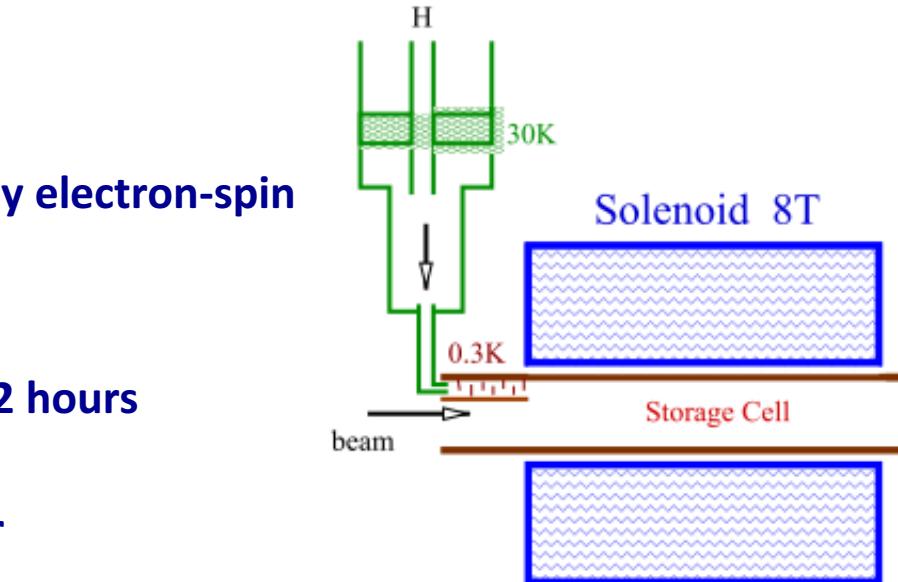
(*)E. Chudakov, V. Luppov: IEEE Trans. Nucl. Sc. 51, 1533 (2004)



Complete trap with 77mm diam.
Cold bore 7T Solenoid
 $\Delta B/B < 10^{-5}$ (1cm³ Volume)(**)

(*): T. Roser et. al. NIM A 301 42-46 (1990)

(**): W. Kaufmann et. al. NIM A 335 17-25 (1993)



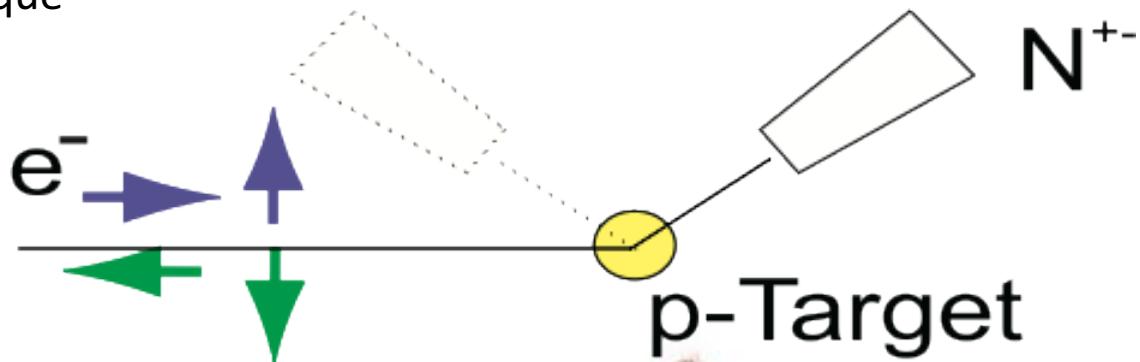
1.1K Stage heat exchangers
Presently in fabrication in KPH
Machine shop



Detector Concept



Counting Technique



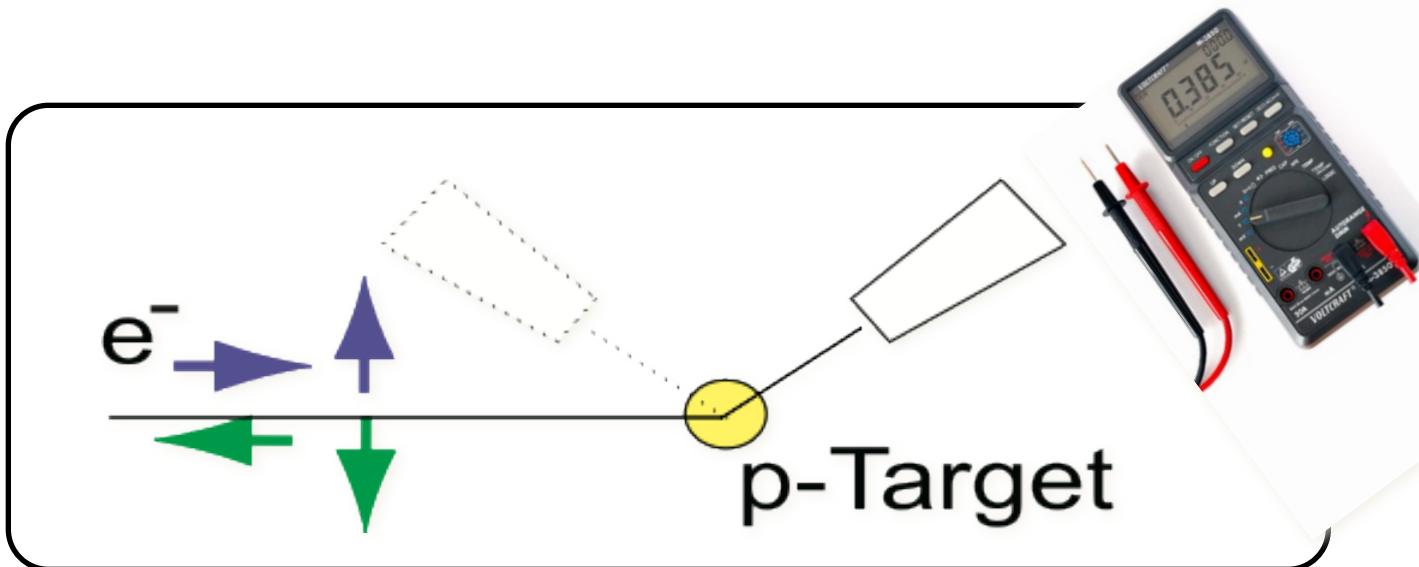
Count scattered electrons:

- pile-up (double count losses)
- Background Asymmetry
- Very Fast Counting (MHz)
- Measure TOF or Energy

A4: 100 MHz
P2: 440 GHz



Analogue Technique



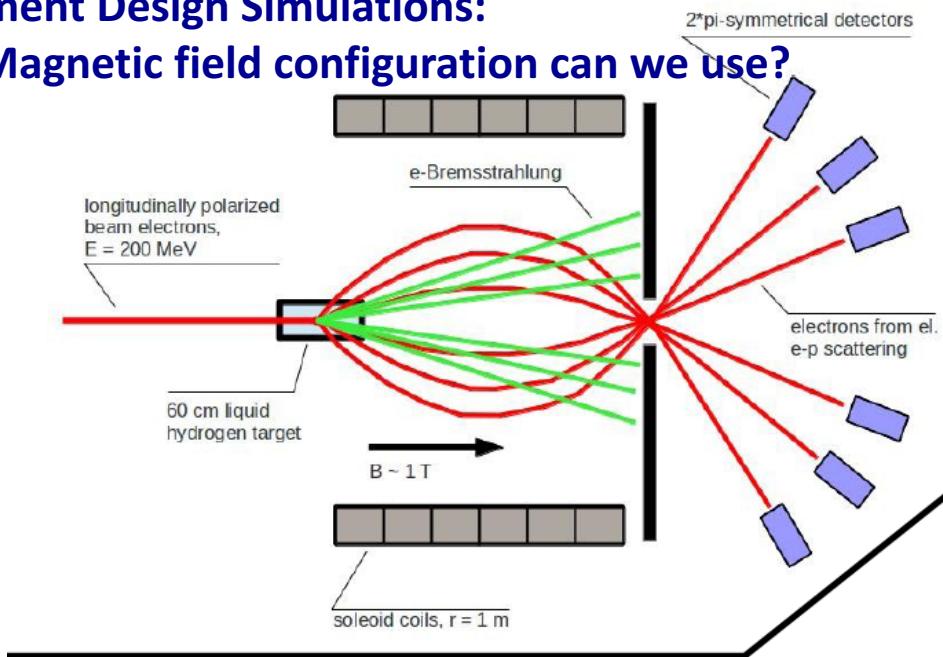
Measure Flux of Scattered electrons:

- no pile-up (double count losses)
- sensitive to small electr. fields.
- no separation of phys. process



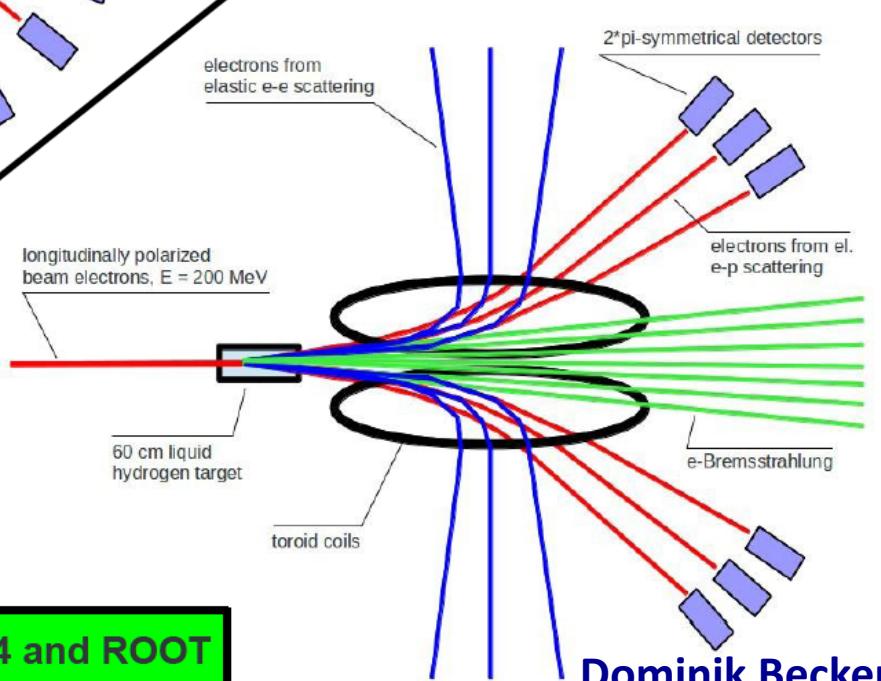
Experiment Design Simulations:

What Magnetic field configuration can we use?

Solenoid:

- Full azimuthal coverage
- Compact setup
- Superconducting coils

P. Souder in "Parity violation in electron scattering"
Proceedings of a workshop at CalTech
Ed: E. J. Beise and R. D. McKeown
World Scientific, 1990

Toroid:

- Loss of ~50% solid angle
→ double measurement time
- Larger setup
- Copper coils

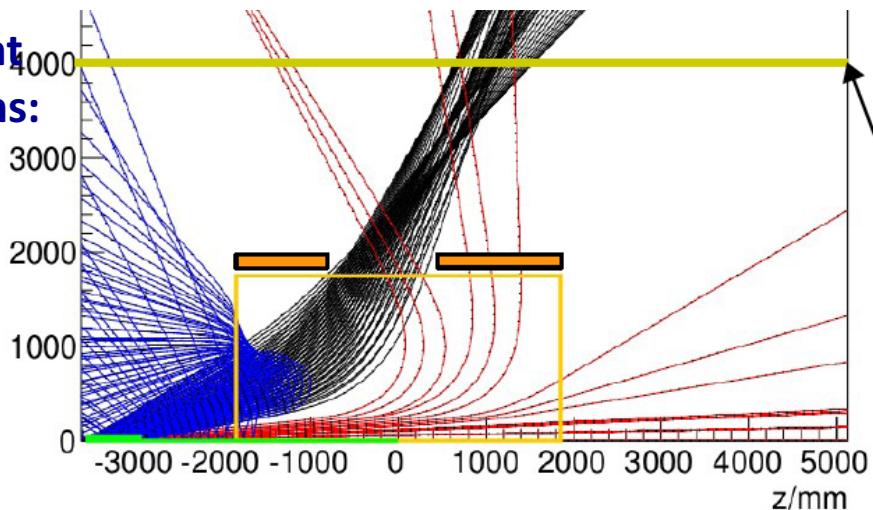


Feasibility study with Geant4 and ROOT

Dominik Becker



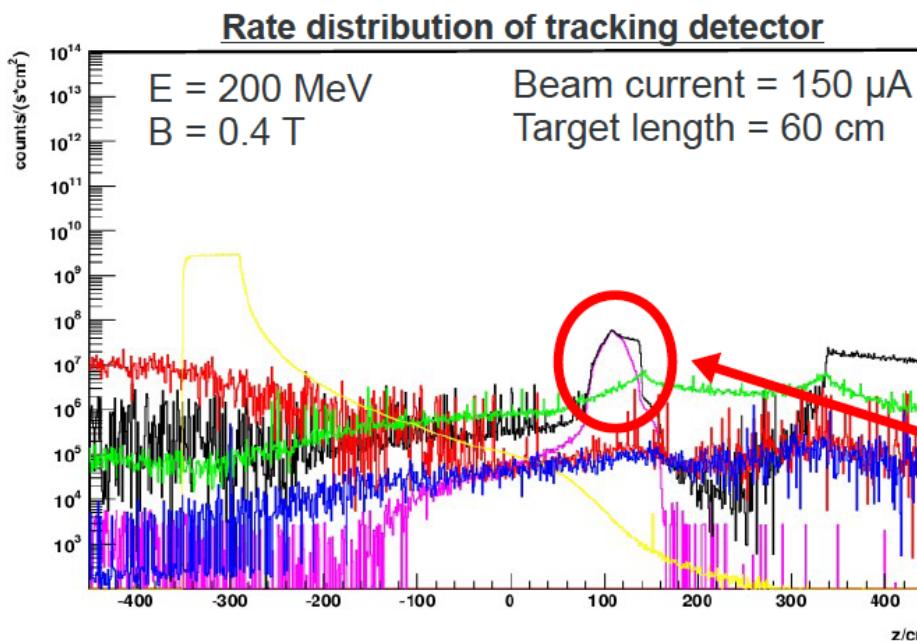
Experiment
Simulations:
Toroid
possible!



- el. e-p scattering
- Moeller scattering in $[0^\circ, 5^\circ]$
- Moeller scattering in $[10^\circ, 30^\circ]$

Simple tracking detector:

- Consists of vacuum
- Analyses particles that fly through



- e-, el. e-p scattering, $[10^\circ, 75^\circ]$
- e-, el. e-p scattering, $[10^\circ, 30^\circ]$
- e-, background
- e+
- γ
- p

Dominated by el. e-p scattering
 $\theta \in [10^\circ, 30^\circ]$



Experiment

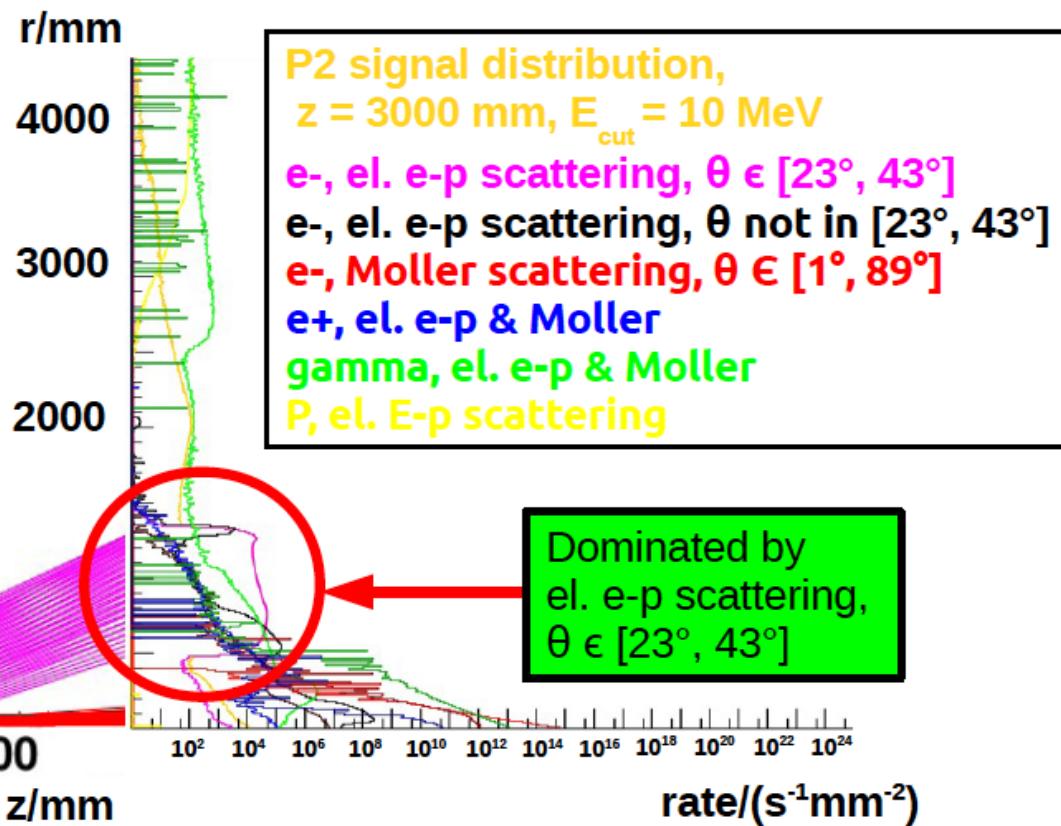
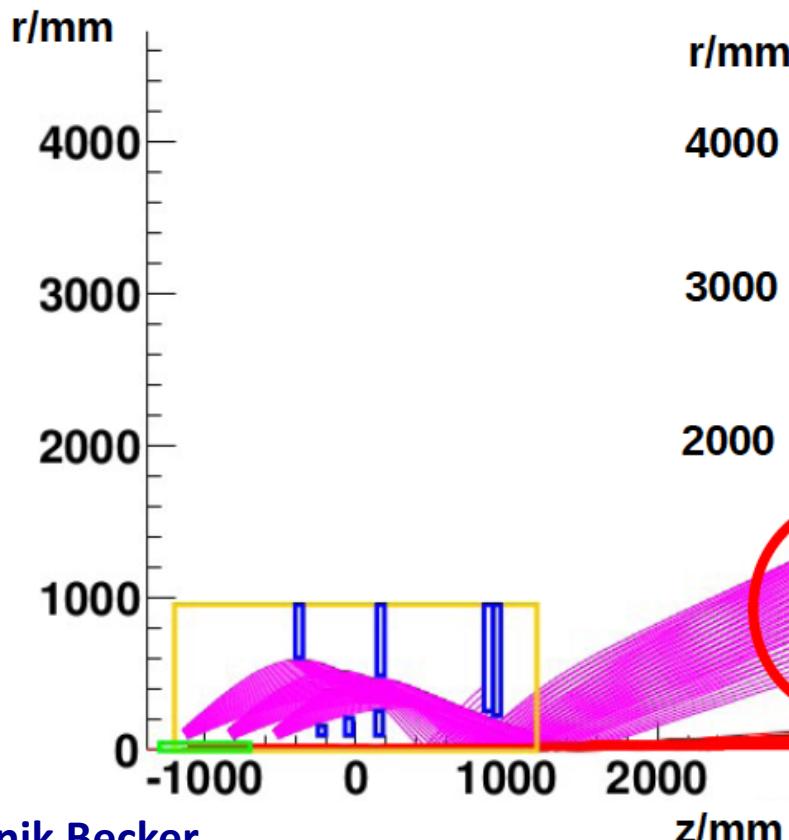
Design

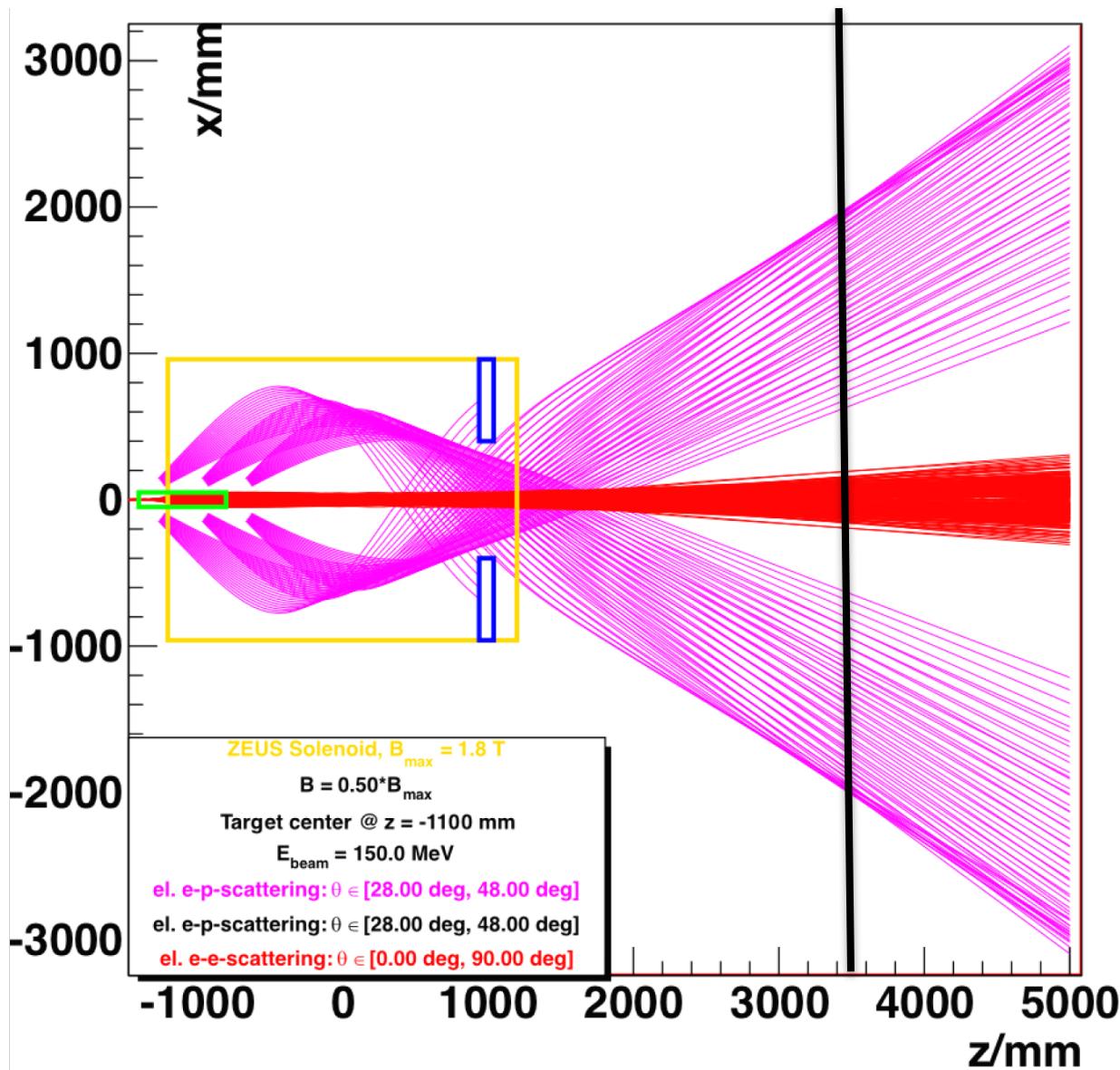
Simulations:

Solenoid
possible!

$E = 150 \text{ MeV}$
 $B = 1.08 \text{ T}$
el. e-p scattering, $\theta \in [23^\circ, 43^\circ]$
Moller scattering, $\theta \in [1^\circ, 89^\circ]$

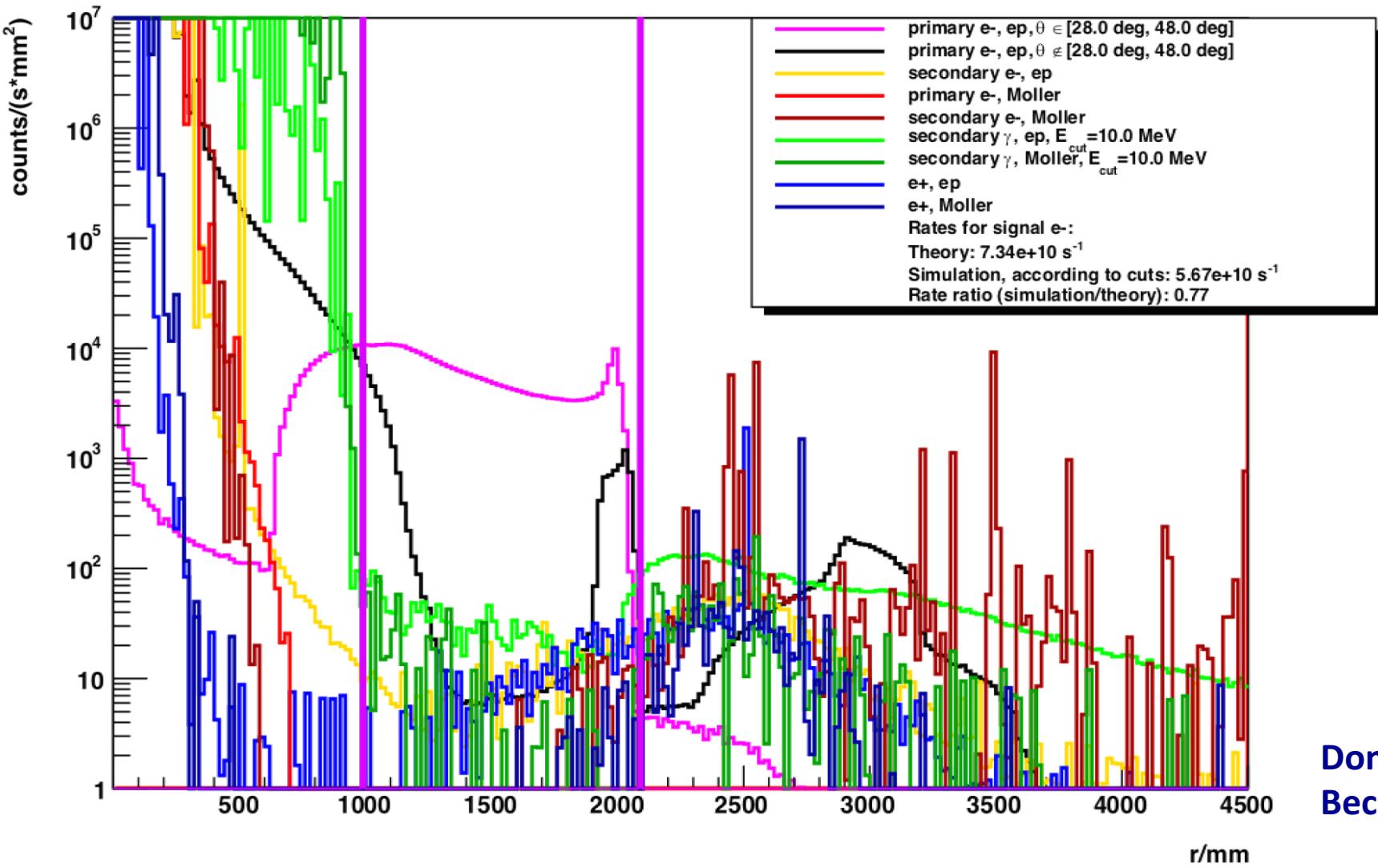
Primary event generators of
Monte Carlo simulation:
el. e-p scattering, $\theta \in [1^\circ, 90^\circ]$
Moller scattering, $\theta \in [1^\circ, 89^\circ]$

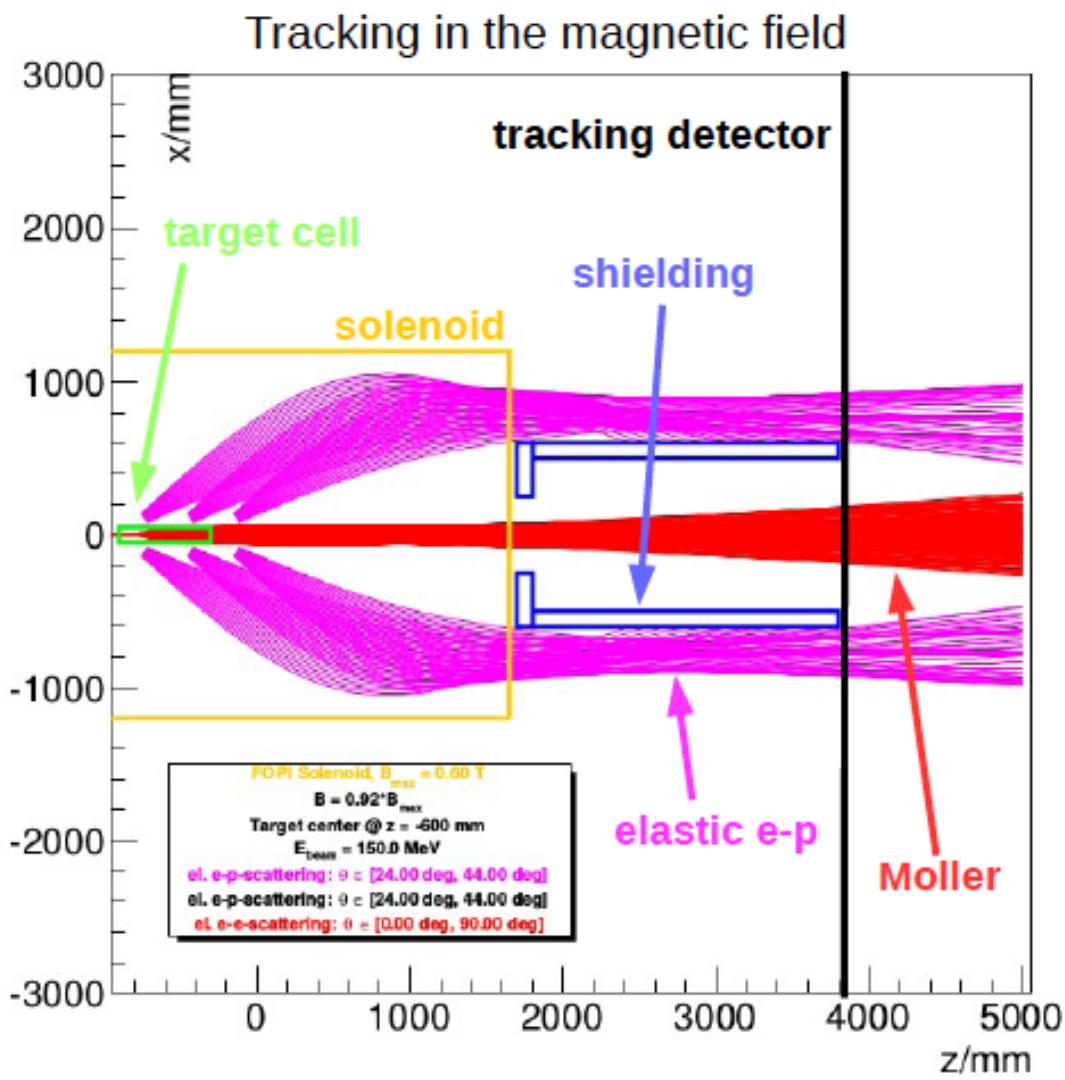


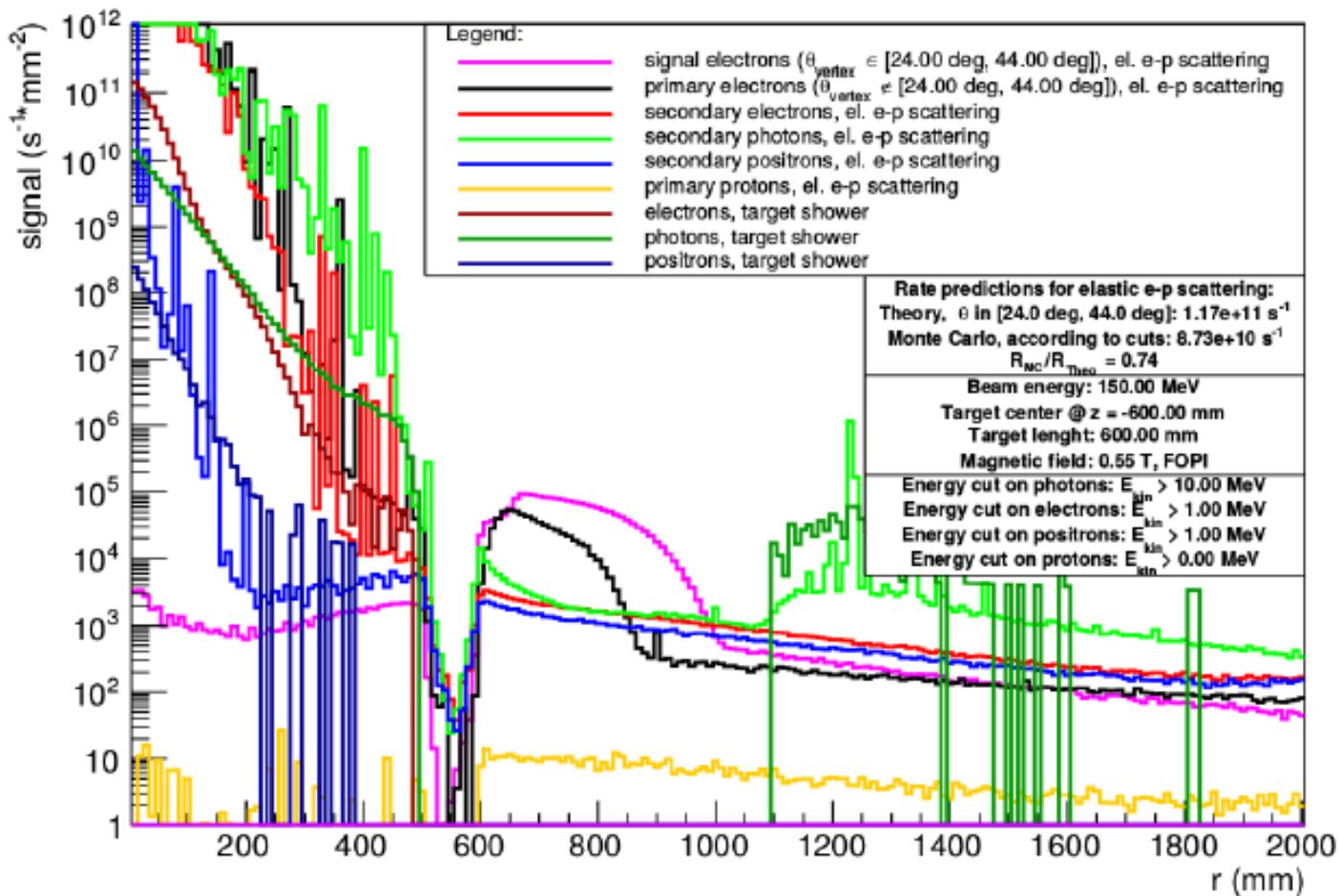


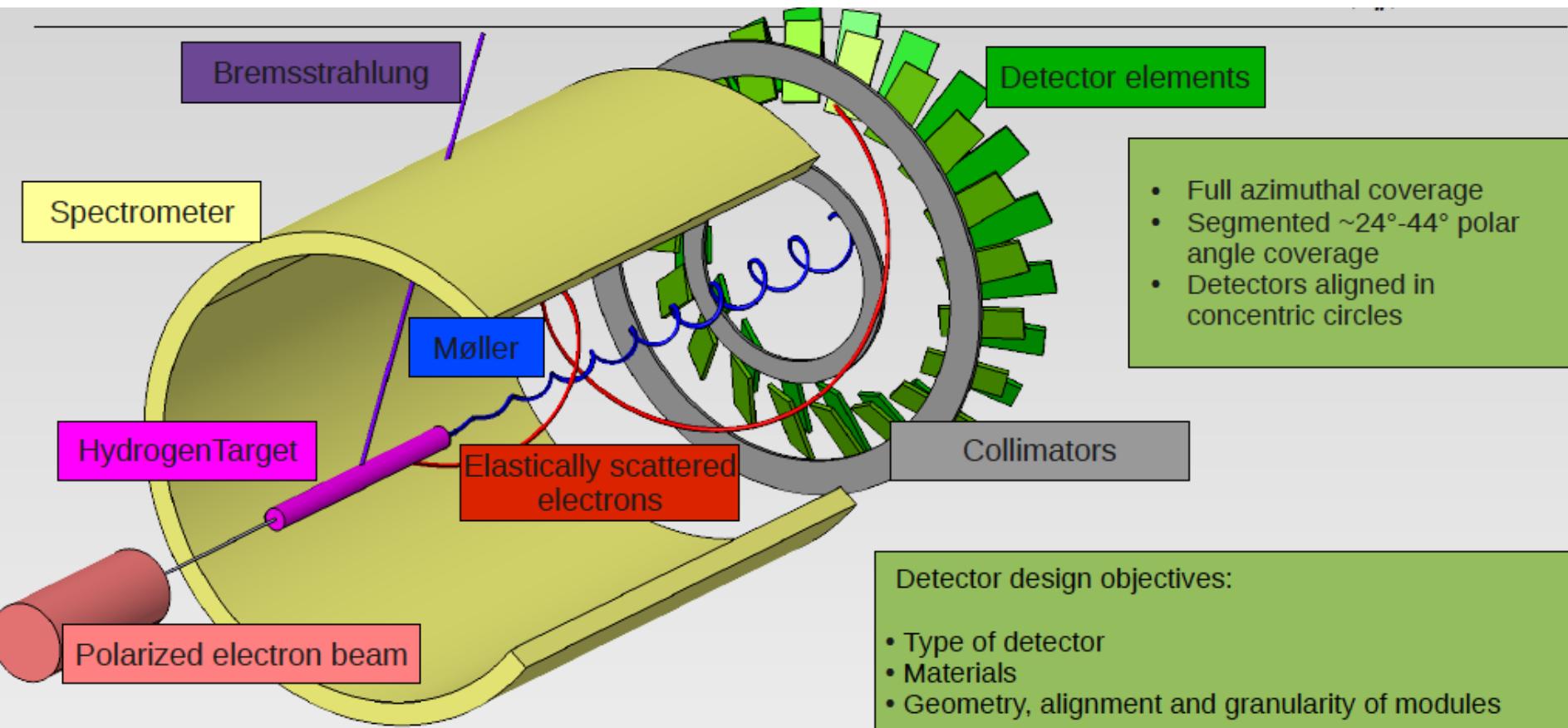


Rate distribution in tracking detector nb 1 @ z = 3500 mm

Dominik
Becker



Rate distribution @ $z = 3810.00$ mm

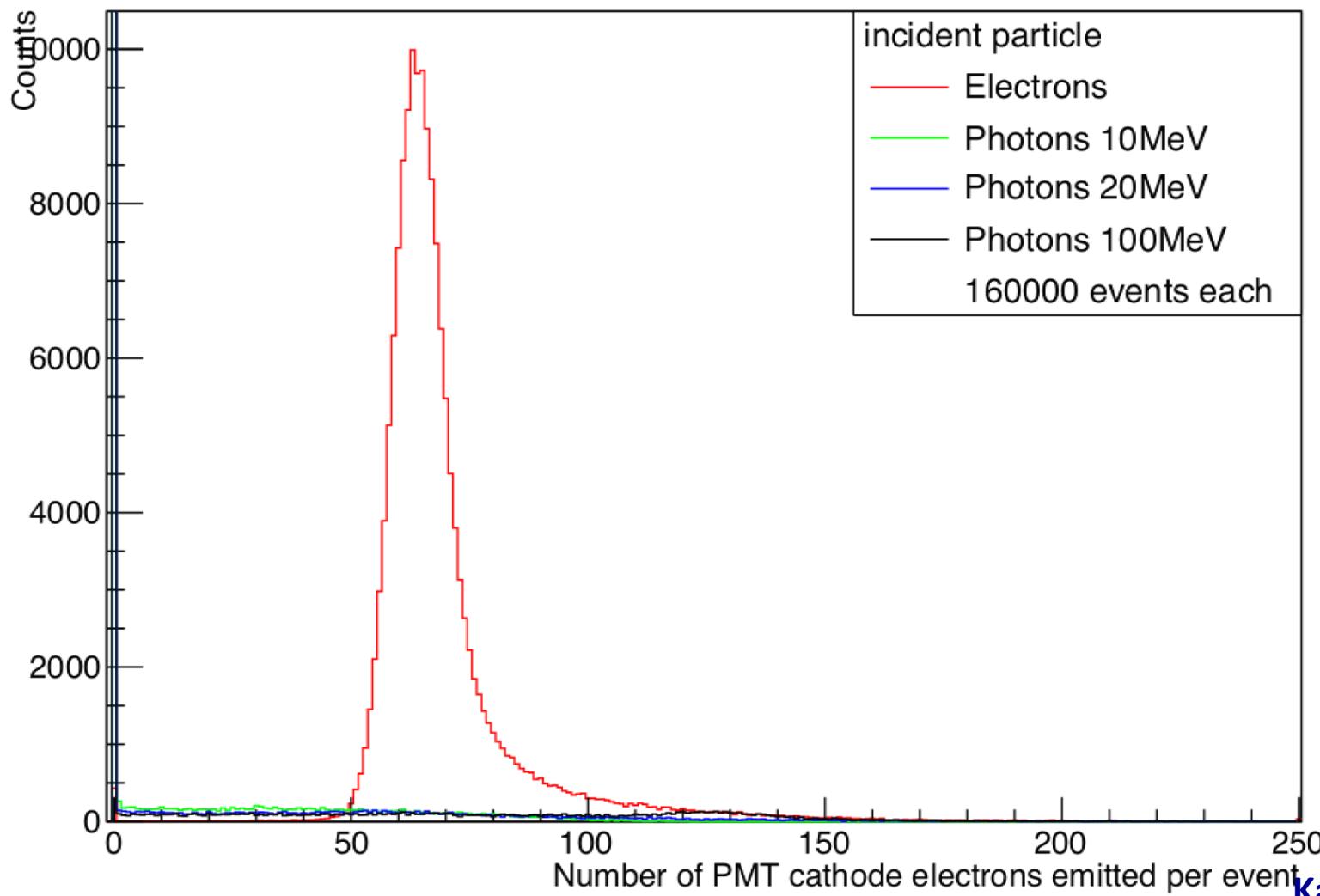


Detector design objectives:

- Type of detector
- Materials
- Geometry, alignment and granularity of modules



Number of PMT cathode electrons emitted per event





Number of PMT cathode electrons emitted per event

