The Electroweak Box

M.J. Ramsey-Musolf

U Mass Amherst



AMHERST CENTER FOR FUNDAMENTAL INTERACTIONS Physics at the interface: Energy, Intensity, and Cosmic frontiers University of Massachusetts Amherst

http://www.physics.umass.edu/acfi/

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Goals For This Talk

- Set the context for the workshop
- Introduce topics to be addressed in more detail during following talks & discussions
- Pose some challenges for the future

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Caveat: I will not provide a comprehensive review, and some results are undoubtedly out of date. Omissions are not intentional, and I welcome corrections, updates, and other input!

Outline

- I. Context
- II. PV Electron Scattering
- III. CC Weak Interactions
- IV. Time Reversal
- V. Workshop Questions



Two EW Boson Exchange



Two EW Boson Exchange



- QED ($\gamma\gamma$) in semileptonic interactions is still a puzzle !
- No direct probes of EW boxes (γZ, γW) available, but reliable SM computations needed. Can we trust the quoted theoretical uncertainties ? Can we reduce them further ?

Two-boson exchange in semileptonic processes: important for elastic PV eN & eA scattering (¹²C) & nuclear β -decay; beam normal asymmetry, Olympus... provide tests



 $V = Z^0, W, \gamma$

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Two EW Boson Exchange



	dσ	A_n	A_{PV}	ft _{1/2}	а,А	δ(Ε)	d_A
γγ	~	~	~	×	×	×	~
γΖ	×	×	~	×	×	×	×
γW	×	×	×	~	~	~	×

Two-boson exchange in semileptonic processes: important for elastic PV eN & eA scattering (¹²C) & nuclear β -decay; beam normal asymmetry provides, Olympus... provide tests



Proposal: (1) carry out a consistent set of computations for A_n , PV asymmetry, & δ_{NS} using different methods (2) develop a program of A_n measurements to test computations



II. PV Electron Scattering

Parity-Violation & Weak Charges



Parity-Violating electron scattering

$$A_{PV} = \frac{N_{\uparrow\uparrow} - N_{\uparrow\downarrow}}{N_{\uparrow\uparrow} + N_{\uparrow\downarrow}} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} \Big[Q_W + F(Q^2, \theta) \Big]$$

Atomic parity-violation

 $E_1^{PV} / \beta = i e \mathcal{M} \times 10^{-11} a_0 (Q_W / N) / \beta$

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Assume SM NC correct & use to probe hadron & nuclear struture

Parity-Violation & Neutral Currents



R. Carlini, PANIC 2017 Beijing

Weak Mixing in the SM: Uncertainties

$$\hat{s}^2 \frac{d\hat{\alpha}}{dt} - \hat{\alpha} \frac{d\hat{s}^2}{dt} = \frac{b_2}{\pi} \hat{\alpha}^2 + \sum_j \frac{b_{2j}}{\pi^2} \hat{\alpha}^2 \hat{\alpha}_j + \cdots$$

$$\sin^2 \hat{\theta}_W(\mu) = \frac{\hat{\alpha}(\mu)}{\hat{\alpha}(\mu_0)} \sin^2 \hat{\theta}_W(\mu_0) + \frac{\sum_i N_i^c \gamma_i Q_i T_i}{\sum_i N_i^c \gamma_i Q_i^2} \bigg[1 - \frac{\hat{\alpha}(\mu)}{\hat{\alpha}(\mu_0)} \bigg],$$

Full $SU(2)_1 \times U(1)_Y RGE$

Erler & R-M

Relate running of $\sin^2 \theta_W$ to running of α

1. Run α & sin² θ_W to $\mu \sim m_c$

2. Bound s-quark contribution to $\alpha(m_c)$ -- relative to u and d contributions -- using heavy quark and SU(3)_f limits Uncertainties: $sin^2 \theta_W(0)$ +/- 3 x 10⁻⁵ : $\Delta \alpha^{(3)}(m_c)$ +/- 5 x 10⁻⁵: $\Delta \alpha^{(2)}(m_s)$ +/- 3 x 10⁻⁵: OZI +/- 1.5 x 10⁻⁴ : $sin^2 \theta_W(M_Z)$

$$A_{PV} = \frac{N_{\uparrow\uparrow} - N_{\uparrow\downarrow}}{N_{\uparrow\uparrow} + N_{\uparrow\downarrow}} = \frac{G_F Q^2}{4\sqrt{2\pi\alpha}} \left[Q_W + F(Q^2, E) \right] \qquad \stackrel{\text{Erler, Kurylov}}{\underset{R-M}{\overset{\& R-M}{\overset{\& R-M}}}$$

$$E-Independent \qquad e^- \qquad W \qquad p^- \qquad e^- \qquad Z \qquad p^- \qquad$$

 e^{-}

e

Z

w

р

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E-dependent: E = 1.165 GeV

Ref. [11]	Ref. [15]	Ref. [17]	This work **
$(3\pm 3)10^{-3}$	$\bigl(4.7^{+1.1}_{-0.4}\bigr)10^{-3}$	$(5.7\pm0.9)10^{-3}$	$(5.4\pm2.0)10^{-3}$

- [11] Gorchtein & Horowitz
- [15] Sibirtsev et al
- [17] Rislow & Carlson
- ** Gorchtein, Horowitz, R-M 1102.3910 [nucl-th]





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Lower energy measurement



 $E = 180 MeV, Q^2 = 0$

[1.32 +/- 0.05 (mod avg) +/- 0.27 (bkg) ^{+0.11}_{-0.08} (res)] x 10 ⁻³

 e^{-}

 e^{-}

w

p

p

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Dominant E-dependence

$$\operatorname{Re}\Box_{\gamma Z_{A}}(\nu) = \frac{2\nu}{\pi} \int_{\nu_{\pi}}^{\infty} \frac{d\nu'}{\nu'^{2} - \nu^{2}} \operatorname{Im}\Box_{\gamma Z_{A}}(\nu')$$

$$\operatorname{Re}\Box_{\gamma Z_{V}}(\nu) = \frac{2}{\pi} \int_{\nu_{\pi}}^{\infty} \frac{\nu' d\nu'}{\nu'^{2} - \nu^{2}} \operatorname{Im}\Box_{\gamma Z_{V}}(\nu')$$

$$e^{-\frac{\nu'}{\mu}}$$

e⁻

p

$$\mathrm{Im}\Box_{\gamma Z_A}(\nu) = \alpha_{\mathrm{em}} g_A^e \int_{W_{\pi}^2}^s \frac{dW^2}{(s-M^2)^2} \int_0^{Q_{max}^2} \frac{dQ^2}{1+\frac{Q^2}{M_Z^2}} \left[F_1^{\gamma Z} + \frac{s(Q_{max}^2-Q^2)}{Q^2(W^2-M^2+Q^2)} F_2^{\gamma Z} \right]$$

Two Issues:

[1] Existence of sufficient SF data in relevant kinematic region

[2] Isospin rotating $F^{\gamma\gamma} \rightarrow F^{\gamma Z}$

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Additional measurements



Dominant contributions; scarce data

e

 e^{-}

р

p

Measure A_{PV} in extrapolation region: direct probe of $F^{\gamma Z}$

Z

w

EW Radiative Corrections to Moller

A. Czarnecki & W.J. Marciano PRD(1996)

- $A_{RL}(ee) = \alpha (1-4\sin^2\theta_W)$ $\sin^2\theta_W(m_Z)_{MS} = 0.23124(6)$ or running + 3.01(25)_{hadronic}% $\sin^2\theta_W(Q=0) = 0.23820(60)$
 - + WWbox (+3.6%) γ Zbox...(-5.5%) partial cancellation + other small 1 loop corrections \rightarrow -40(3)% reduction!

E158 $\Delta A_{RL}/A_{RL} = \pm 12.5\%$ vs Running unc. $\pm 6\%$?

Erler & Ramsey-Musolf \rightarrow factor of 8.6 error reduction! +3.01(25)% \rightarrow +2.99(3)% <u>Theory ±0.6% vs Moller exp ±2.4%</u> $\Delta sin^2 \theta_W^{RC} \sim \pm 0.00007!$ Pristine Potentially another factor of 2 reduction via lattice <u>W. Marciano</u>

Beam Normal Asymmetry

- Increasingly important for many precision measurements.
- Can isolate some radiative corrections with only polarized electrons (no need for positrons).
- PREX, CREX provide unique data sets on high Z targets. Comparing these to low Z data allows "Rosenbluth like" separations of different coulomb distortion, dispersion ... contributions vs Z.
 Instead of long / transverse vs angle, have coulomb distortion / dispersion contributions vs Z.
- Analyzing high Z and low Z data together can provide important additional insight even if only interested in low Z experiments.



Beam Normal Asymmetry



- Coulomb distortions are coherent, order Zα. Important for PREX (Pb has Z=82).
- Dispersion corrections order α (not Zα). Important for QWEAK because correction is order α/Q_w ~ 10% relative to small Born term (Q_w). --- M. Gorshteyn
- Both Coulomb distortion and dispersion cor. can be important for Transverse Beam Asymmetry An for ²⁰⁸Pb. Note Born term gives zero by time reversal symmetry.

Beam Normal Asymmetry

- Left / Right cross section asymmetry for electrons with transverse polarization.
- Potential systematic error for PV from small trans components of beam polarization.
- A_n vanishes in Born approx (time reversal) --> Sensitive probe of 2 or more photon effects. Can measure radiative corrections directly!
- Full dispersion calculations include all excited states but only for 2 photon exchange.

A_n for a Range of Nuclei



Coulomb Distortions for PREX

 We sum elastic intermediate states to all orders in Zα by solving Dirac equ. for e moving in coulomb V and weak axial A potentials.

 $A \propto G_F \rho_W(r) \approx 10 \text{ eV}$ $V(r) \approx 25 \text{MeV}$

 Right handed e sees V+A, left handed V-A

 $A_{pv} = [d\sigma/d\Omega|_{V+A} - d\sigma/d\Omega|_{V-A}]/2d\sigma/d\Omega$

 Coulomb distortions reduce A_{pv} by ~30%, but they are accurately calculated. Q² shared between "hard" weak, and soft interactions so weak amplitude G_FQ² reduced.



III. CC Weak Interactions

Weak Decays: New Interactions

Decay Correlations: Scalar & Tensor Currents

SUSY Corrections to CKM Unitarity



Neutron & Nuclear β *-decay:* $0^+ \rightarrow 0^+$ *, Nab,* ⁶*He...*

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$0^+ \rightarrow 0^+$ Dispersion Corrections: δ_{NS}



Towner & Hardy, PRC 91 (2015) 2, 025501

$0^+ \rightarrow 0^+$ Dispersion Corrections: δ_{NS}



Towner & Hardy, PRC 91 (2015) 2, 025501





J. Engel





J. Engel





Dispersion Corrections: pp Reaction



Project: pionless EFT computation

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IV. Time Reversal

Diamagnetic Systems: P- & T-Odd Moments



nuclear finite size: Schiff moment



Schiff moment, MQM,...

EDMs of diamagnetic atoms (¹⁹⁹Hg)

Diamagnetic Systems

Nuclear Moments



Diamagnetic Systems

Nuclear Moments



Diamagnetic Systems

Nuclear Moments



Diamagnetic Systems: Schiff Moments



Atomic effect from nuclear finite size: Schiff moment

EDMs of diamagnetic atoms (¹⁹⁹Hg)



Nuclear Schiff Moment

Nuclear Enhancements



Schiff moment, MQM,...



Nuclear polarization: mixing of opposite parity states by $H^{TVPV} \sim 1 / \Delta E$

EDMs of diamagnetic atoms (¹⁹⁹Hg)

Nuclear Schiff Moment

Nuclear Enhancements: Octupole Deformation



Calculated ²²⁵Ra density

 $|\pm\rangle = \frac{1}{\sqrt{2}} \left(| \bullet \rangle \pm | \bullet \rangle \right)$

Opposite parity states mixed by H^{TVPV}



"Nuclear amplifier"

Nuclear polarization: mixing of opposite parity states by $H^{TVPV} \sim 1 / \Delta E$

EDMs of diamagnetic atoms (²²⁵Ra)

Thanks: J. Engel

Schiff Screening & Corrections



EDMs of diamagnetic atoms (¹⁹⁹Hg)

PT PT PT PT T $C_{J} E \times O EDM, Schiff...$ $T^{M}_{J} O \times E E MQM...$ $T^{E}_{J} \otimes T^{E}_{J=1} \otimes T^{E}_{J=2} ?$

S. Inoue, MRM 53

Two-boson exchange in semileptonic processes: important for elastic PV eN & eA scattering (¹²C) & nuclear β -decay; beam normal asymmetry, Olympus... provide tests



V. Workshop Questions

- What is the path forward for improving our understanding of γγ exchange in semileptonic processes?
- How reliable are the present contributions of Zγ and Wγ boxes for nucleons and nuclei ?
- What additional theoretical developments/ computations are needed?
- Is there a program of experimental measurements that could be used to refine theoretical predictions ?

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