

# Electroweak-Scale Objects at a 100 TeV Collider

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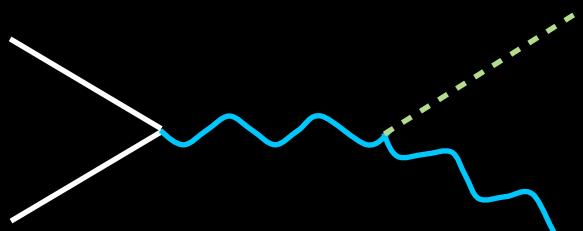
@ ACFI Workshop

19 September 2015

# How EW-Scale Objects are Made

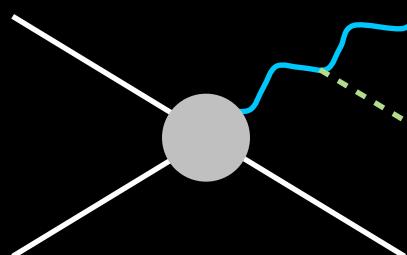
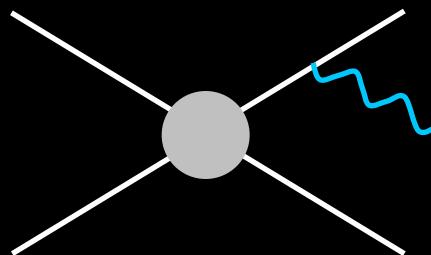
**At the hard process scale**

More beam energy  $\Rightarrow$  more parton lumi



**Hierarchically below the hard process scale...EW parton shower**

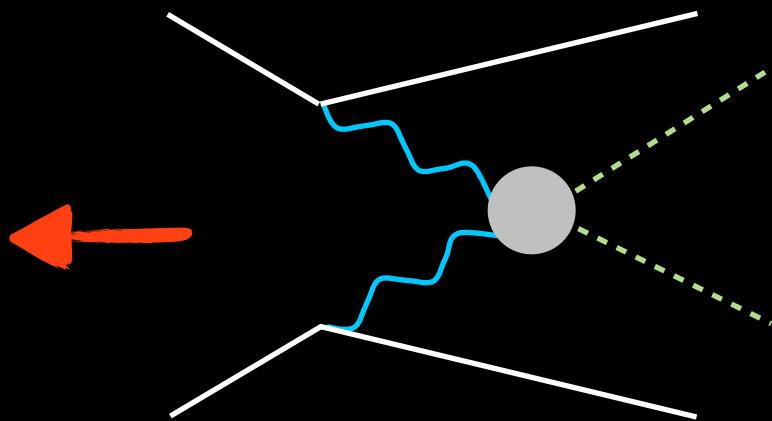
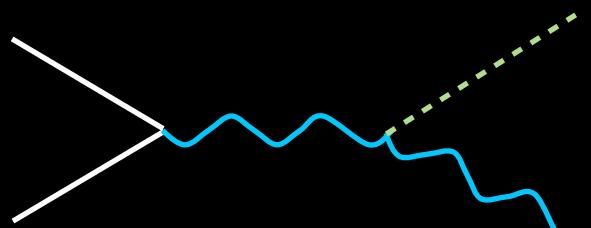
More beam energy  $\Rightarrow$  easier access to extreme event kinematics



# How EW-Scale Objects are Made

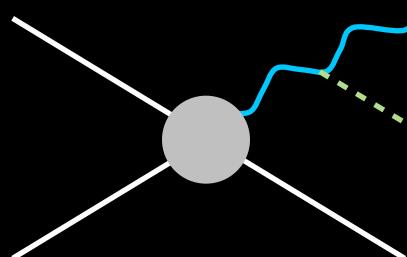
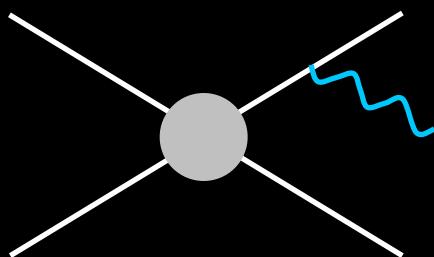
**At the hard process scale**

More beam energy  $\Rightarrow$  more parton lumi



**Hierarchically below the hard process scale...EW parton shower**

More beam energy  $\Rightarrow$  easier access to extreme event kinematics

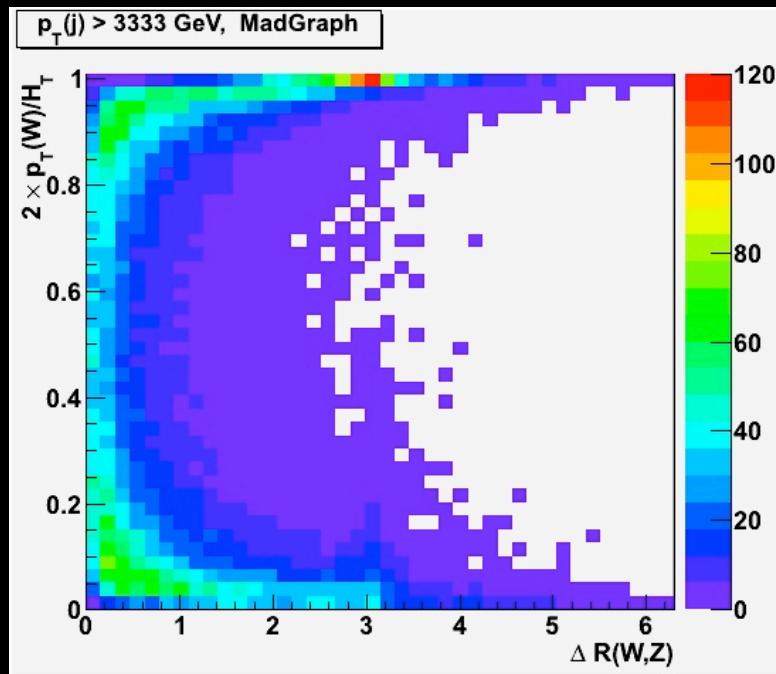


# Why Think About EW Parton Showering?

- No choice
  - impacts almost all physics at  $E > \text{TeV}$
- New regime to measure couplings of full EW/Higgs theory
  - different systematics
  - different (smaller?) backgrounds
- New leverage against new physics
  - opportunities for new “light” particle states associated with EWPT?

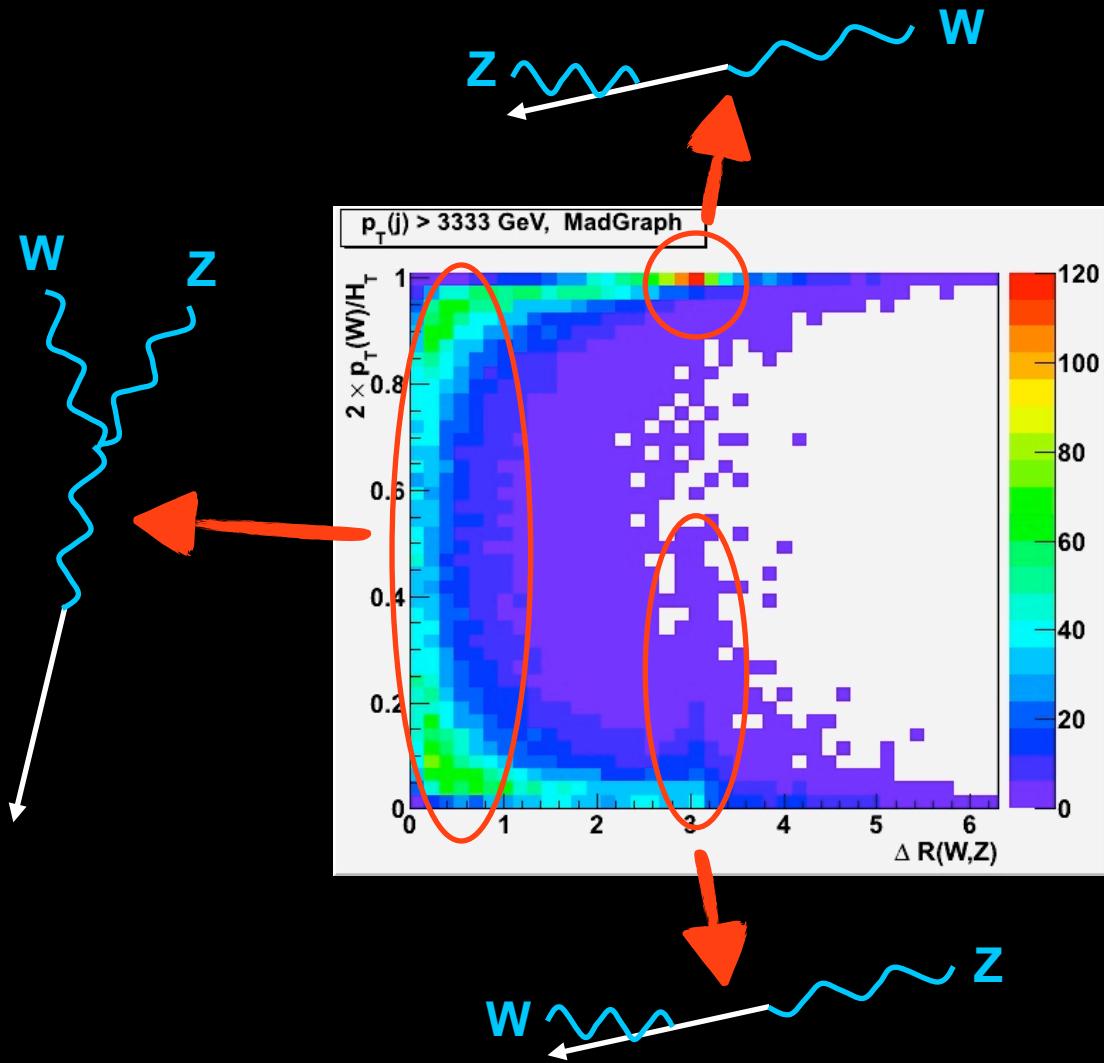
# Example: WZ+Jet @ 100 TeV

$p_T(j) > 3300 \text{ GeV}$



\* using lumi = 1 ab<sup>-1</sup>

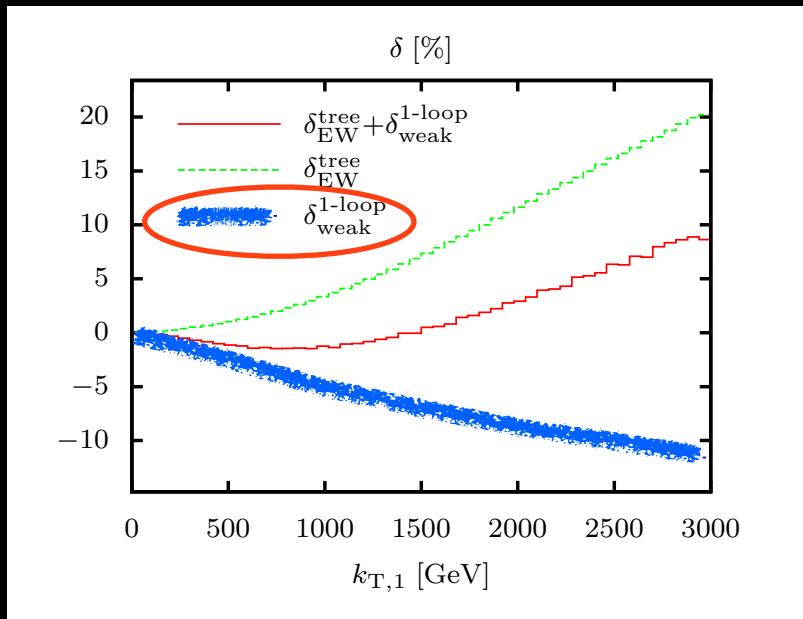
# Example: WZ+Jet @ 100 TeV



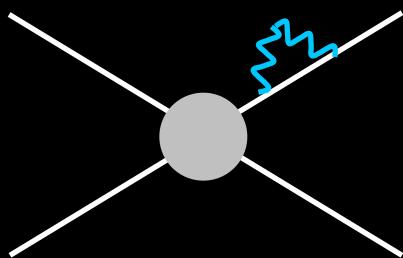
also Moretti, Nolten, Ross (hep-ph/0606201),  
 Denner & Pozzorini (hep-ph/0010202,0104127),  
 many Manohar papers, many other related works

# Electroweak Sudakovs

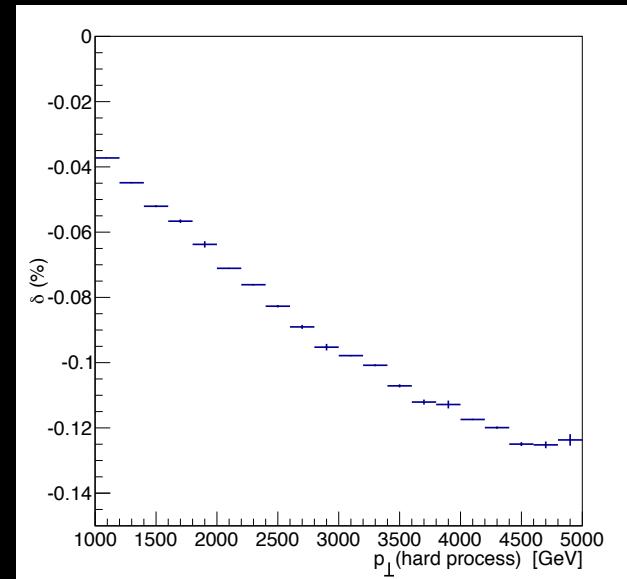
Dittmaier, Huss, Speckner (1210.0438)



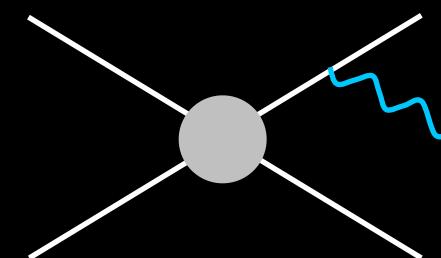
**Virtual weak corrections to  
exclusive dijets at LHC14**



Christiansen & Sjöstrand (1401.5238)



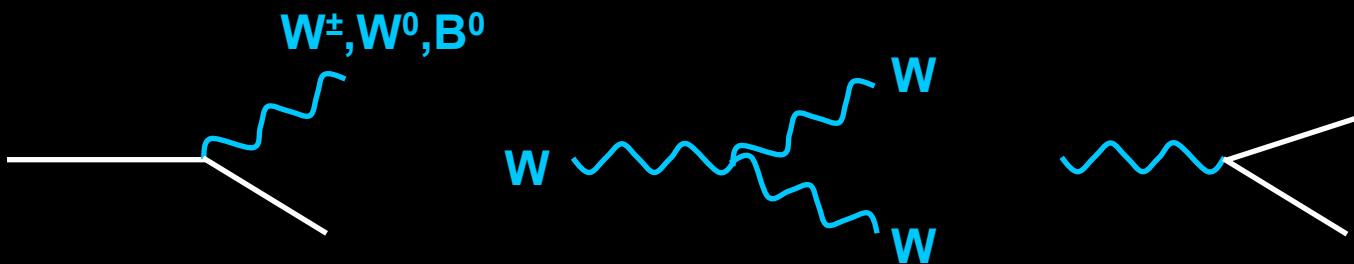
**LO rate minus real W/Z  
emission events**



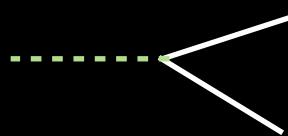
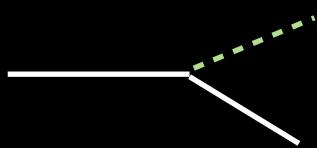
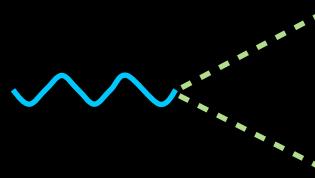
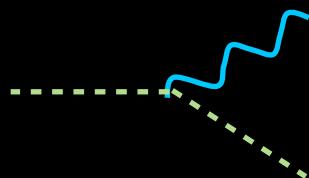
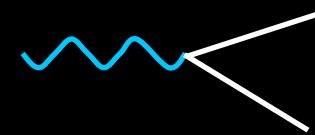
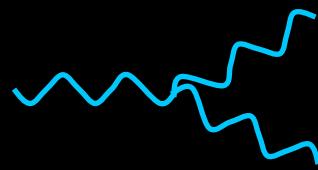
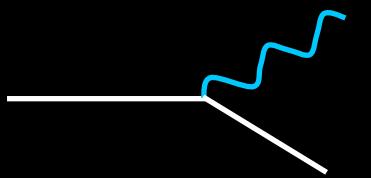
# Novelties wrt QCD/QED Parton Showering

- Perturbative cutoff via SSB
  - physically-measurable soft/collinear emissions
- Longitudinals/scalars
- Chirality
- Yukawa showers
- Neutral boson interference
  - correct basis is  $W^0/B^0$ , not  $\gamma/Z$
- Weak isospin self-averaging
  - $u(x) > d(x) \rightarrow u_R(x) > Q_L(x) > d_R(x)$

# Electroweak Splittings



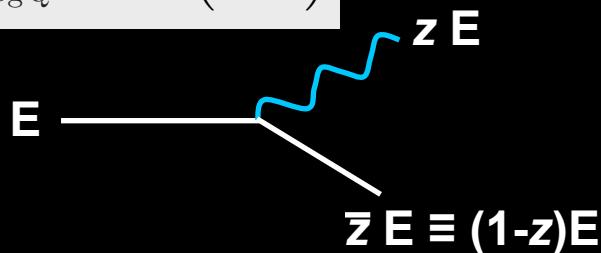
# Electroweak Splittings



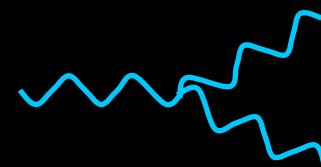
+ 1 $\rightarrow$ 3 splittings

# Electroweak Splittings

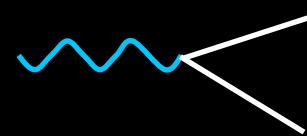
$$\frac{d\mathcal{P}}{dz d \log Q^2} \propto \frac{1}{8\pi^2} \left( \frac{1+\bar{z}^2}{z} \right)$$



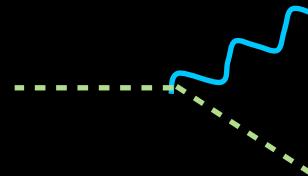
$$\frac{1}{8\pi^2} \frac{(1-z\bar{z})^2}{z\bar{z}}$$



$$\frac{1}{8\pi^2} \left( \frac{z^2 + \bar{z}^2}{2} \right)$$

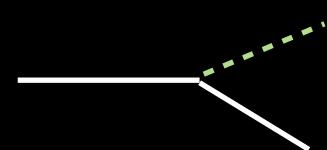


$$\frac{1}{8\pi^2} \left( \frac{2\bar{z}}{z} \right)$$

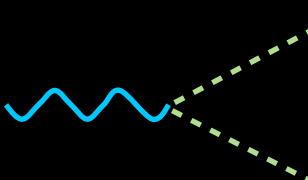


$$\frac{1}{8\pi^2} (z\bar{z})$$

$$\frac{1}{8\pi^2} \left( \frac{z}{2} \right)$$



$$\frac{1}{8\pi^2} \left( \frac{1}{2} \right)$$



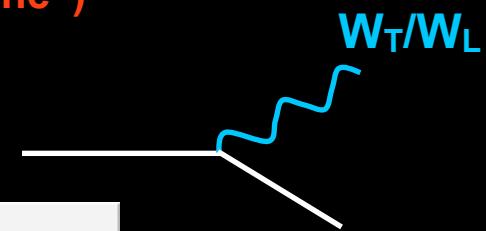
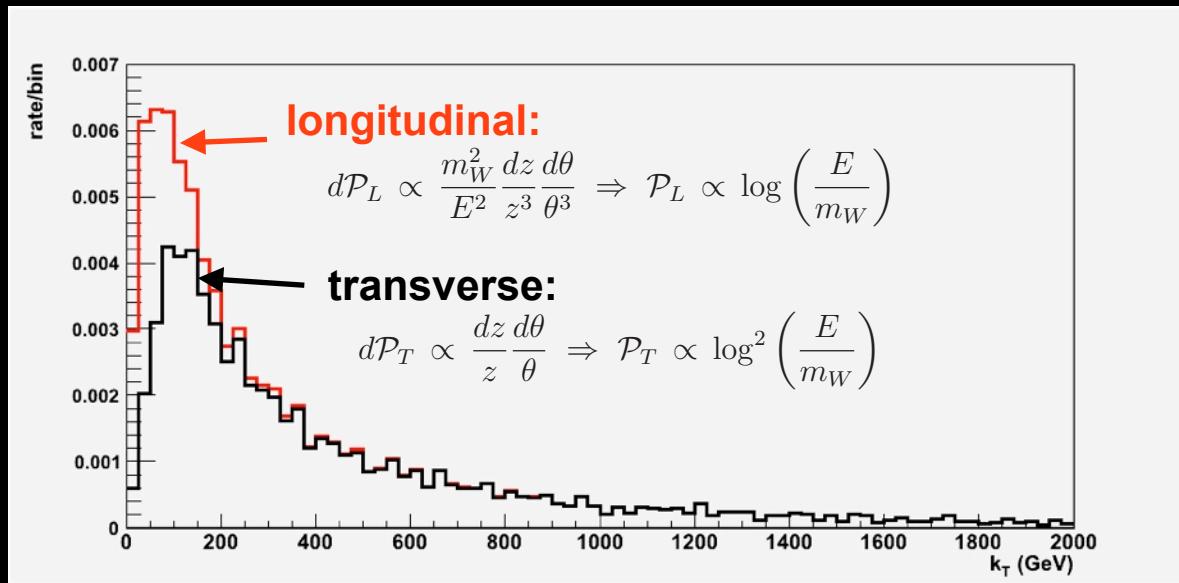
+ 1→3 splittings

# Massive Splitting Functions

$$\frac{d\mathcal{P}(a \rightarrow bc)}{dz dk_T^2} \simeq \frac{1}{16\pi^2} \frac{z_b z_c}{(k_T^2 + z_c m_b^2 + z_b m_c^2 - z_b z_c m_a^2)^2} |\mathcal{M}(a \rightarrow bc)|^2$$

shower shuts off at  $k_T \sim m$  ("dead cone")

**W-boson FSR within 10 TeV quark-jet**



\* E.g., ISR  $\Rightarrow$  polarized W/Z PDFs: Kane, Repko, Rolnik (1984), Dawson (1985)

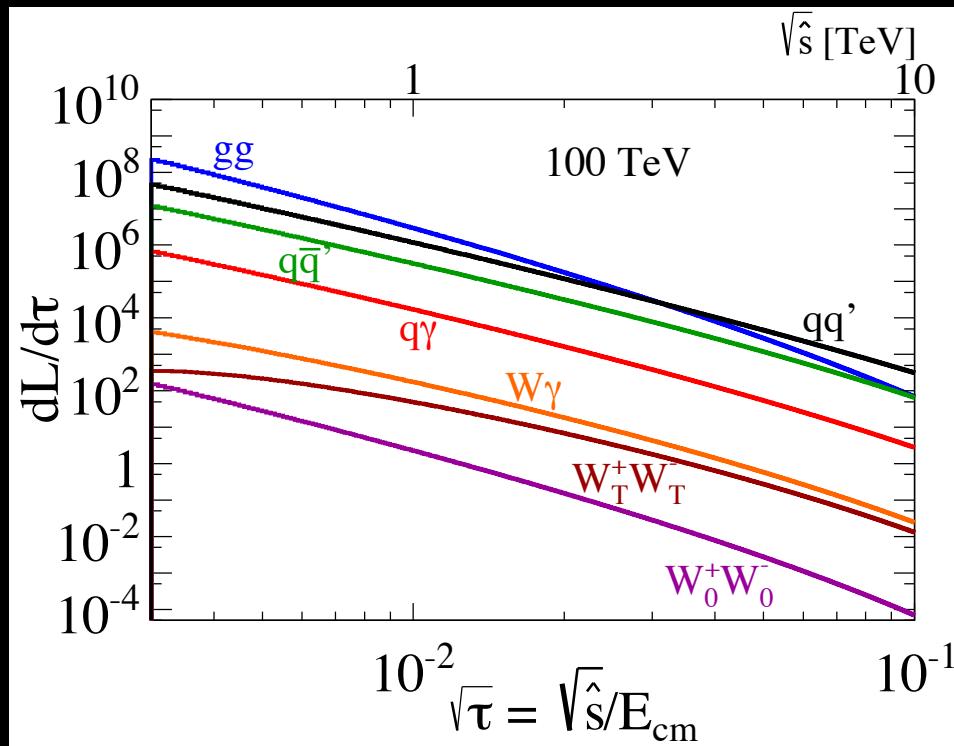
# Light Quark Total Splitting Rates

Averaged over flavors & helicities,  
summed over W & Z

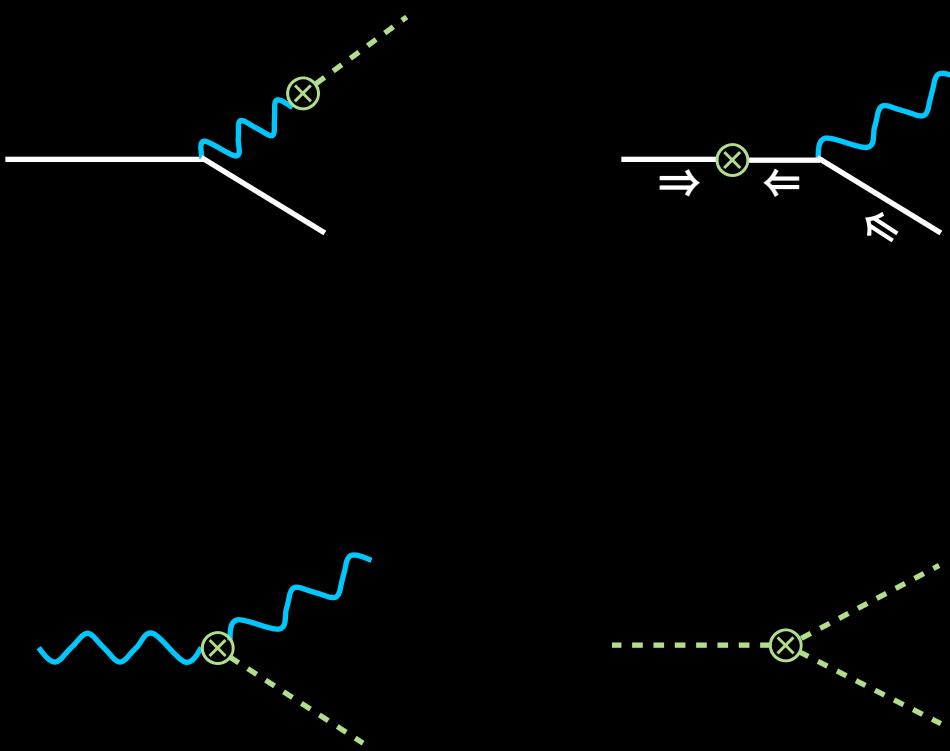
$$\mathcal{P}(q \rightarrow V_T q) \simeq (3 \times 10^{-3}) \left[ \log \frac{E}{m_{EW}} \right]^2 \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 1.7\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 7\%$$

$$\mathcal{P}(q \rightarrow V_L q) \simeq (2 \times 10^{-3}) \log \frac{E}{m_{EW}} \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 0.5\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 1\%$$

# Parton Lumis at 100 TeV Collider

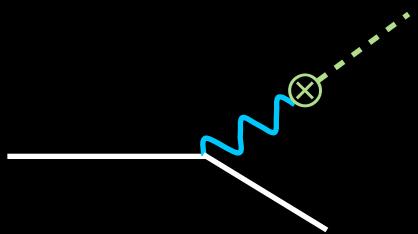


# "Broken" Showering at $O(v)$

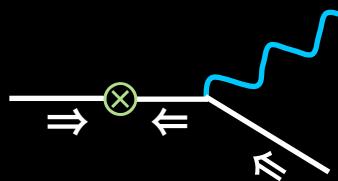


# “Broken” Showering at $O(v)$

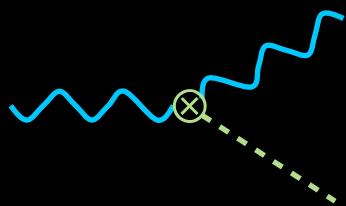
$\Rightarrow \log(E/m)$



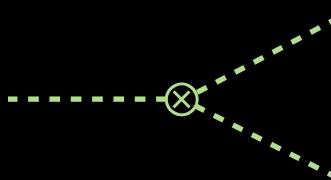
$\Rightarrow \text{constant}^*$



$\Rightarrow \text{constant}^*$



$\Rightarrow \text{constant}^*$   
 $(\sim 0.001)$



\* All beamed into a cone of size  $\sim m/E$

# Gauging to Manifest Goldstone Equivalence

(rotating) lightcone gauge condition

$$n(k) \cdot A(k) = 0$$

$$n^0(k) \equiv 1, \quad \vec{n}(k) \equiv -\frac{k^0}{|k^0|} \frac{\vec{k}}{|\vec{k}|}$$

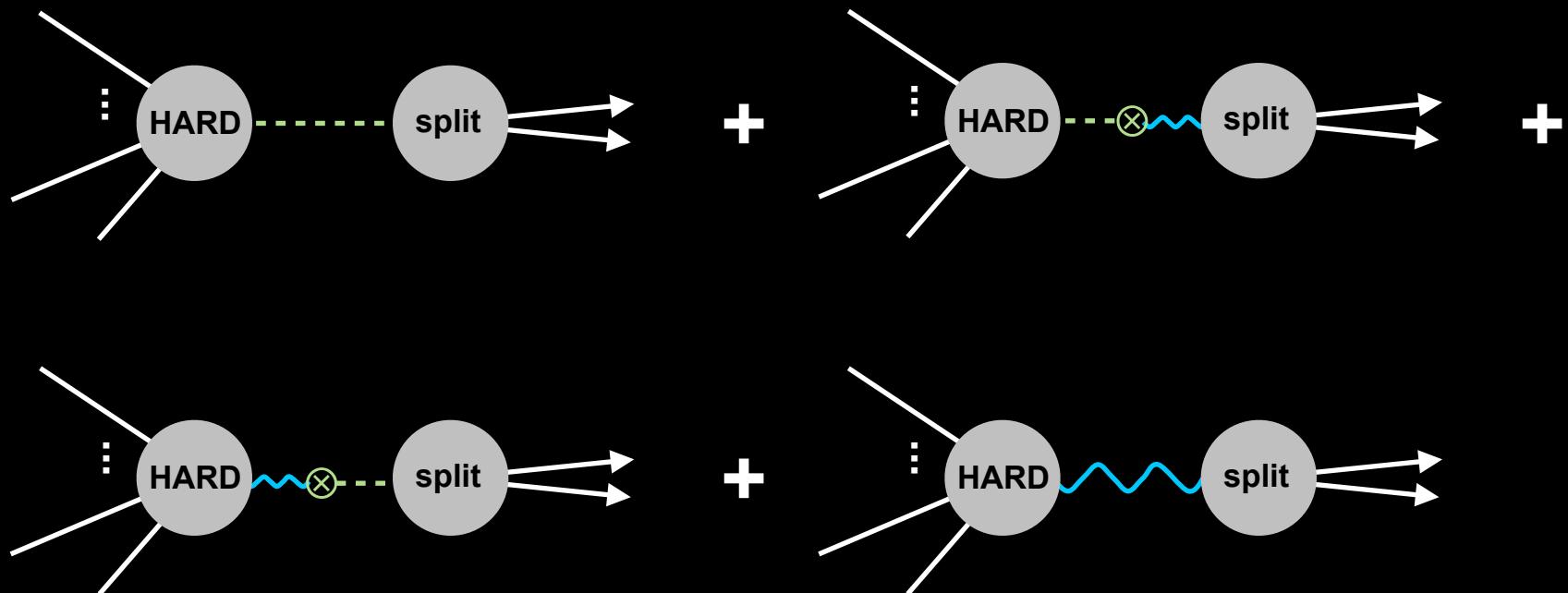
$$\text{long. polarization } \epsilon_\phi^\mu(k) \equiv \frac{\sqrt{|k^2|}}{n(k) \cdot k} n^\mu(k)$$

$$\begin{aligned}\langle A_T(k)A_T(-k) \rangle &= \frac{i}{k^2 - m^2} \\ \langle A_\phi(k)A_\phi(-k) \rangle &= \frac{i}{k^2 - m^2} \text{sign}(k^2) \\ \langle \phi(k)\phi(-k) \rangle &= \frac{i}{k^2 - m^2} \\ \langle A_\phi(k)\phi(-k) \rangle &= \frac{i}{k^2 - m^2} \frac{-im}{\sqrt{|k^2|}}.\end{aligned}$$

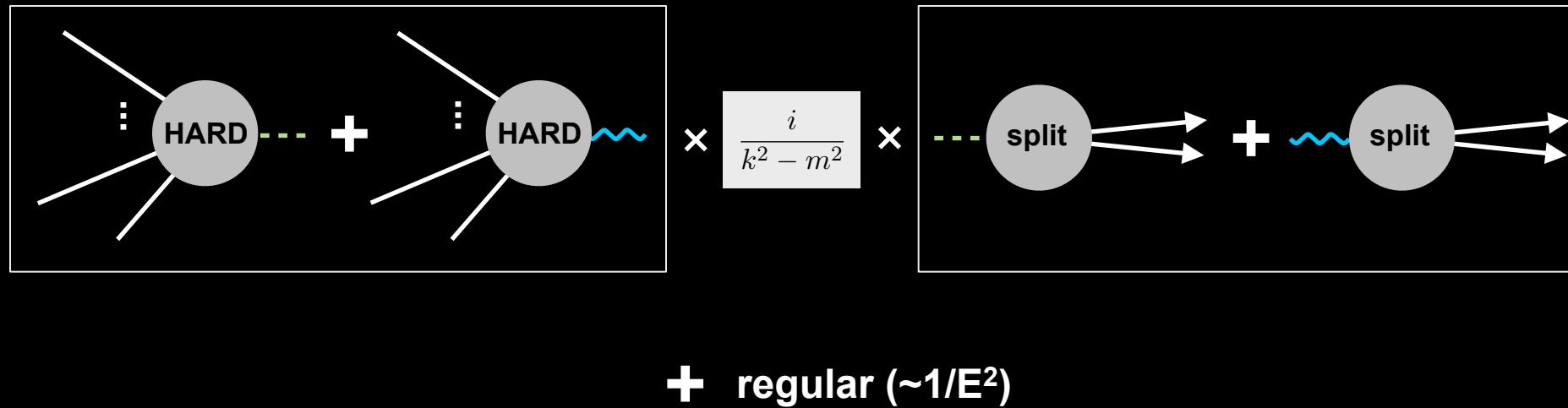
- Delete (sometimes) problematic  $k^\mu/m$  part of longitudinal polarization
  - replaced by on- & off-shell in Feynman rules by Goldstone
  - amplitude to create on-shell longitudinal from  $A^\mu \sim m/E$
- Keep mixed field basis
- Unlike  $R_\xi$ , Goldstone field interpolates physical longitudinal bosons (amplitude  $\sim i$ )

\* see also Wulzer (1309.6055), Srivastava & Brodsky (hep-ph/0202141), earlier papers

# Factorization for Longitudinals



# Factorization for Longitudinals



# Transverse Vector Total Splitting Rates

$$\mathcal{P}(V_T \rightarrow V_T V_T) \simeq (0.01) \left[ \log \frac{E}{m_{\text{EW}}} \right]^2 \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 6\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 22\%$$

$$\mathcal{P}(V_T \rightarrow V_T V_L) \simeq (0.01) \log \frac{E}{m_{\text{EW}}} \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 2\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 5\%$$

$$\mathcal{P}(V_T \rightarrow V_L V_L) \simeq (4 \times 10^{-4}) \log \frac{E}{m_{\text{EW}}} \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 0.1\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 0.2\%$$

$$\mathcal{P}(V_T \rightarrow f\bar{f}) \simeq (0.02) \log \frac{E}{m_{\text{EW}}} \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 5\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 10\%$$

$$\mathcal{P}(V_T \rightarrow V_L h) \simeq (4 \times 10^{-4}) \log \frac{E}{m_{\text{EW}}} \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 0.1\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 0.2\%$$

$$\mathcal{P}(V_T \rightarrow V_T h) \simeq (3 \times 10^{-4}) \Rightarrow \mathcal{P}(1 \text{ TeV}) \simeq 0.03\%, \quad \mathcal{P}(10 \text{ TeV}) \simeq 0.03\%$$

# Longitudinal Vector Total Splitting Rates

$$\mathcal{P}(V_L \rightarrow V_T V_L) \sim (2 \times 10^{-3}) \left[ \log \frac{E}{m_{EW}} \right]^2 \Rightarrow \mathcal{P}(1 \text{ TeV}) \sim 1\%, \quad \mathcal{P}(10 \text{ TeV}) \sim 4\%$$

$$\mathcal{P}(V_L \rightarrow V_T h) \sim (2 \times 10^{-3}) \left[ \log \frac{E}{m_{EW}} \right]^2 \Rightarrow \mathcal{P}(1 \text{ TeV}) \sim 1\%, \quad \mathcal{P}(10 \text{ TeV}) \sim 4\%$$

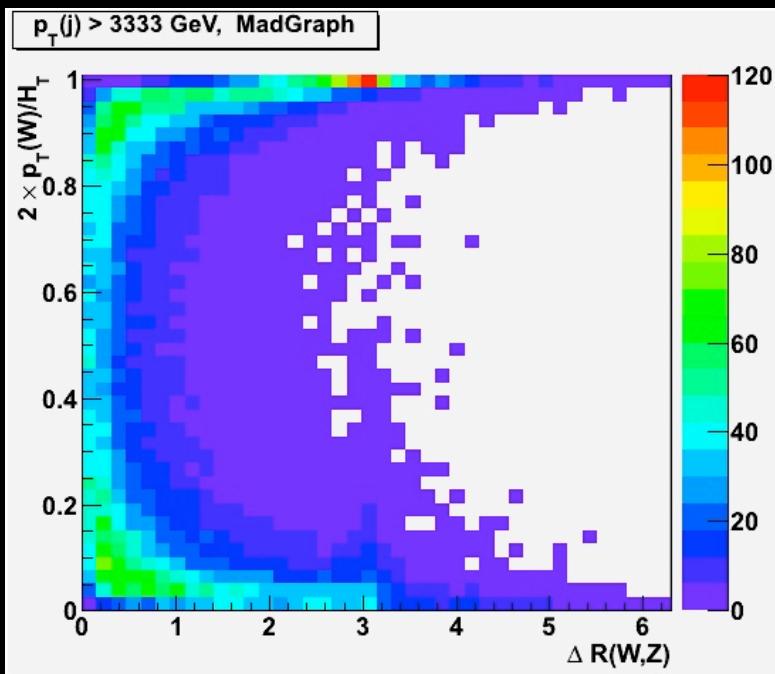
**Plus many others.....**

# Our Shower Program

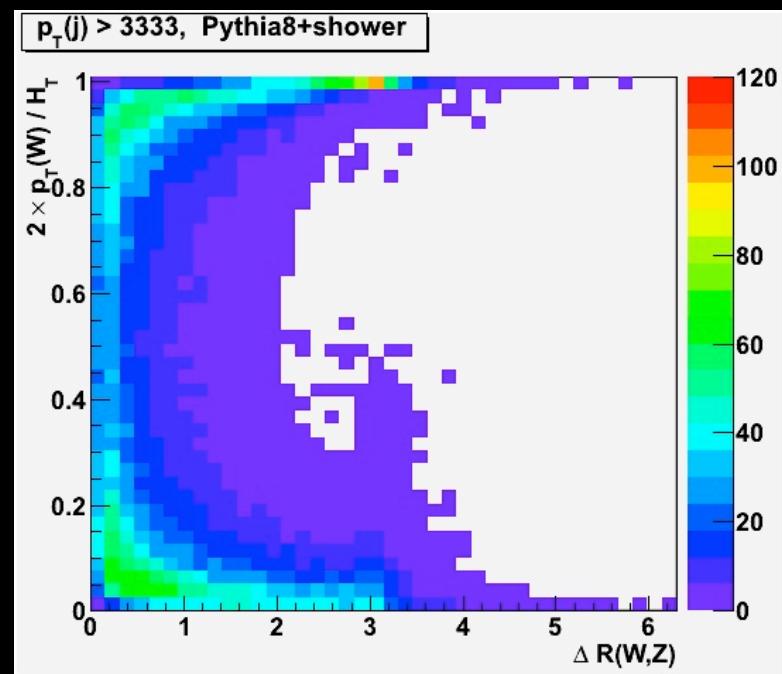
- Currently PYTHIA6-like virtuality-ordered
  - collinear approximation, no coherence between dipoles
- Polarized splittings
- Massive splitting functions
  - amplitudes and phase space
- Reweighting of secondary splittings
- Interleaved with QCD
- Only FSR (so far)
- Built in C++...ideally adapt to run within PYTHIA 8 framework

# WZ+Jet Revisited

MadGraph



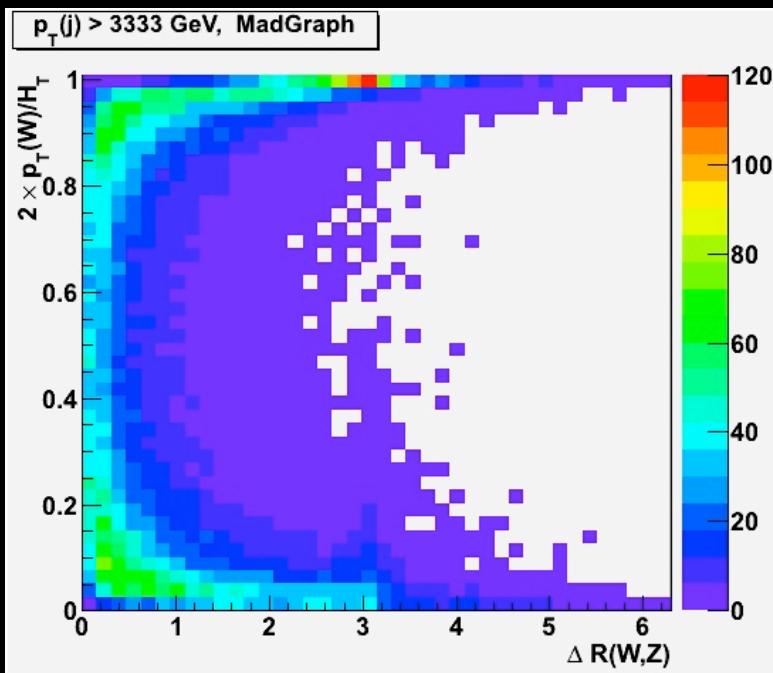
Pythia8 W/Z+jet + EW-Shower



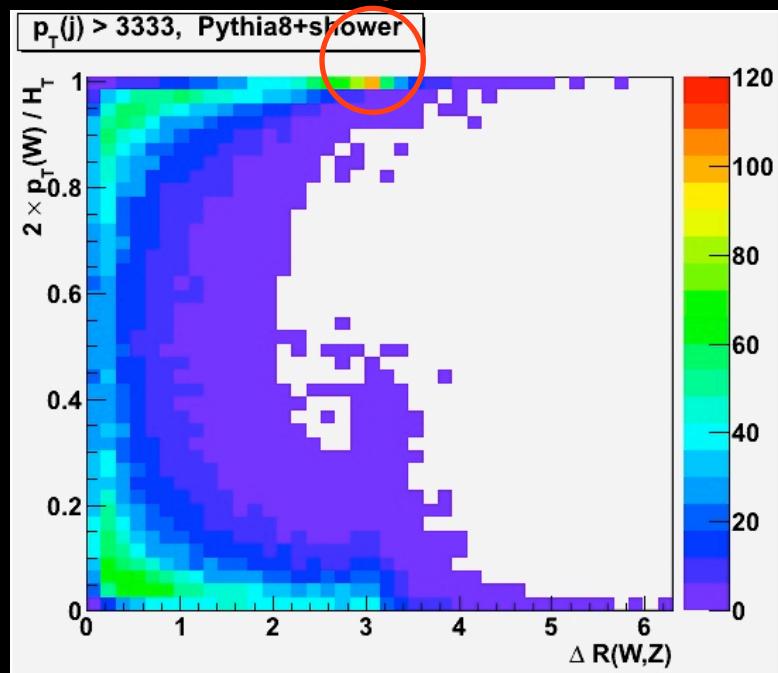
# WZ+Jet Revisited

~10% loss from further showering

MadGraph

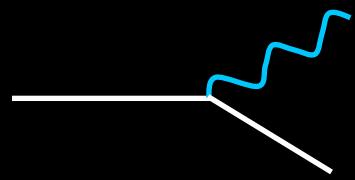
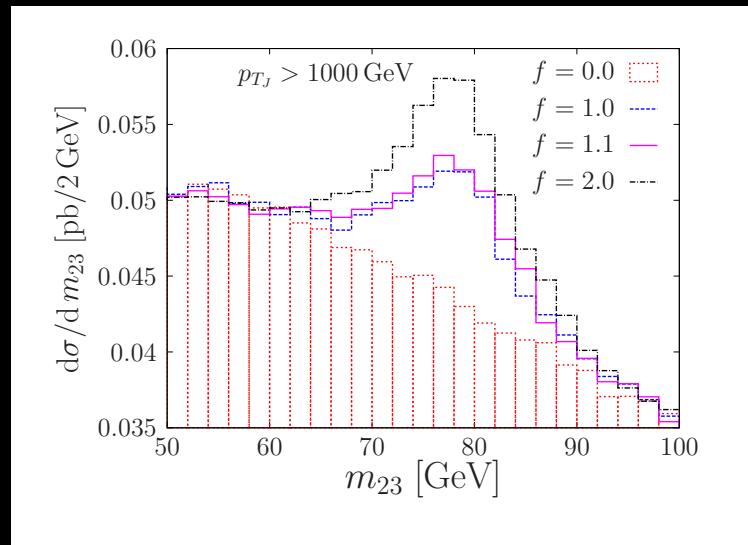


Pythia8 W/Z+jet + EW-Shower



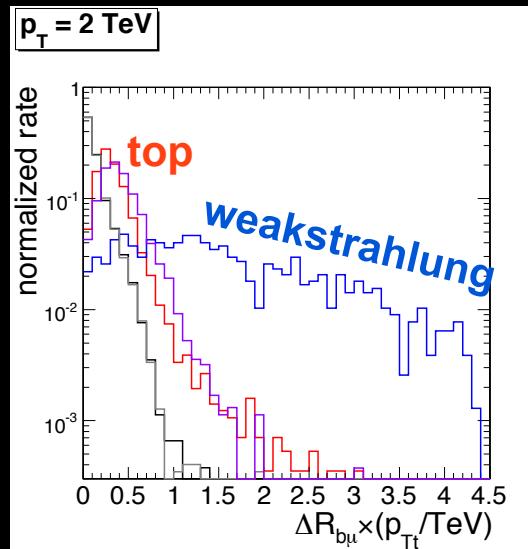
# Measurement of Weakstrahlung Rate (LHC)

Krauss, Petrov, Schönherr, Spannowsky (1403.4788)



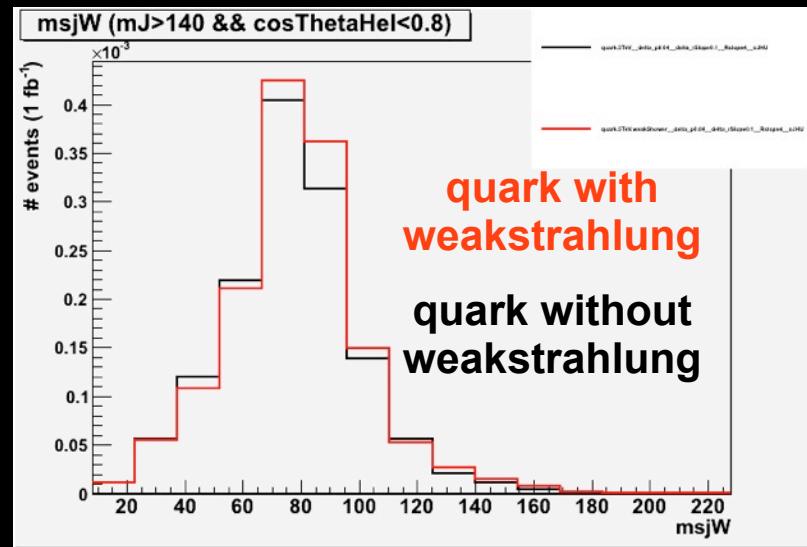
# Effect on Top-Tagging (Any $p_T > \text{TeV}$ )

Leptonic top-jets:  
main background ( $\sim 10^{-3}$  quark-mistag)



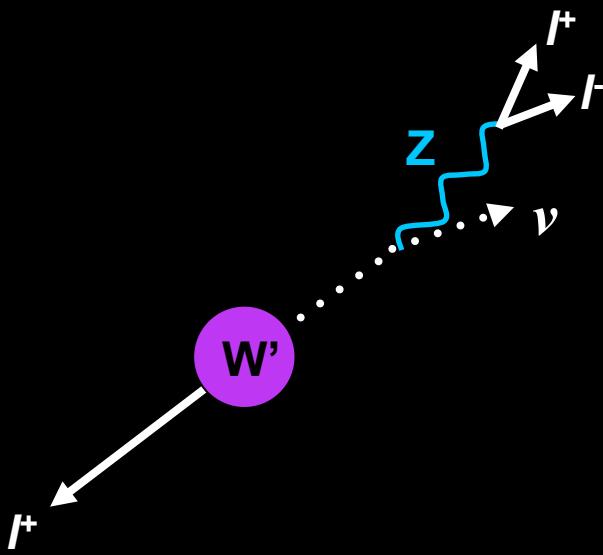
Rehermann & Tweedie (1007.2221)

Hadronic top-jets:  
5-10% perturbation to quark mistag

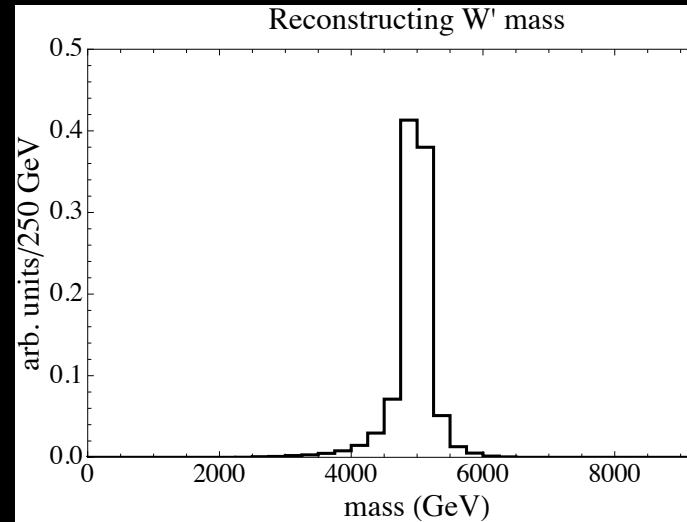


with Z Han & M Son

# As a Handle on Heavy New Physics



Hook & Katz (1407.2607)  
also Rizzo (1403.5465)



Radiated Z-boson traces neutrino's  
3-vector direction  
(and probes  $W'$  chirality)

# Some Other Back-of-the Envelope Applications

- $W_T W_T$  production at  $O(10 \text{ TeV})$ 
  - $W_T W_T \rightarrow W_T W_T$  scattering: potentially  $O(1)$  showering probability
  - KK graviton: corrections up to  $O(50\%)$
- $W_L W_L$  production at  $O(10 \text{ TeV})$ 
  - $W_L W_L \rightarrow W_L W_L / hh, Z' \rightarrow Z_L h, W' \rightarrow W_L h / W_L Z_L$ :  $O(10\%)$  showering probability

# "New" Higgs Production Modes

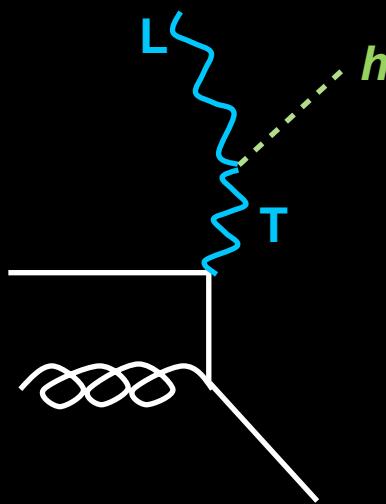
Are they good for something? Reduced systematics? Complementary information?

Process	$\sigma_{\text{NLO}}(8 \text{ TeV}) [\text{fb}]$	$\sigma_{\text{NLO}}(100 \text{ TeV}) [\text{fb}]$	$\rho$
$pp \rightarrow H (m_t, m_b)$	$1.44 \cdot 10^4 {}^{+20\%}_{-16\%} {}^{+1\%}_{-2\%}$	$5.46 \cdot 10^5 {}^{+28\%}_{-27\%} {}^{+2\%}_{-2\%}$	38
$pp \rightarrow Hjj$ (VBF)	$1.61 \cdot 10^3 {}^{+1\%}_{-0\%} {}^{+2\%}_{-2\%}$	$7.40 \cdot 10^4 {}^{+3\%}_{-2\%} {}^{+2\%}_{-1\%}$	46
$pp \rightarrow Ht\bar{t}$	$1.21 \cdot 10^2 {}^{+5\%}_{-9\%} {}^{+3\%}_{-3\%}$	$3.25 \cdot 10^4 {}^{+7\%}_{-8\%} {}^{+1\%}_{-1\%}$	269
$pp \rightarrow Hb\bar{b}$ (4FS)	$2.37 \cdot 10^2 {}^{+9\%}_{-9\%} {}^{+2\%}_{-2\%}$	$1.21 \cdot 10^4 {}^{+2\%}_{-10\%} {}^{+2\%}_{-2\%}$	51
$pp \rightarrow Htj$	$2.07 \cdot 10^1 {}^{+2\%}_{-1\%} {}^{+2\%}_{-2\%}$	$5.21 \cdot 10^3 {}^{+3\%}_{-5\%} {}^{+1\%}_{-1\%}$	252
$pp \rightarrow HW^\pm$	$7.31 \cdot 10^2 {}^{+2\%}_{-1\%} {}^{+2\%}_{-2\%}$	$1.54 \cdot 10^4 {}^{+5\%}_{-8\%} {}^{+2\%}_{-2\%}$	21
$pp \rightarrow HZ$	$3.87 \cdot 10^2 {}^{+2\%}_{-1\%} {}^{+2\%}_{-2\%}$	$8.82 \cdot 10^3 {}^{+4\%}_{-8\%} {}^{+2\%}_{-2\%}$	23
$pp \rightarrow HW^+W^-$ (4FS)	$4.62 \cdot 10^0 {}^{+3\%}_{-2\%} {}^{+2\%}_{-2\%}$	$1.68 \cdot 10^2 {}^{+5\%}_{-6\%} {}^{+2\%}_{-1\%}$	36
$pp \rightarrow HZW^\pm$	$2.17 \cdot 10^0 {}^{+4\%}_{-4\%} {}^{+2\%}_{-2\%}$	$9.94 \cdot 10^1 {}^{+6\%}_{-7\%} {}^{+2\%}_{-1\%}$	46
$pp \rightarrow HW^\pm\gamma$	$2.36 \cdot 10^0 {}^{+3\%}_{-3\%} {}^{+2\%}_{-2\%}$	$7.75 \cdot 10^1 {}^{+7\%}_{-8\%} {}^{+2\%}_{-1\%}$	33
$pp \rightarrow HZ\gamma$	$1.54 \cdot 10^0 {}^{+3\%}_{-2\%} {}^{+2\%}_{-2\%}$	$4.29 \cdot 10^1 {}^{+5\%}_{-7\%} {}^{+2\%}_{-2\%}$	28
$pp \rightarrow HZZ$	$1.10 \cdot 10^0 {}^{+2\%}_{-2\%} {}^{+2\%}_{-2\%}$	$4.20 \cdot 10^1 {}^{+4\%}_{-6\%} {}^{+2\%}_{-1\%}$	38
$pp \rightarrow HW^\pm j$	$3.18 \cdot 10^2 {}^{+4\%}_{-4\%} {}^{+2\%}_{-1\%}$	$1.07 \cdot 10^4 {}^{+2\%}_{-7\%} {}^{+2\%}_{-1\%}$	34
$pp \rightarrow HW^\pm jj$	$6.06 \cdot 10^1 {}^{+6\%}_{-8\%} {}^{+1\%}_{-1\%}$	$4.90 \cdot 10^3 {}^{+2\%}_{-6\%} {}^{+1\%}_{-1\%}$	81
$pp \rightarrow HZj$	$1.71 \cdot 10^2 {}^{+4\%}_{-4\%} {}^{+1\%}_{-1\%}$	$6.31 \cdot 10^3 {}^{+2\%}_{-7\%} {}^{+2\%}_{-1\%}$	37
$pp \rightarrow HZjj$	$3.50 \cdot 10^1 {}^{+7\%}_{-10\%} {}^{+1\%}_{-1\%}$	$2.81 \cdot 10^3 {}^{+2\%}_{-5\%} {}^{+1\%}_{-1\%}$	80

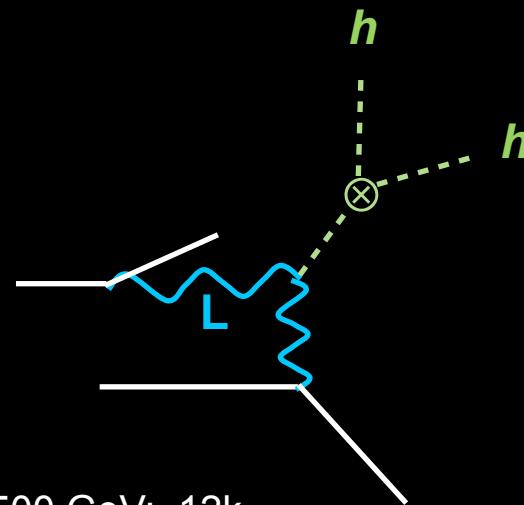
\*slide from  
Mangano  
(HXSWG  
meeting, July)

Table 1: Production of a single Higgs boson at the LHC and at a 100 TeV FCC-hh. The rightmost column reports the ratio  $\rho$  of the FCC-hh to the LHC cross sections. Theoretical uncertainties are due to scale and PDF variations, respectively. Monte-Carlo-integration error is always smaller than theoretical uncertainties, and is not shown. For  $pp \rightarrow HVjj$ , on top of the transverse-momentum cut of section 2, I require  $m(j_1, j_2) > 100 \text{ GeV}$ ,  $j_1$  and  $j_2$  being the hardest and next-to-hardest jets, respectively. Processes  $pp \rightarrow Htj$  and  $pp \rightarrow Hjj$  (VBF) do not feature jet cuts.

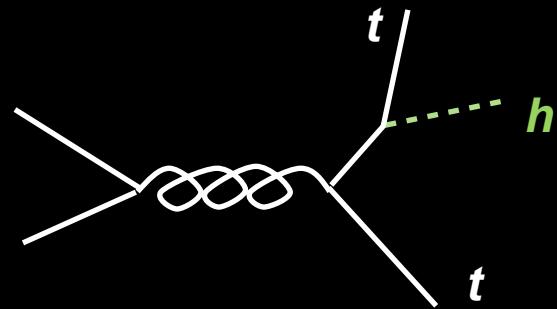
# Example Topologies



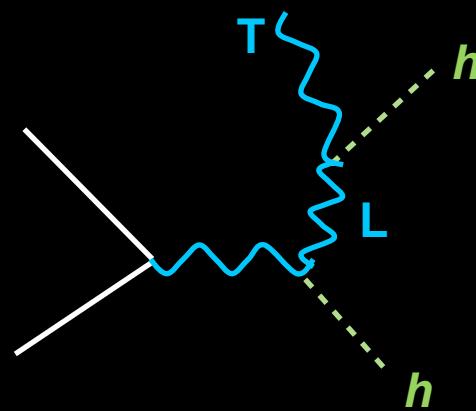
500 GeV: 2.5M  $(30 \text{ ab})^{-1}$   
1 TeV: 250k



500 GeV: 12k  
1 TeV: 1.4k



500 GeV: 75M  
1 TeV: 6M

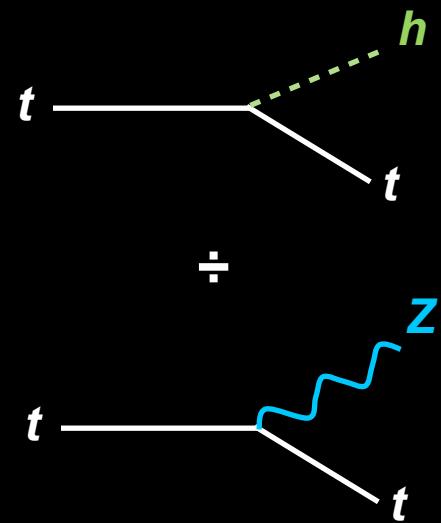
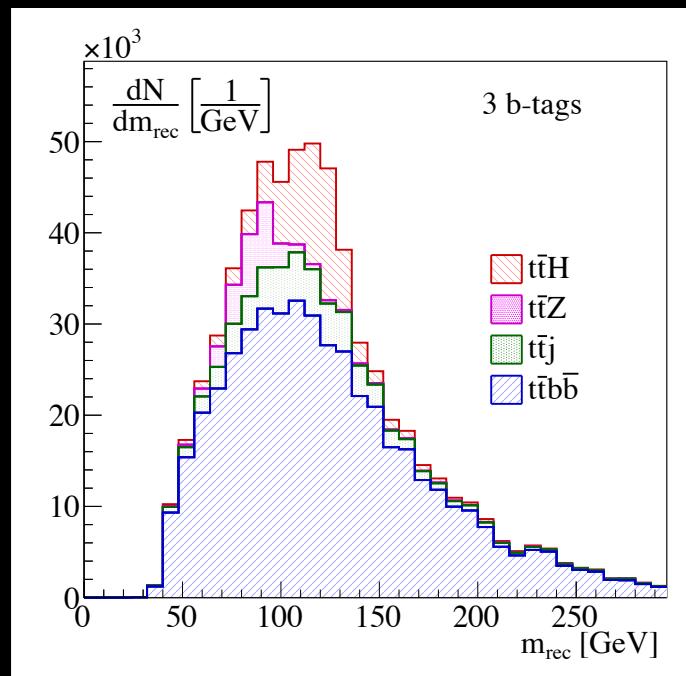


500 GeV: 14k  
1 TeV: 2.5k

Balance of “clean” high- $p_T$  topologies vs small high- $p_T$  rates not a priori obvious

# Semi-Boosted Measurement of Top Yukawa

Mangano, et al (1507.08169)



$\Delta y \sim \% \text{ with } 20 \text{ ab}^{-1}$

PDF uncertainties cancel

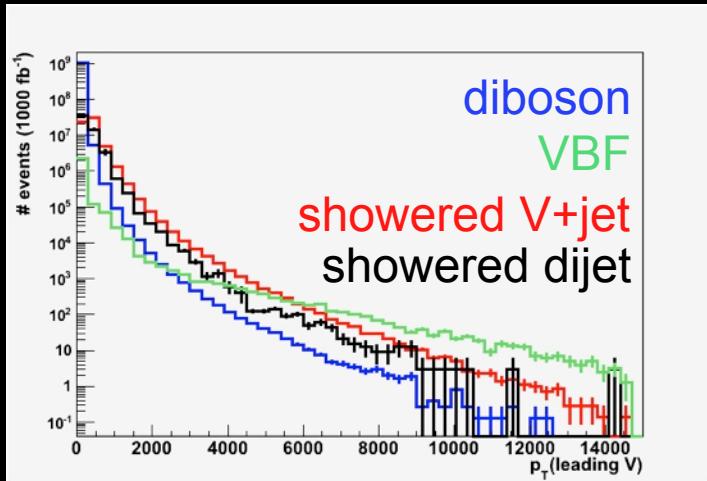
# Summary

- 100 TeV collider opens up new kinematic regimes for interactions of EW-scale particles
  - hopefully this at least served as a reminder
- EW splitting processes quickly grow/asymptote in rate
  - range from totally negligible to  $O(1)$ , depending on what you're looking at
- We're working on a multipurpose EW shower program
  - “quick and dirty” way to capture universal collinear physics
  - main addition is  $W \rightarrow WW$ , lots of other Higgs and Goldstone-equivalent processes
- Opportunities for precision/supplementary coupling measurements in/near these kinematic regions
- Sensitivity to new “light” states?

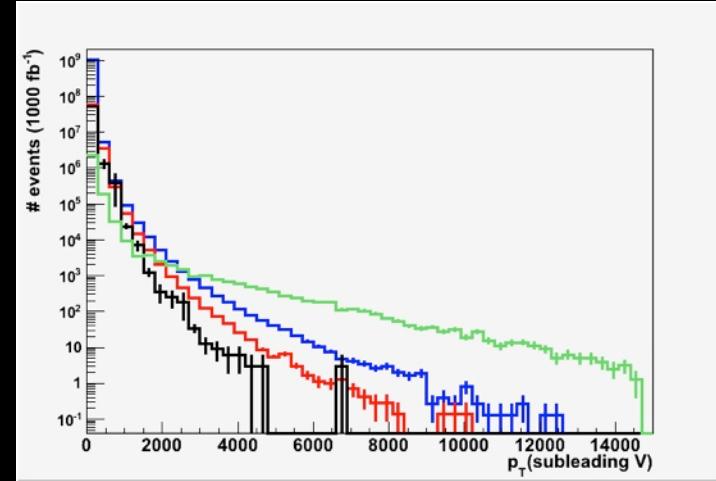
More...

# “Shower” Vs “Prompt” Diboson

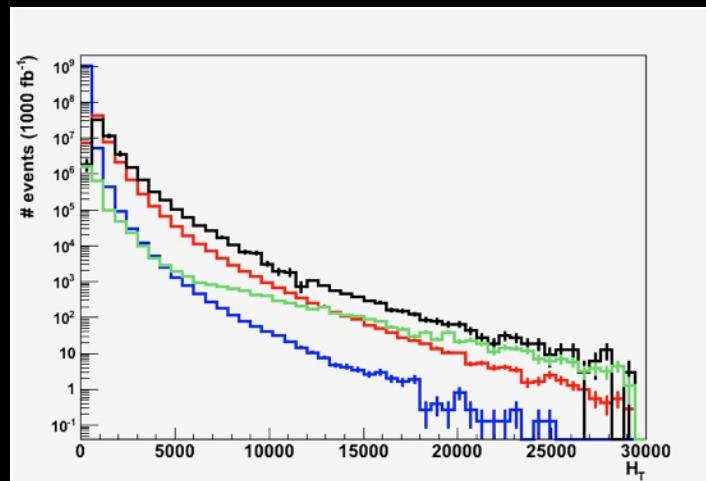
$p_T(\text{leading V})$



$p_T(\text{subleading V})$

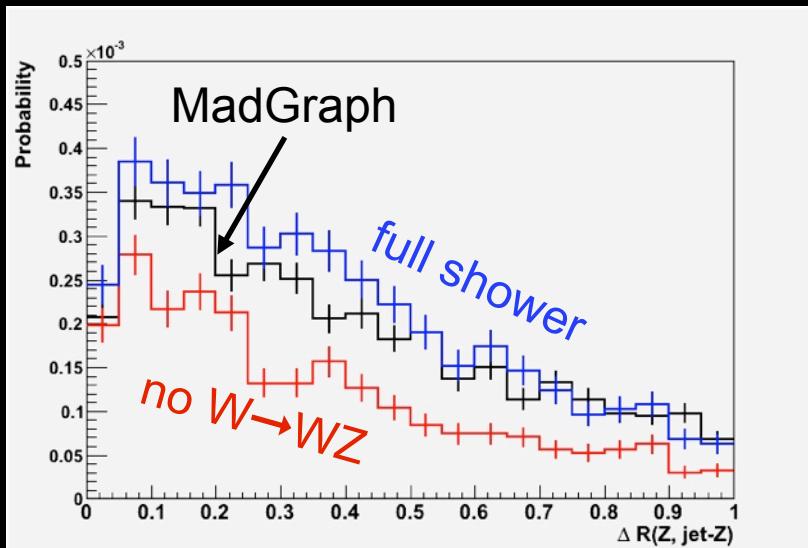


$H_T(\text{jets + V's})$

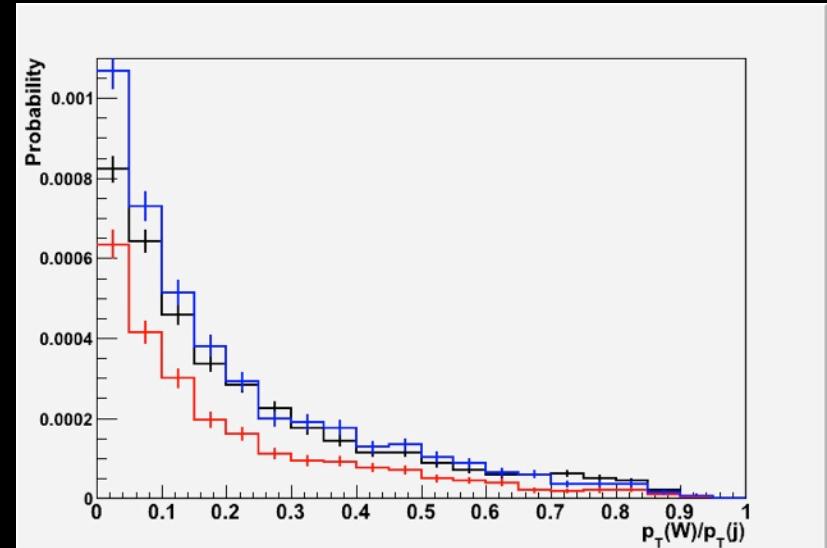


# Multiple Weak Emissions Inside One Jet

$u_L(10 \text{ TeV}) \rightarrow d_L W^+ Z$



$\Delta R(Z, \text{rest of jet})$



$p_T(W) / p_T(j)$

\*  $R=1.0$  anti- $kT$  jet,  $W/Z$  as partons

# Isospin Self-Averaged PDFs

