



Light Meson Physics with Crystal Ball at MAMI

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Outline

- Crystal Ball Set-up at MAMI
- η/η' Cross Sections
- Results from Crystal Ball at MAMI
 - Dalitz Plot Parameter for $\eta \rightarrow 3\pi^0$
 - Preliminary Result for $\eta \rightarrow \pi^0 \gamma \gamma$
 - Timelike Transition Form Factor from $\eta \rightarrow e^+ e^- \gamma$
 - C-violation in ω decays
- Future Plans
- Summary



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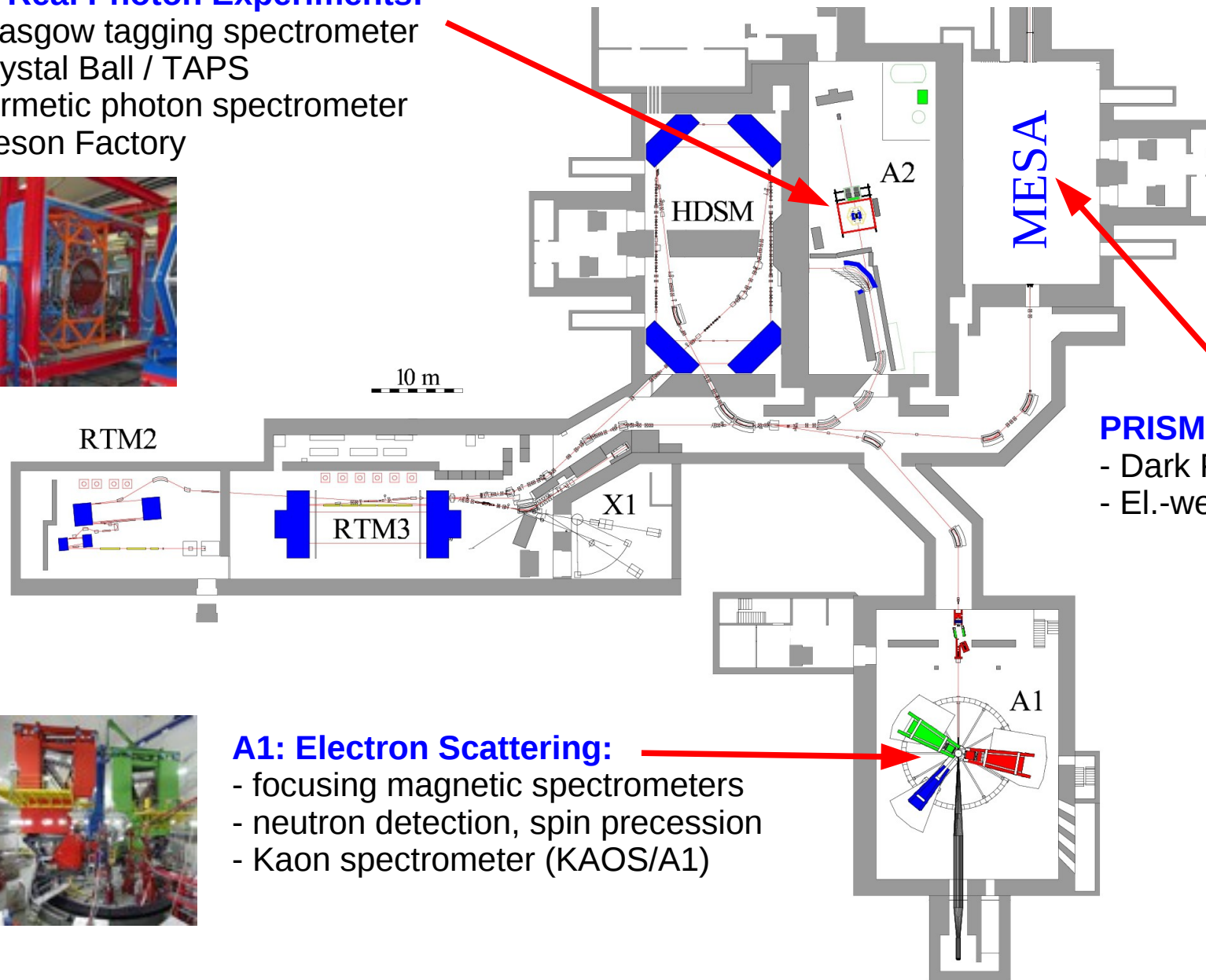
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Experiments at MAMI

A2: Real Photon Experiments:

- Glasgow tagging spectrometer
- Crystal Ball / TAPS hermetic photon spectrometer
- Meson Factory



- ## PRISMA/SFB 1044:
- Dark Photon Search
 - El.-weak Mixing Angle

A1: Electron Scattering:

- focusing magnetic spectrometers
- neutron detection, spin precession
- Kaon spectrometer (KAOS/A1)

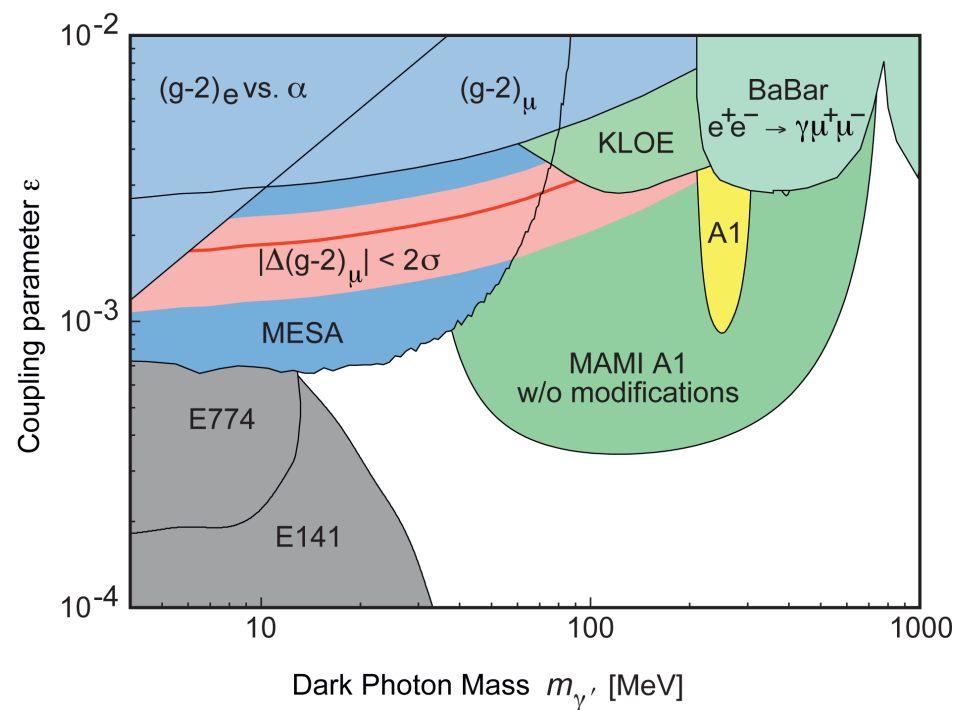
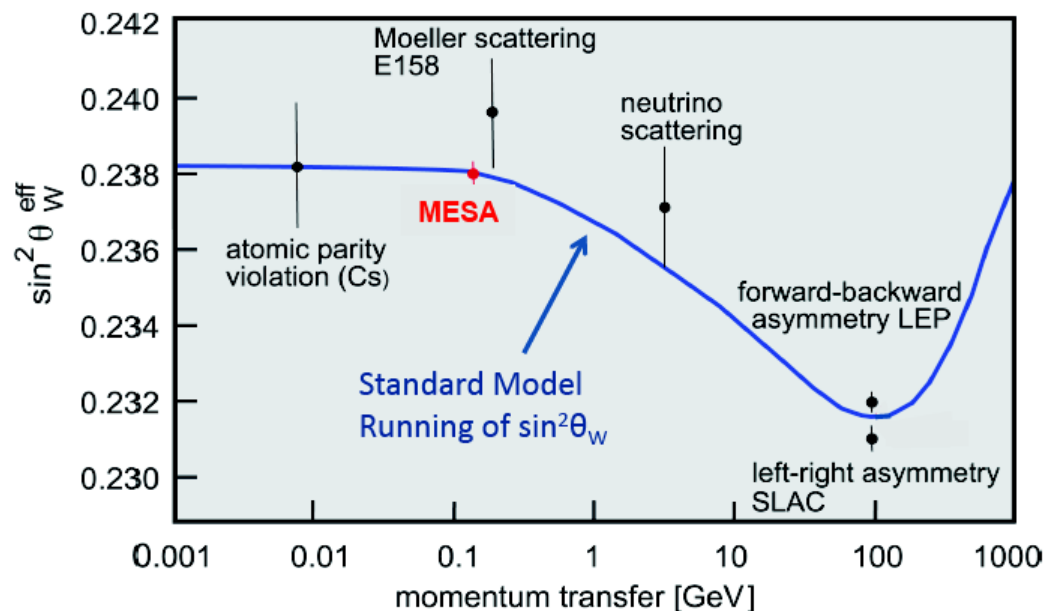


MESA

Mainz Energy-Recovering Superconducting Accelerator High-Intensity Electron Accelerator: 200 MeV @ 1 mA current

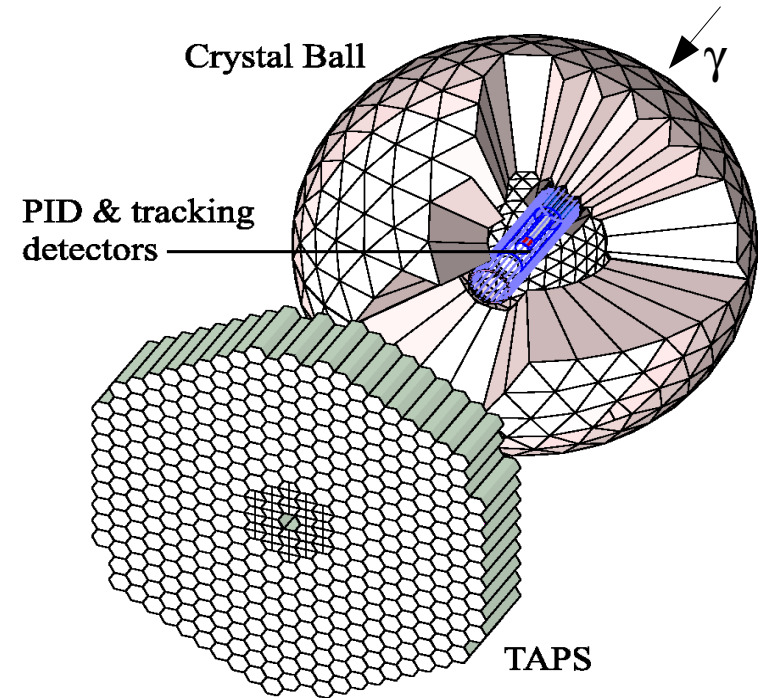
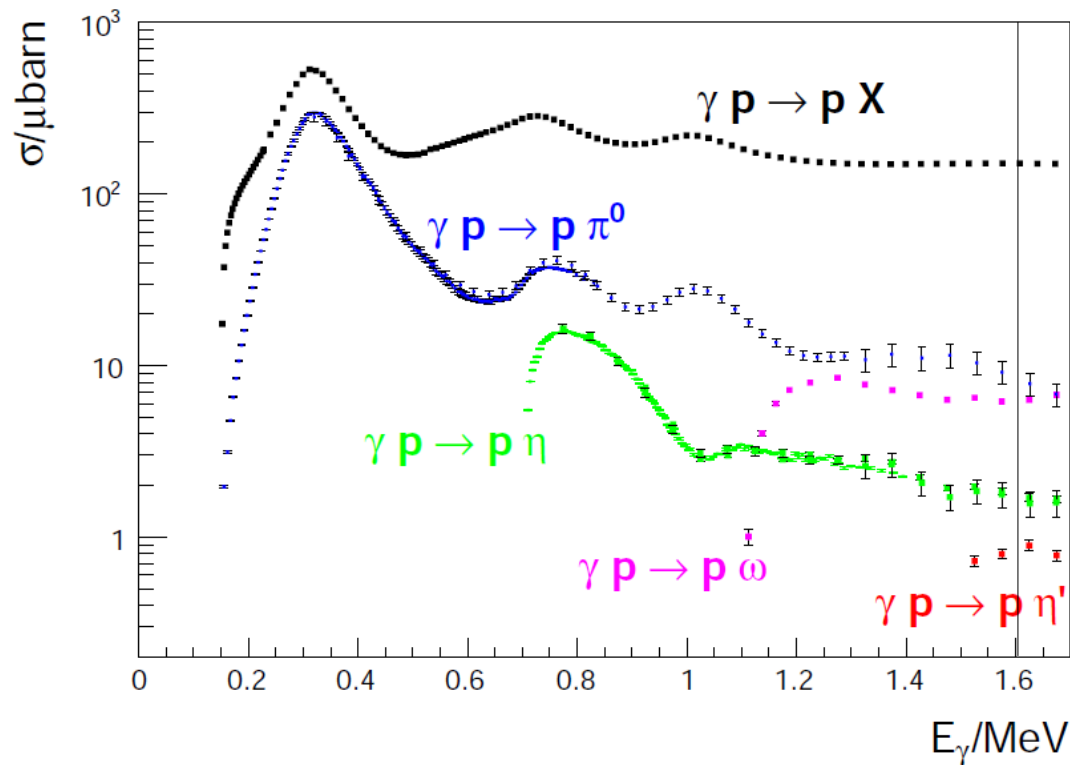
Frontier Experiments:

- Precision measurement of $\sin^2\theta_W$
- Search for Dark Photon
- Frontier Projects in Particle, Hadron, Nuclear Physics, ...



Meson Production with Real Photons

Data from CB@MAMI, CB@ELSA, CLAS, SAPHIR



Current production rates on IH_2 target feasible for taking data (Meson Factory):

$$\eta: 10^5 \text{ h}^{-1} \Rightarrow \text{Goal } 10^6 \text{ h}^{-1}$$

$$\eta': 2 \cdot 10^3 \text{ h}^{-1} \Rightarrow \text{Goal } 1.5 \cdot 10^4 \text{ h}^{-1}$$

Has to be imposed by detection and analysis efficiencies

$\Rightarrow 4\pi$ Crystal Ball/TAPS setup, e.m. Production mechanism very clean

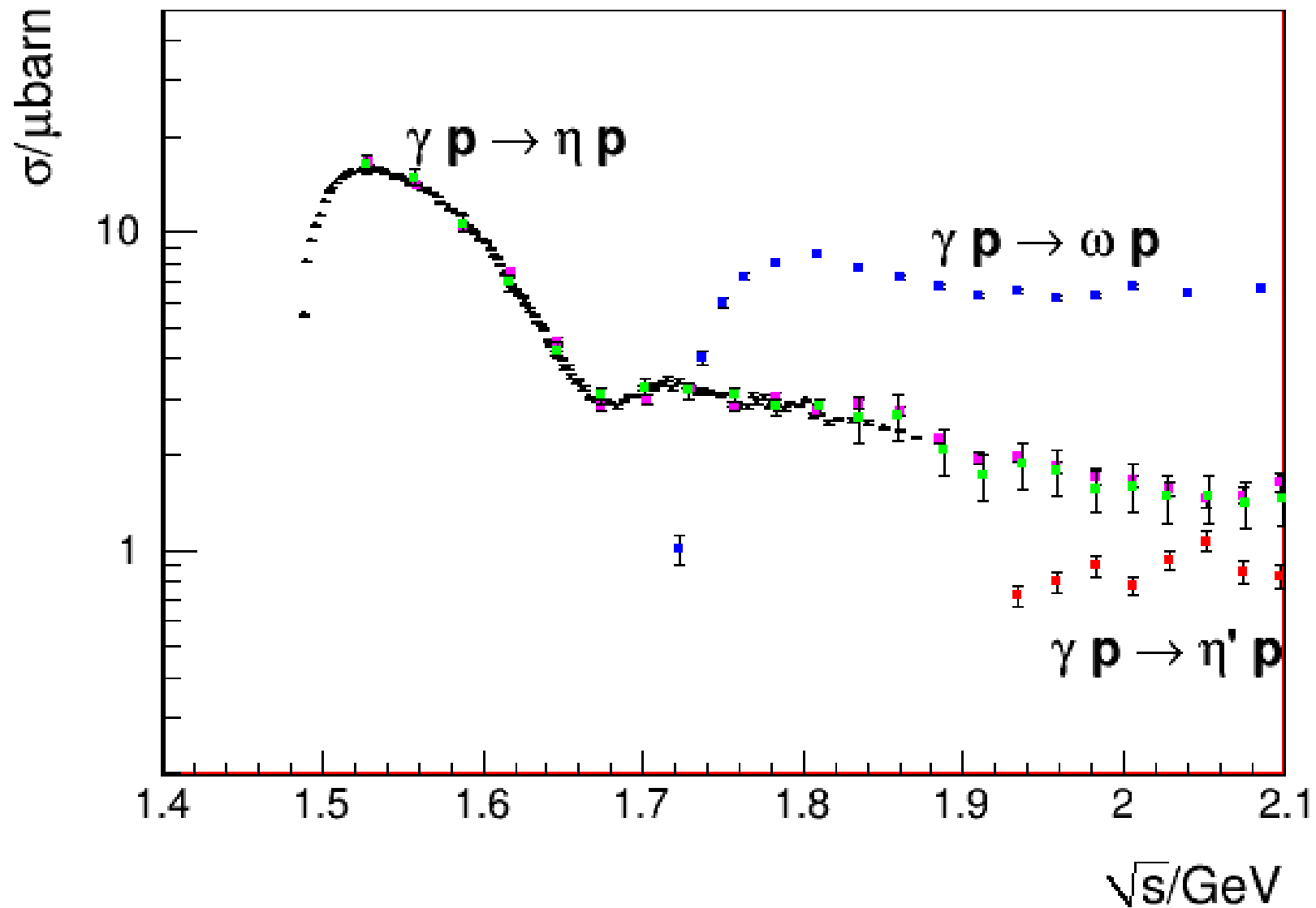
\Rightarrow Ideally suited to measure high rates of meson decays

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η Photoproduction Cross Section



Crystal Ball: E.F. McNicoll et al., Phys. Rev. C 82 (2010) 035208.

Crystal Barrel: V. Crede et al., Phys. Rev. Lett. 94 (2005) 012004.

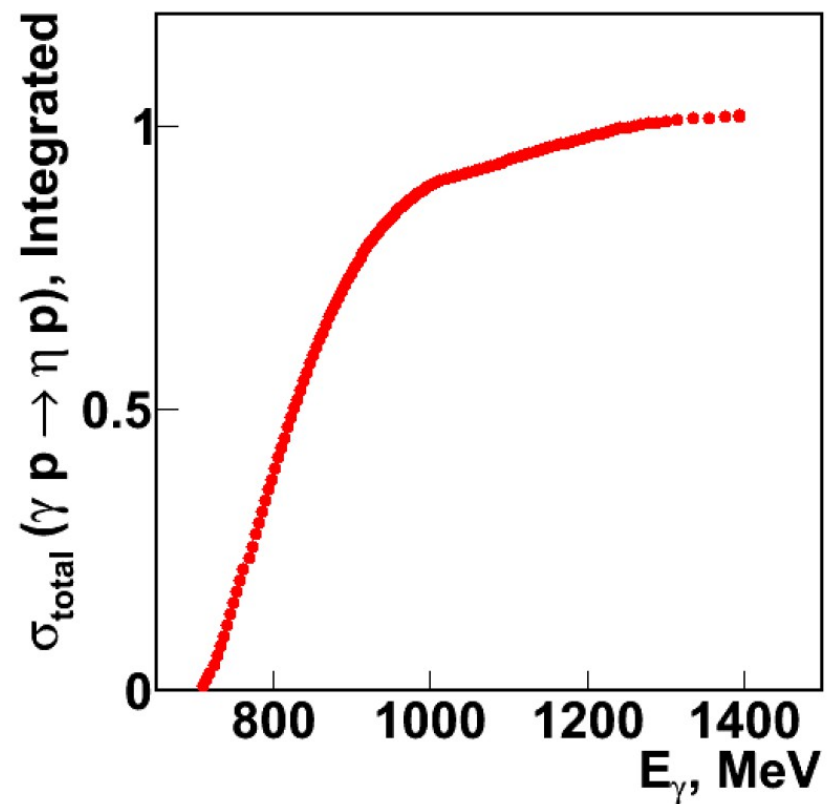
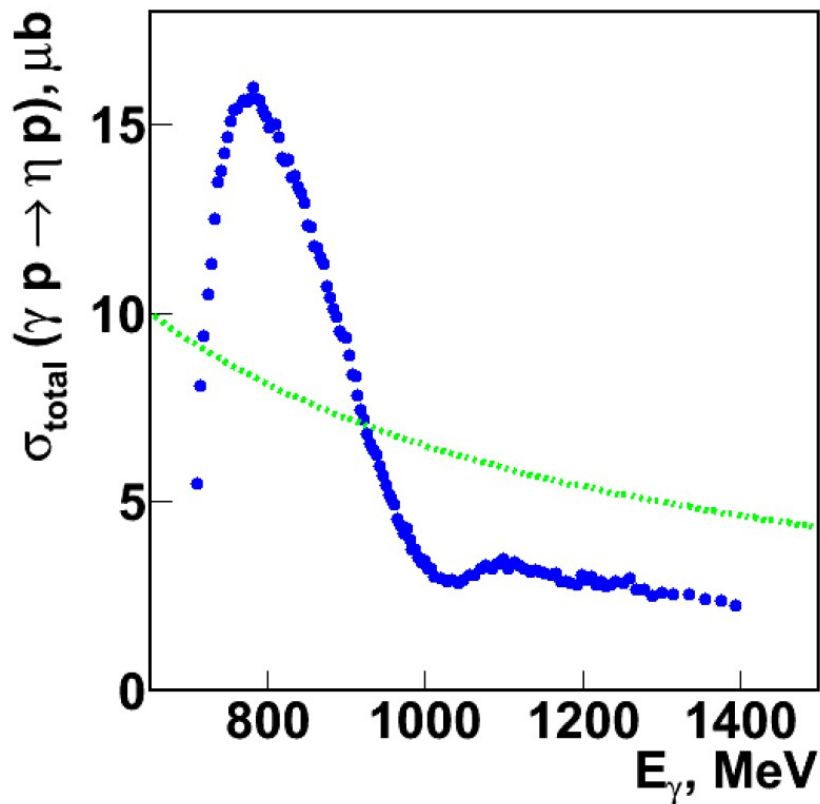
CLAS: M. Dugger et al., Phys. Rev. Lett. 89 (2002) 222002.

Erratum-ibid. 89 (2002) 249904.

SAPHIR: J. Barth et al., Eur. Phys. J. A 18 (2003) 117.

Crystal Barrel: V. Crede et al., Phys. Rev. C 80 (2009) 055202.

η Photoproduction

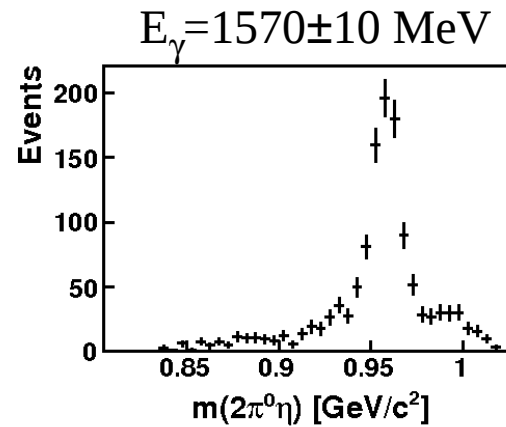
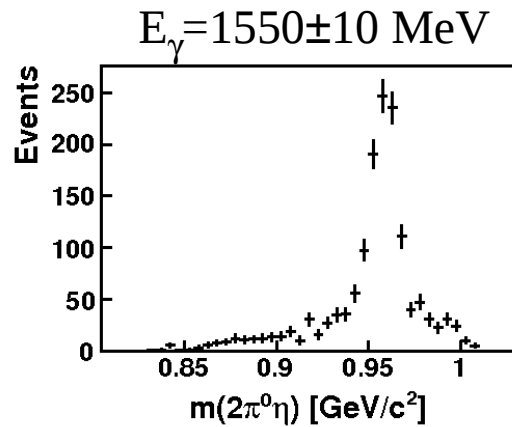
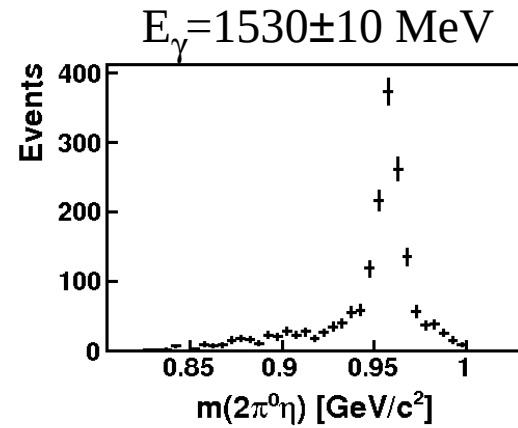
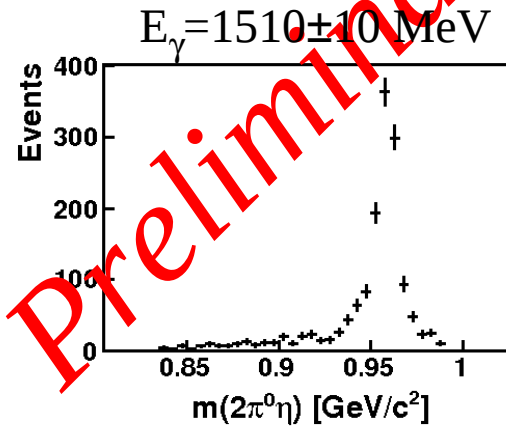
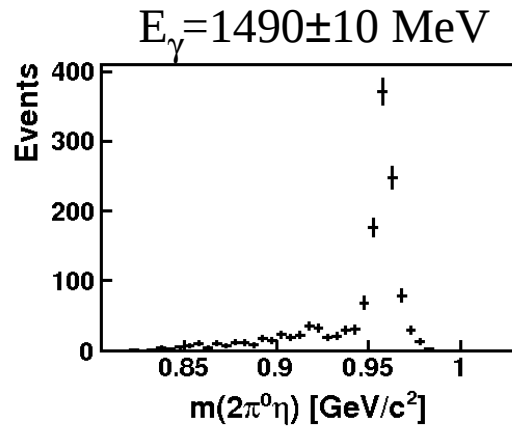
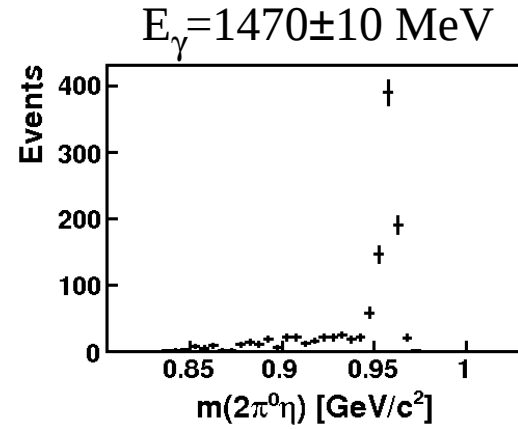
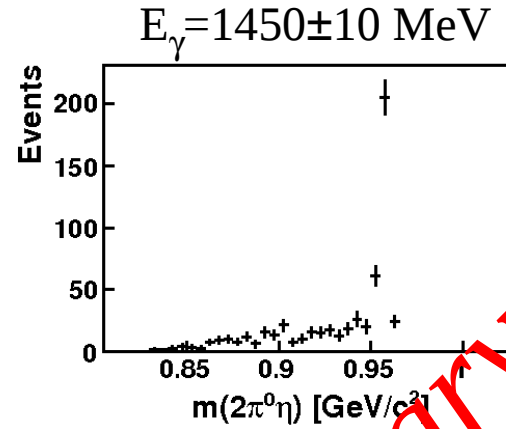
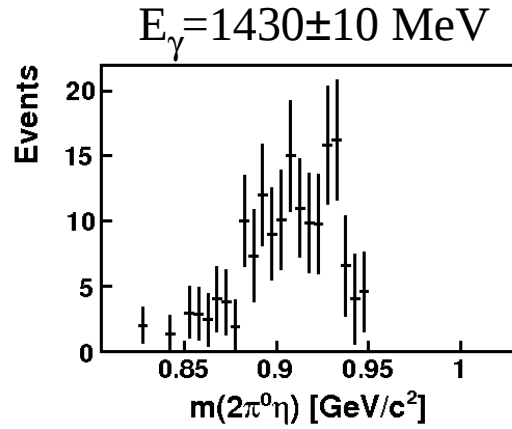


At MAMI a beam of tagged photons of excellent quality is available:

- High intensity photon beam
- Fine energy resolution
- Outstanding stability

Beam energy nearly perfect for high statistics η photoproduction

$\eta' \rightarrow \eta \pi^0 \pi^0$ Invariant Mass

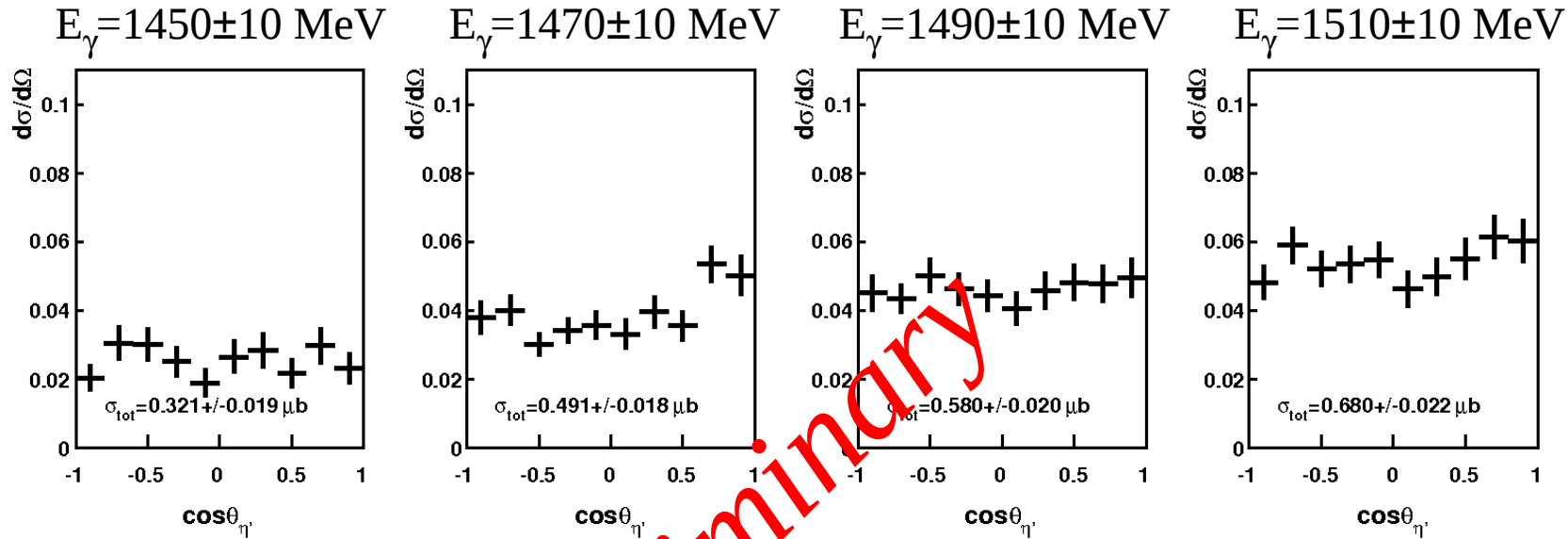


Preliminary

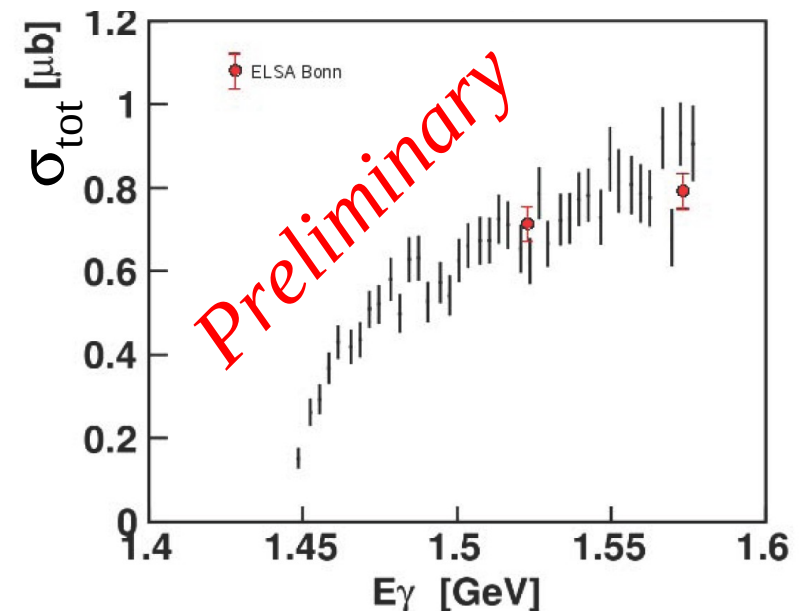
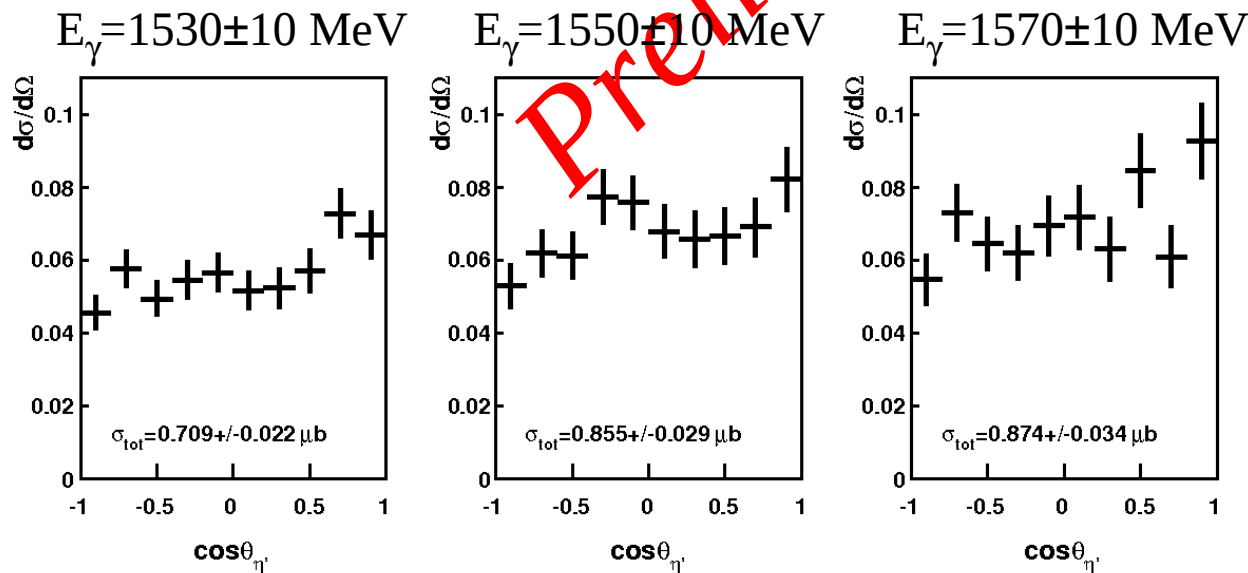
S. Prakhov (UCLA)

η' Cross Section

Using $\eta' \rightarrow \eta\pi^0\pi^0$



S. Prakhov (UCLA)



Preliminary

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$\eta \rightarrow 3\pi$

$\eta \rightarrow 3\pi \rightarrow$ Isospin breaking

$$H_Y = \frac{1}{2}(m_u - m_d)(\bar{u}u - \bar{d}d)$$

Lowest Order χ PT:

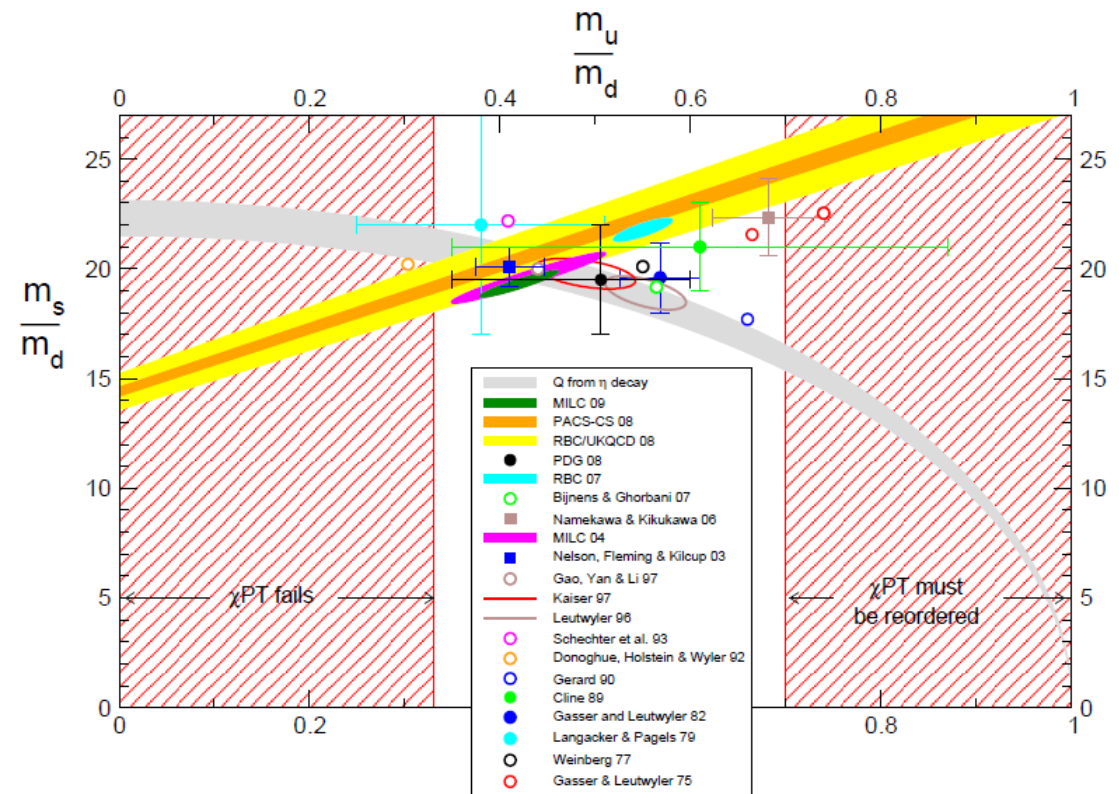
$$A(\eta \rightarrow \pi^+ \pi^- \pi^0) = \frac{B_0(m_u - m_d)}{3\sqrt{3}F_\pi^2} \cdot \frac{3s - 4m_\pi^2}{m_\eta^2 - m_\pi^2}$$

$$A(\eta \rightarrow 3\pi^0) = \frac{B_0(m_u - m_d)}{\sqrt{3}F_\pi^2} \propto (m_u - m_d)$$

$$\Gamma(\eta \rightarrow 3\pi) \propto |A|^2 \propto Q^{-4}$$

$$Q^2 = \frac{m_s^2 - (m_u + m_d)^2/4}{m_d^2 - m_u^2}$$

Allows to extract information
on
quark masses



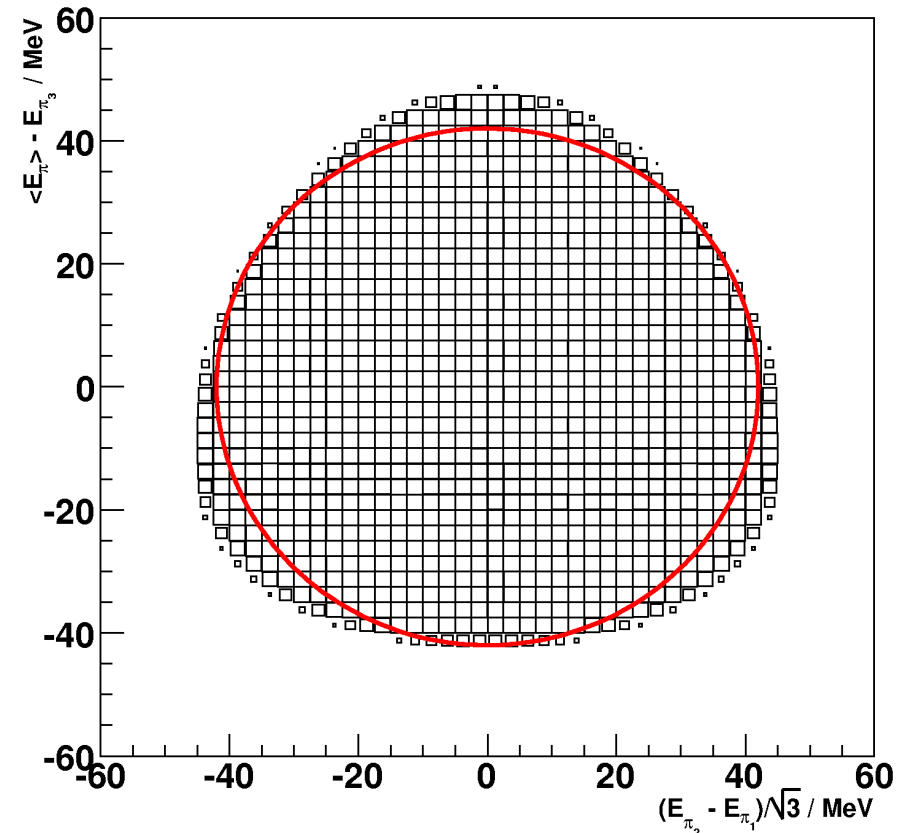
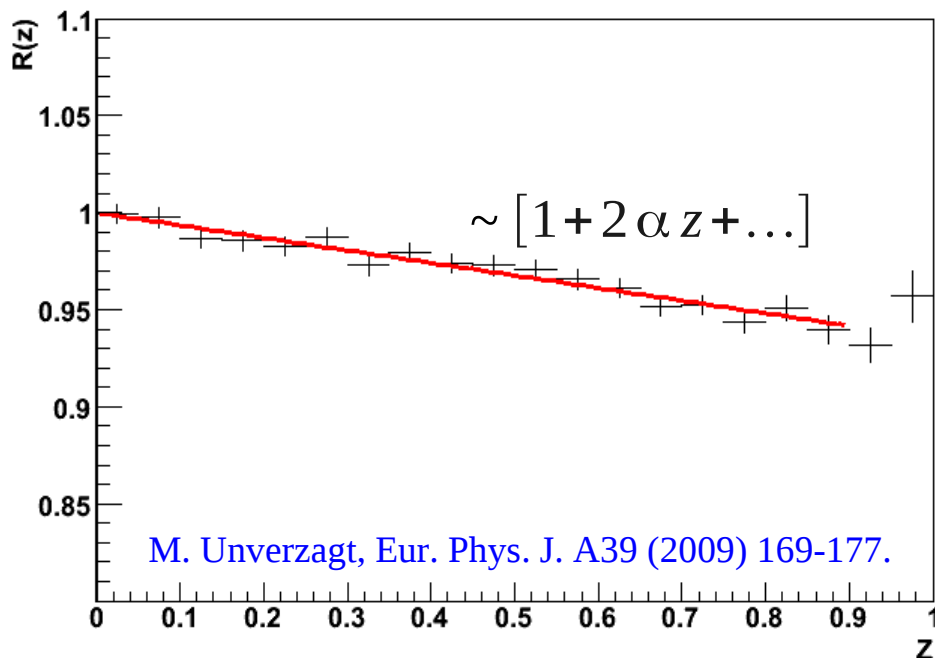
H. Leutwyler, arXiv:0911.1416

$\eta \rightarrow 3\pi$

Parametrization of $\eta \rightarrow 3\pi^0$ Dalitz plot:

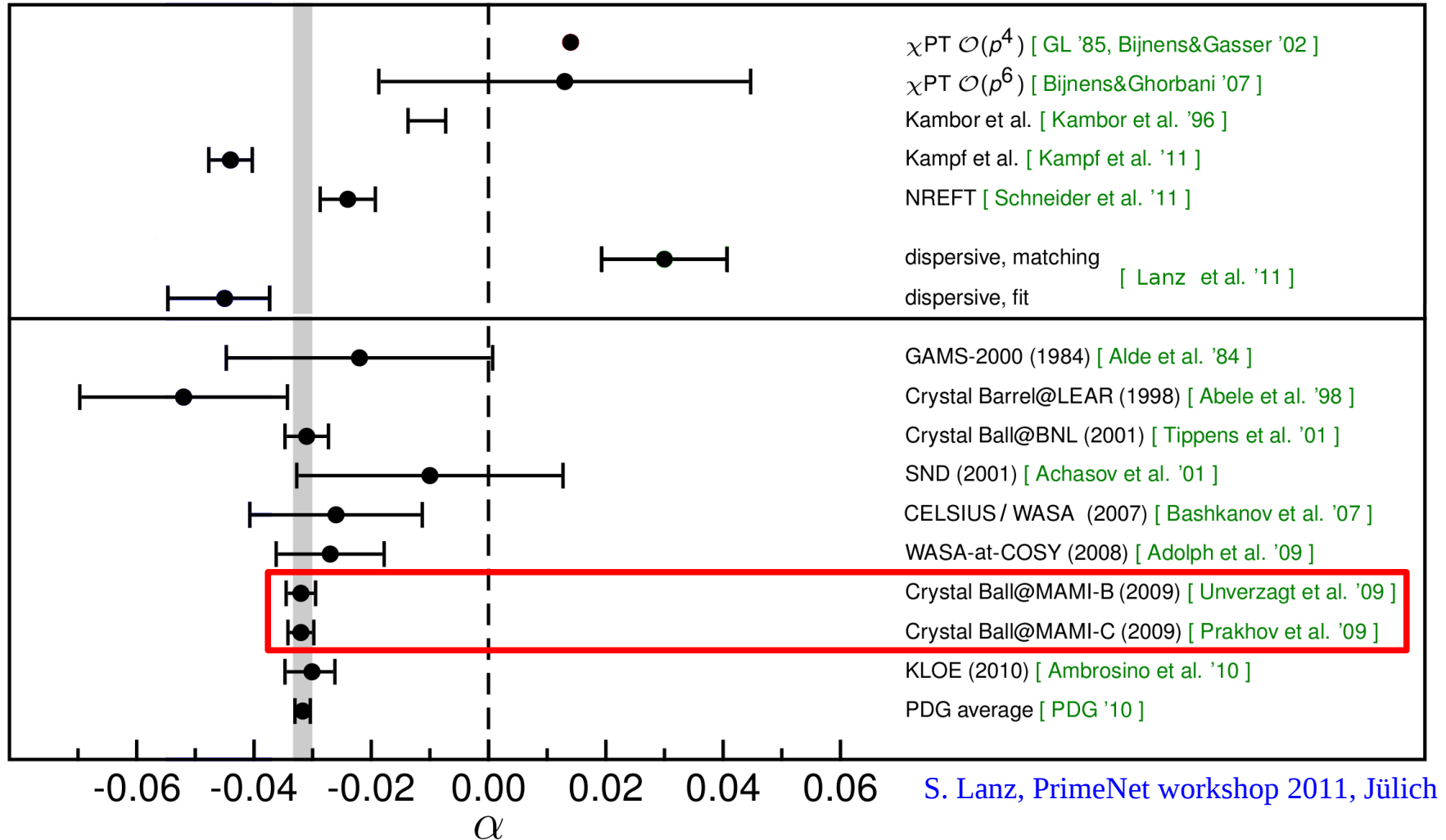
$$|A(\eta \rightarrow 3\pi^0)|^2 = N \cdot (1 + 2\alpha z + \dots)$$
$$z = 6 \sum_{i=1}^3 \left(\frac{E_i - m_\eta/3}{m_\eta - 3m_{\pi^0}} \right)^2 = \frac{\rho^2}{\rho_{max}^2}$$

E_i : π^0 energies in h rest frame,
 ρ : radial distance to center of Dalitz plot



$\eta \rightarrow 3\pi^0$ Dalitz Plot Parameter

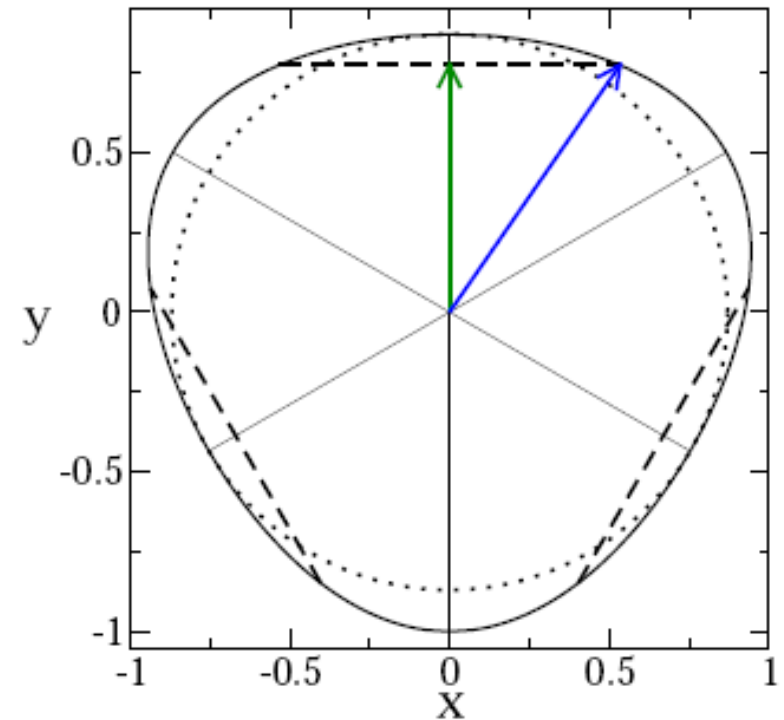
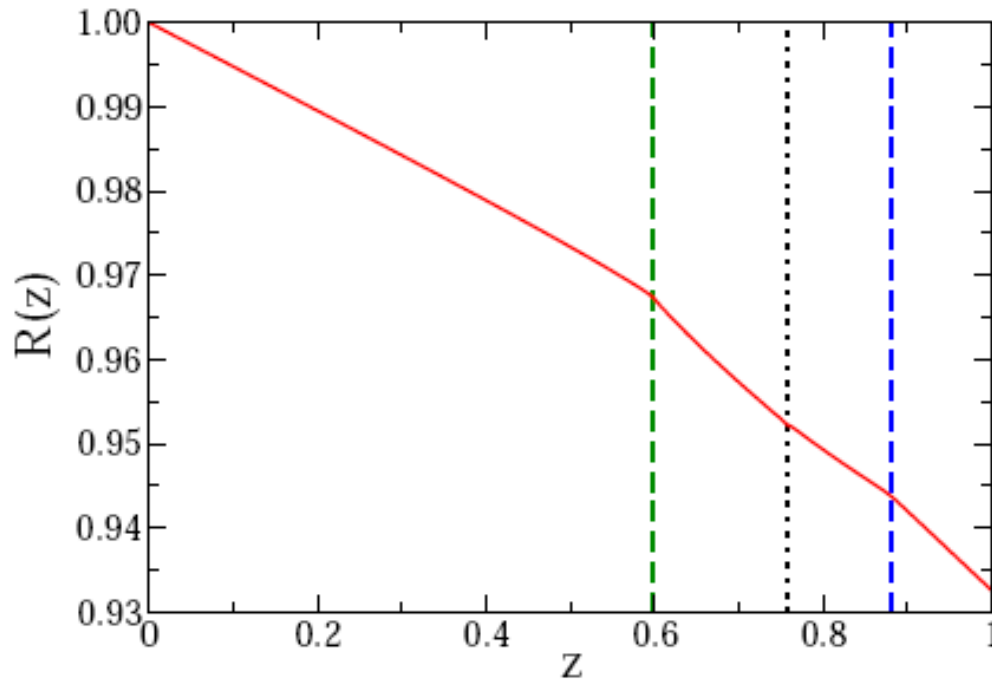
- World's most precise results on $\eta \rightarrow 3\pi^0$ decay from CB at MAMI



Experiments reach precision where higher order effects (cusp-effect, second order term in expansion) become visible

Effect of Cusp in α

Taken from PhD thesis of R. Nissler, University Bonn, 2007.



Cusp has 5% effect on Dalitz Plot Parameter

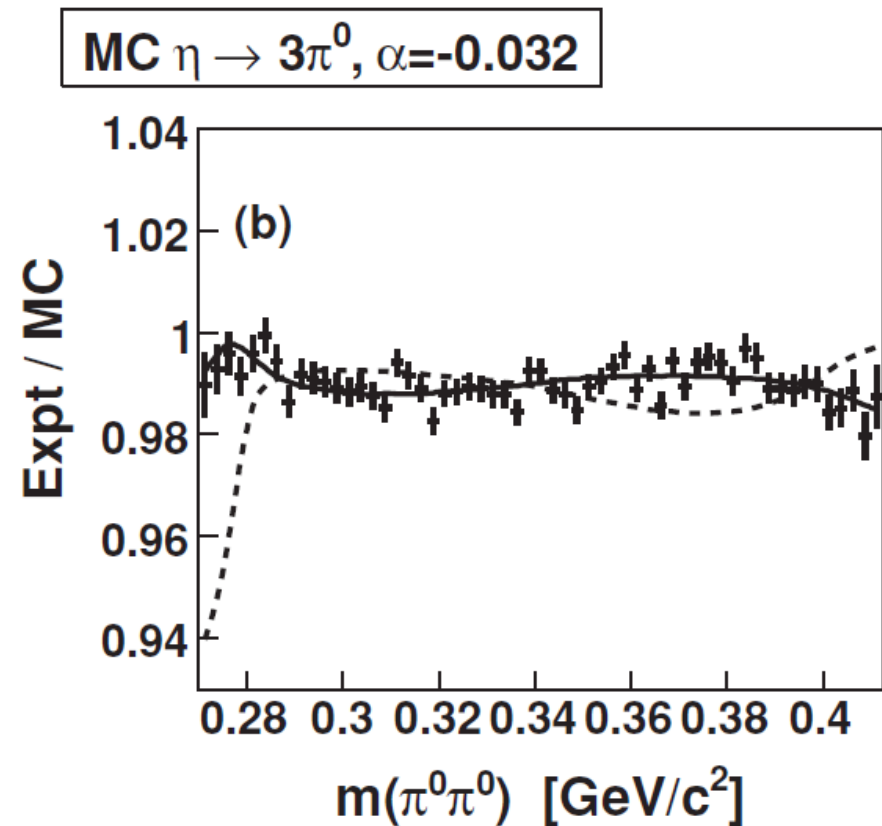
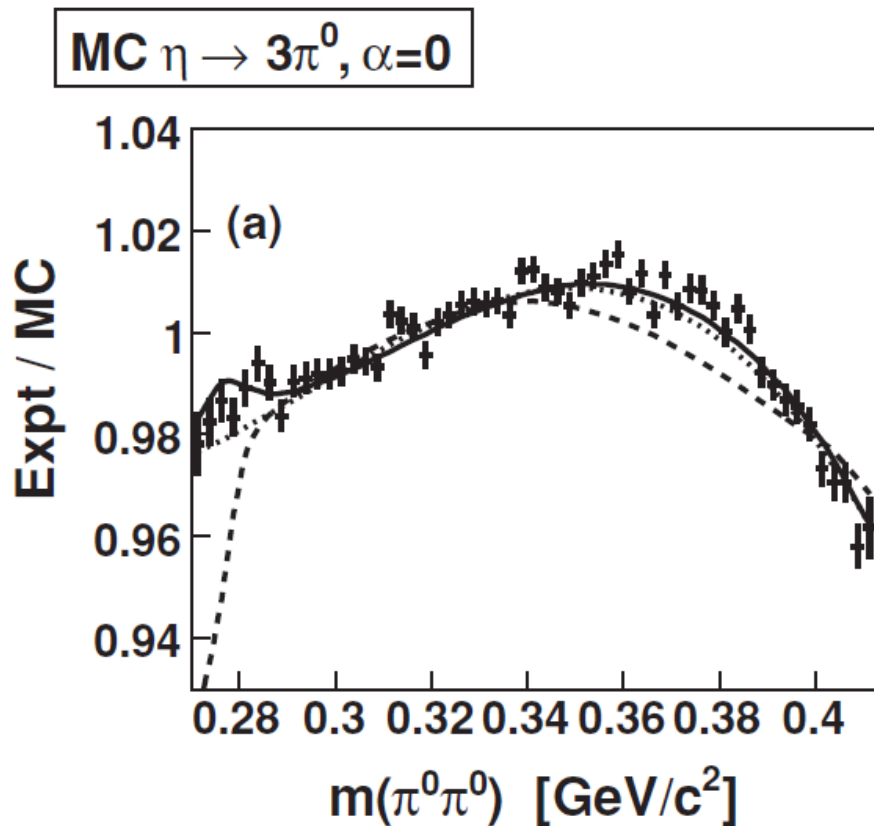
C. Ditsche, B. Kubis, Ulf-G. Meißner, Eur. Phys. J. C 60, 83 (2009).

Further effects:

- Kinematic boundaries
- Second order in amplitude expansion

Cusp-Effect

- $\eta \rightarrow \pi^0 \pi^+ \pi^-$ contributes via $\pi^+ \pi^- \rightarrow \pi^0 \pi^0$
- Cabibbo, Isidori and Bissegger *et al.* have developed framework to extract a_0 - a_2 from $K \rightarrow 3\pi$ (NA48) and $\eta \rightarrow 3\pi$ invariant $\pi^0 \pi^0$ mass spectra
- Cusp effect in η decay only at **few % level** \rightarrow need high precision



S. Prakhov et al. (Crystal Ball at MAMI), Phys. Rev. C **79** (2009) 035204.
Bissegger, Fuhrer, Gasser, Kubis, Rusetsky, Phys.Lett. B **659** (2008), 576 (solid line)
J. Belina, Diploma thesis, University Bern, Switzerland (dashed line).

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Double Radiative $\eta \rightarrow \pi^0 \gamma \gamma$

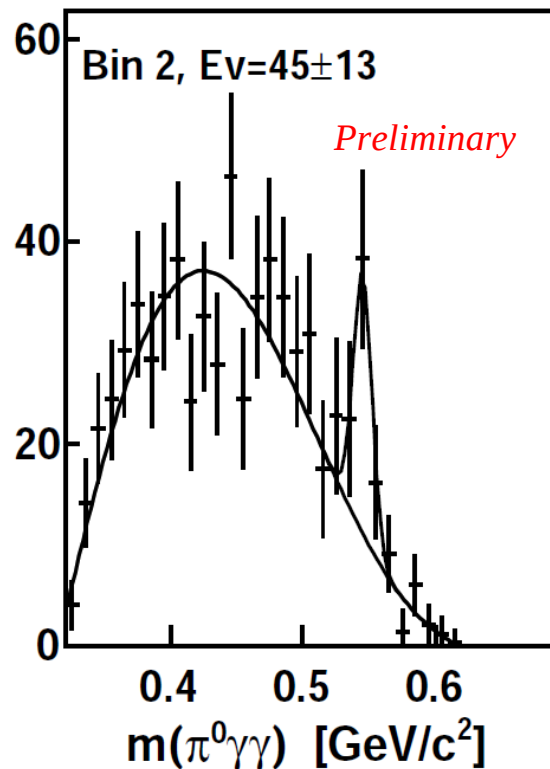
- Tree level amplitudes at $O(p^2)$ and $O(p^4)$ vanish
- π and K loops largely suppressed by G -parity and large Kaon mass
- First sizable contribution from (p^6)
- Coefficients must be determined using models (e.g. VMD)
 - \Rightarrow Stringent test for χ PT at $O(p^6)$ as well as models
- Calculations must describe $\Gamma(\eta \rightarrow \pi^0 \gamma \gamma)$ and differential decay width $d\Gamma/dm^2(\gamma\gamma)$
- Discrepancies between models in $d\Gamma/dm^2(\gamma\gamma)$
- Discrepancies in experimental results for $\Gamma(\eta \rightarrow \pi^0 \gamma \gamma)$
- Experimental challenges:
 - Small rate
 - Large background (e.g. $\pi^0 \pi^0$)
 - Only three measurements of $d\Gamma/dm^2(\gamma\gamma)$: [CB@AGS](#), [CB@MAMI](#), [WASA@COSY](#)
- New [CB@MAMI](#) analysis based on data taken in 2007 and 2009 ($6 \cdot 10^7$ η produced)

Analysis of $\eta \rightarrow \pi^0 \gamma \gamma$

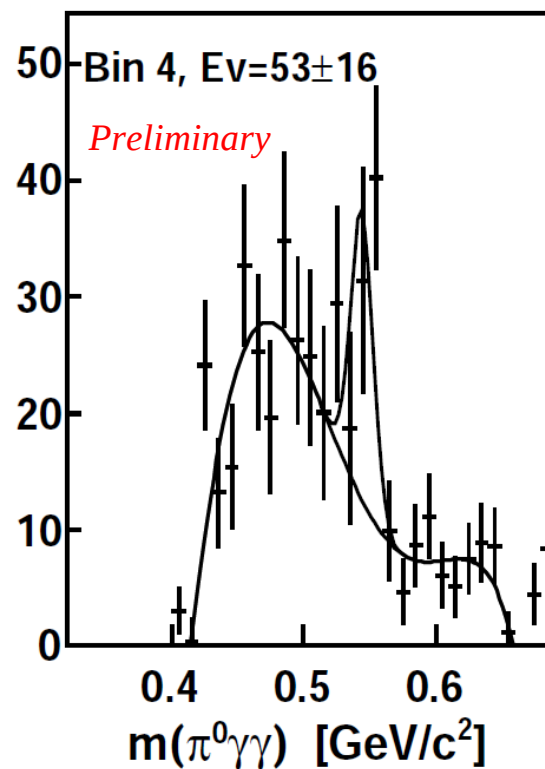
- Based on **kinematic fitting**
- $\pi^0 \pi^0$ background suppressed by anti-hypothesis
- Results based on $1.2 \cdot 10^3$ $\eta \rightarrow \pi^0 \gamma \gamma$ events

- **Below preliminary results from 2009**

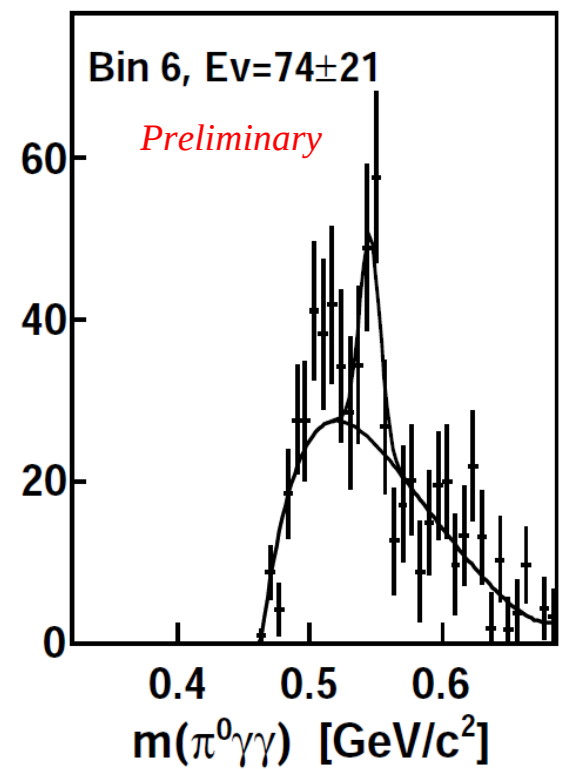
$$m^2(\gamma\gamma) = (0.0375 \pm 0.0100) \text{ GeV}^2/c^4$$



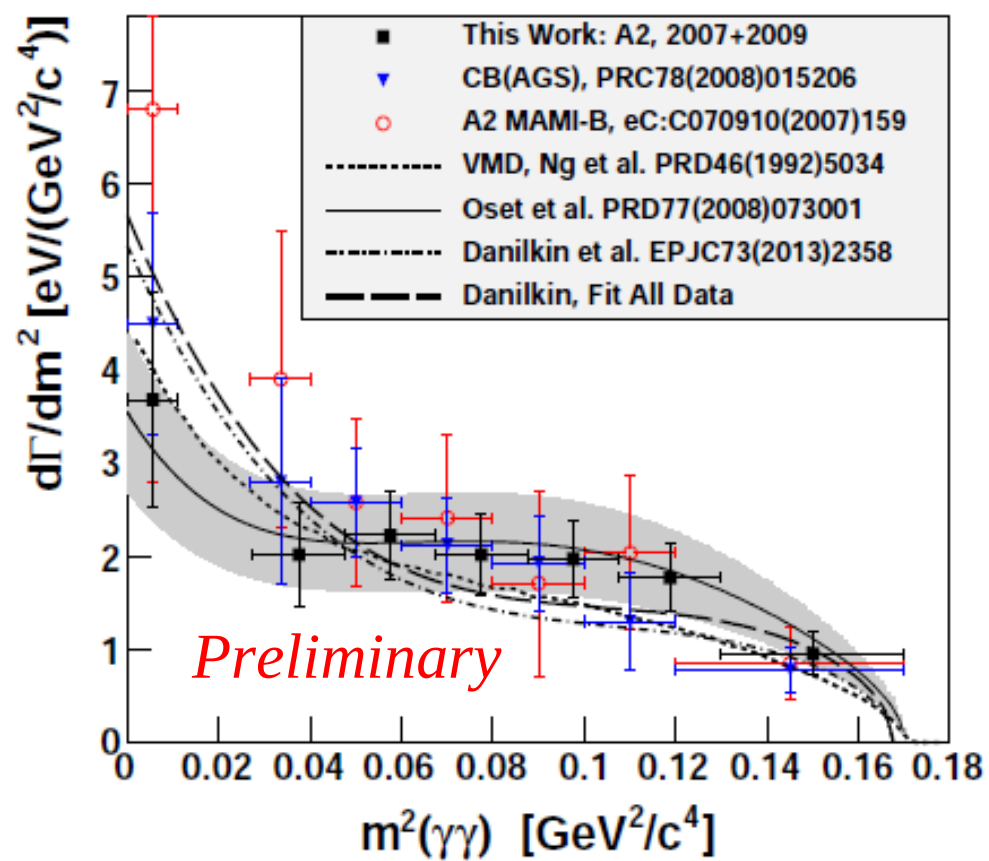
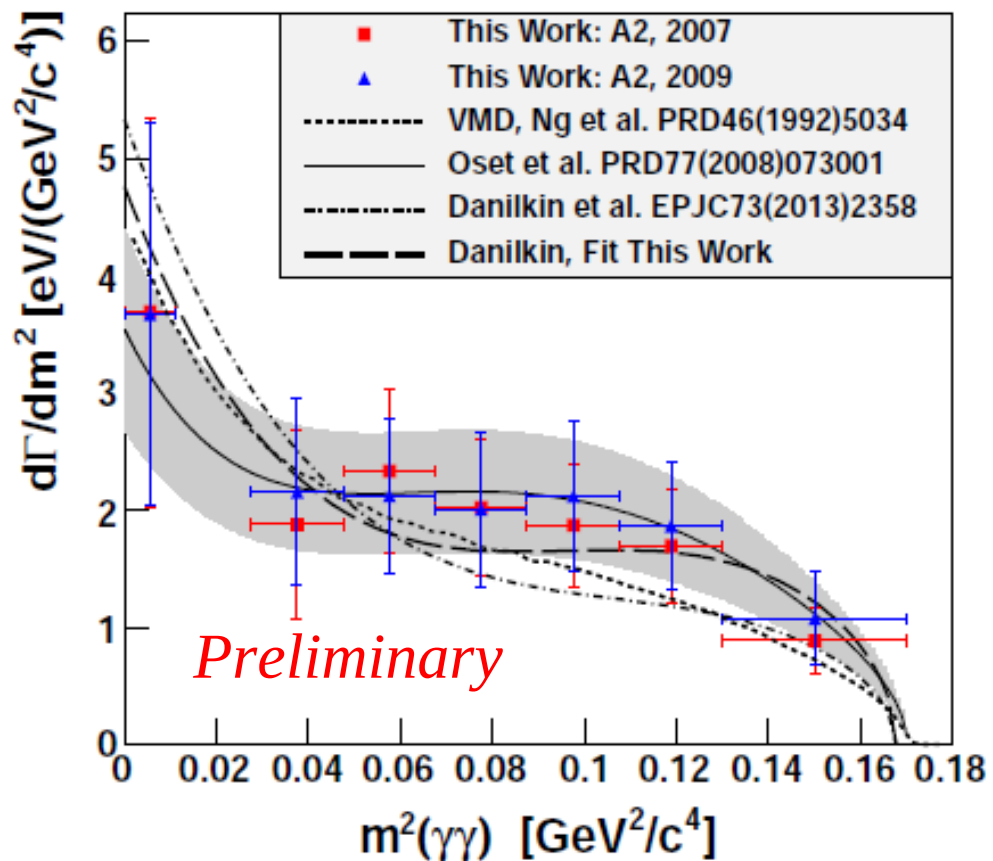
$$m^2(\gamma\gamma) = (0.0775 \pm 0.0100) \text{ GeV}^2/c^4$$



$$m^2(\gamma\gamma) = (0.11875 \pm 0.01125) \text{ GeV}^2/c^4$$

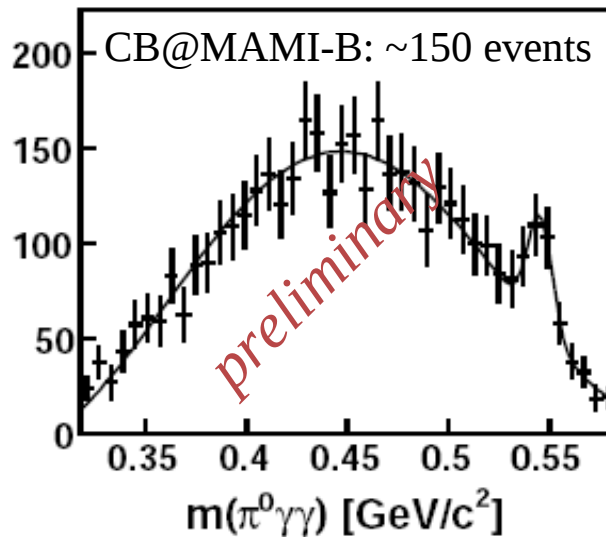


Decay Rate $\eta \rightarrow \pi^0 \gamma \gamma$

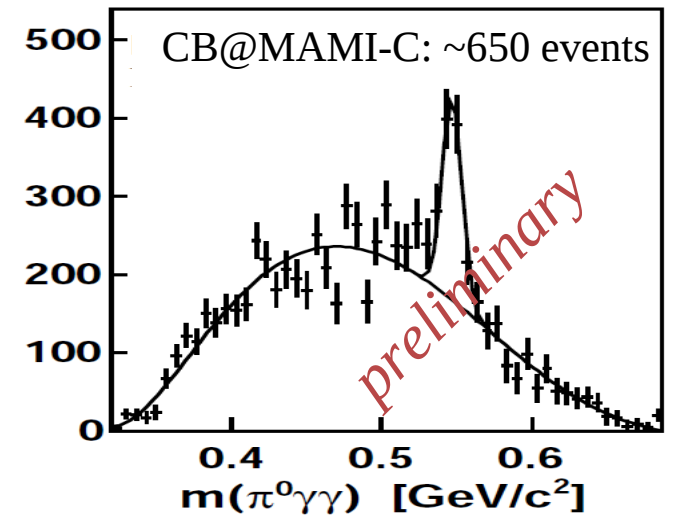


General agreement but statistics still not sufficient to distinguish between models!
Need more statistics to examine Dalitz plot!
To be submitted soon!

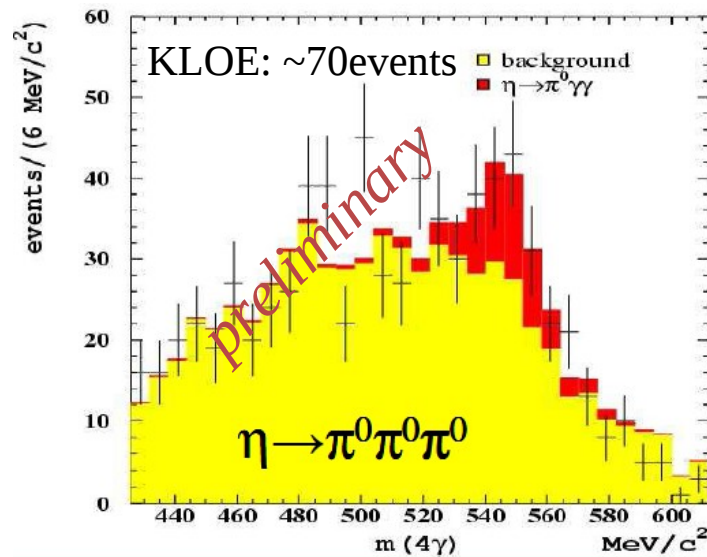
Comparison $\eta \rightarrow \pi^0 \gamma \gamma$



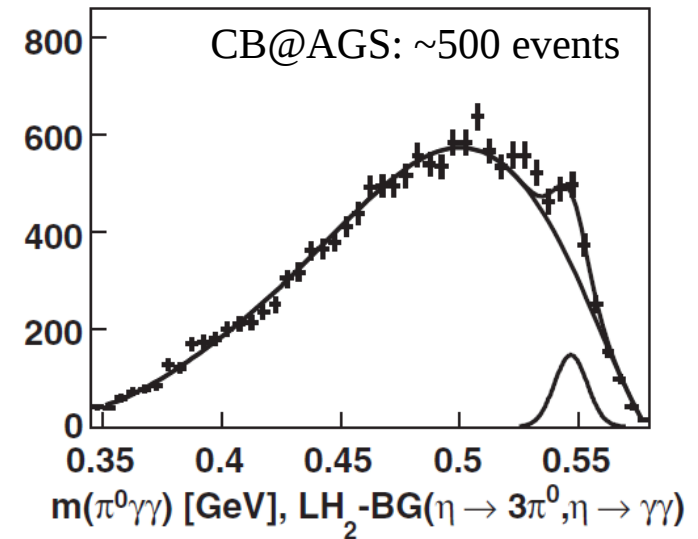
S. Prakhov (UCLA), private communication



S. Prakhov (UCLA), private communication
Only 2007 data set. 2009 has ~400 events.



P. Gauzzi (KLOE), J. Phys. Conf. Ser. **349** (2012) 012002.



S. Prakhov et al. (CB@AGS),
Phys. Rev. C **78**, 015206 (2008)

Decay Width of $\eta \rightarrow \pi^0 \gamma \gamma$

$$\Gamma = (0.84 \pm 0.19) \text{ eV, GAMS2000, 1984}$$

$$\Gamma = (0.45 \pm 0.12) \text{ eV, CB(AGS), 2005}$$

$$\Gamma = (0.11 \pm 0.04) \text{ eV, KLOE, 2006 (preliminary)}$$

$$\Gamma = (0.290 \pm 0.063) \text{ eV, A2(MAMI B), 2007 (preliminary)}$$

$$\Gamma = (0.285 \pm 0.068) \text{ eV, CB(AGS), 2008 (reanalysis of 2005)}$$

$$\Gamma = (0.33 \pm 0.11) \text{ eV, WASA at COSY, Ph.D. thesis of K. Lalwani, 2010 (preliminary)}$$

$$\Gamma = (0.30^{+0.16}_{-0.13}) \text{ eV, VMD, 1992}$$

$$\Gamma = (0.33 \pm 0.08) \text{ eV, Ch. Unitary, 2008}$$

$$\Gamma = 0.31 \text{ eV, Ch. Lagrang., 2012}$$

CB at MAMI (2013): [S. Prakhov \(UCLA, University Mainz\)](#)

- **Data from 2007 and 2009 combined:**

$$\Gamma(\eta \rightarrow \pi^0 \gamma \gamma) = (0.33 \pm 0.03_{\text{tot}}) \text{ eV} \quad \textit{preliminary}$$

- Agreement with latest results, except KLOE
- Most precise value from CB@MAMI

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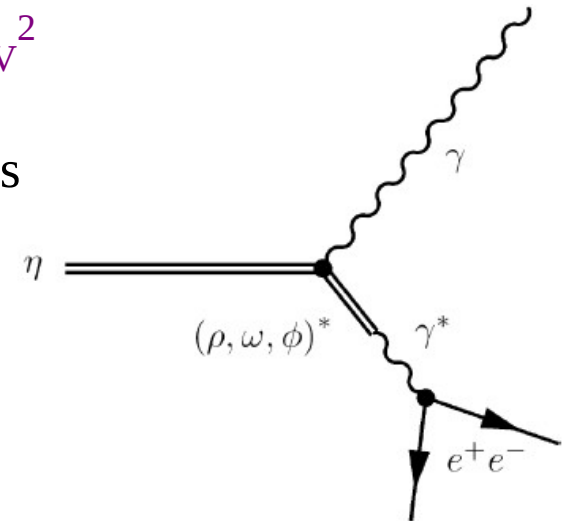
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Transition Form Factor with VMD

- Mechanism especially pronounced in timelike region at $q^2 \approx m_V^2$
 - Virtual meson reaches „mass shell“, becomes real
 - Strong resonance enhancement around vector meson mass
- TFF behaviour, especially for η' , not well known
- TFF modifies differential decay width

$$\frac{d\Gamma}{dm^2} = \left[\frac{d\Gamma}{dm^2} \right]_{\text{QED}} \cdot |F(m^2)|^2$$



- For η often one-pole approximation used:

$$|F(m^2)|^2 = \left(1 - \frac{m^2}{\Lambda^2} \right)^{-2}$$

Exp: $\Lambda \approx 0.72 \text{ GeV} \Rightarrow \Lambda^{-2} = 1.93 \text{ GeV}^{-2}$

VMD: $\Lambda \approx m_\rho = 0.77 \text{ GeV}$

- For η' resonance shape:

$$|F(m^2)|^2 = \frac{\Lambda^2(\Lambda^2 + \gamma^2)}{(\Lambda^2 - m^2)^2 + \Lambda^2\gamma^2}$$

$\Lambda \approx 0.76 \text{ GeV} \quad \gamma \approx 0.10 \text{ GeV}$

- Gain information on structure of meson and η/η' mixing, (dark photon? $\eta \rightarrow \gamma' \gamma \rightarrow e^+e^- \gamma$)

Hadronic LbL Contribution to $a_\mu = (g-2)_\mu$

- QED contributions:

$$a_\mu^{\text{QED}} = (11658471.895 \pm 0.008) \cdot 10^{-10}$$

T. Kinoshita et al., Phys. Rev. Lett. **109** (2012) 111808.

- Electro-Weak contribution:

$$a_\mu^{\text{Weak}} = (15.4 \pm 0.2) \cdot 10^{-10}$$

A. Czarnecki et al., Phys. Rev. D **67** (2003) 073006.

Erratum-ibid. D **73** (2006) 119901.

M. Knecht et al., JHEP 0211 (2002) 003.

- Hadronic vacuum polarisation:

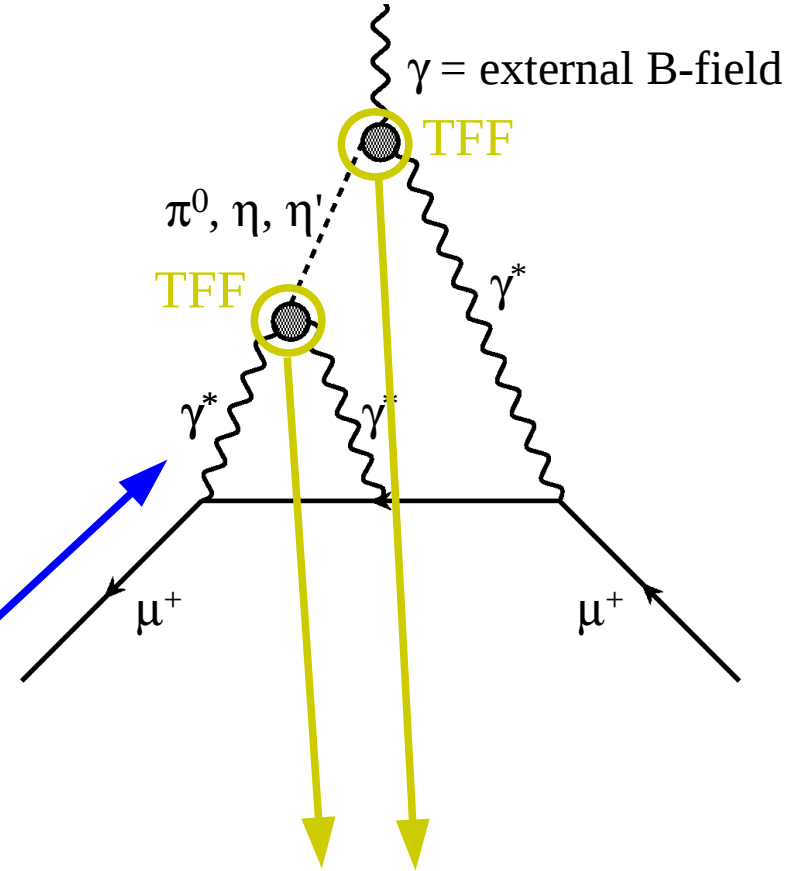
$$a_\mu^{\text{VP}} = (692.3 \pm 4.2) \cdot 10^{-10}$$

M. Davier et al., Eur. Phys. J. C **71** (2011) 1515.

- Hadronic light-by-light:

$$a_\mu^{\text{LbL}} = (10.5 \pm 2.6) \cdot 10^{-10}$$

J. Prades et al., arXiv:0901.0306 (2009).

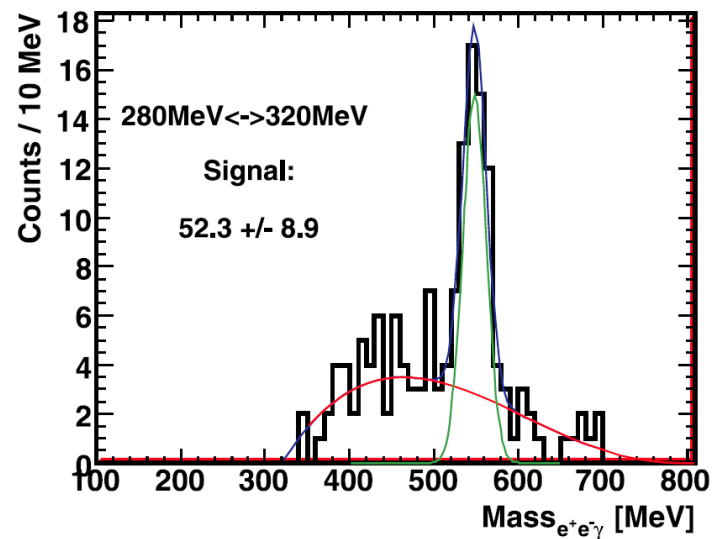
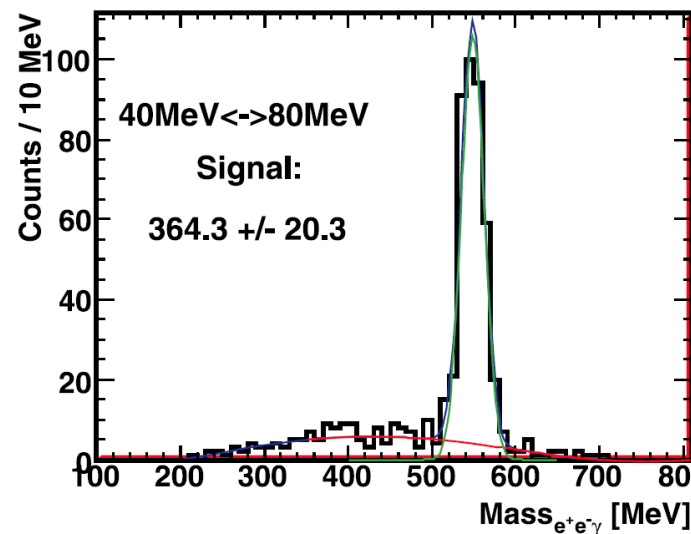
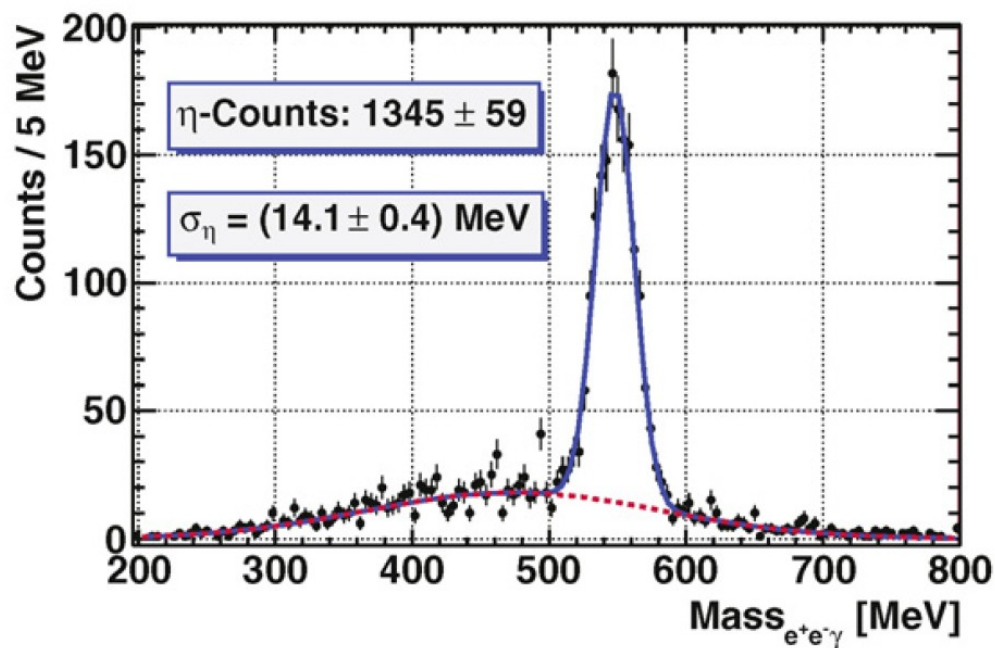


Transition Form Factors of light pseudoscalar mesons could give important input for SM calculations of $(g-2)_\mu$

First A2 Analysis for η TFF

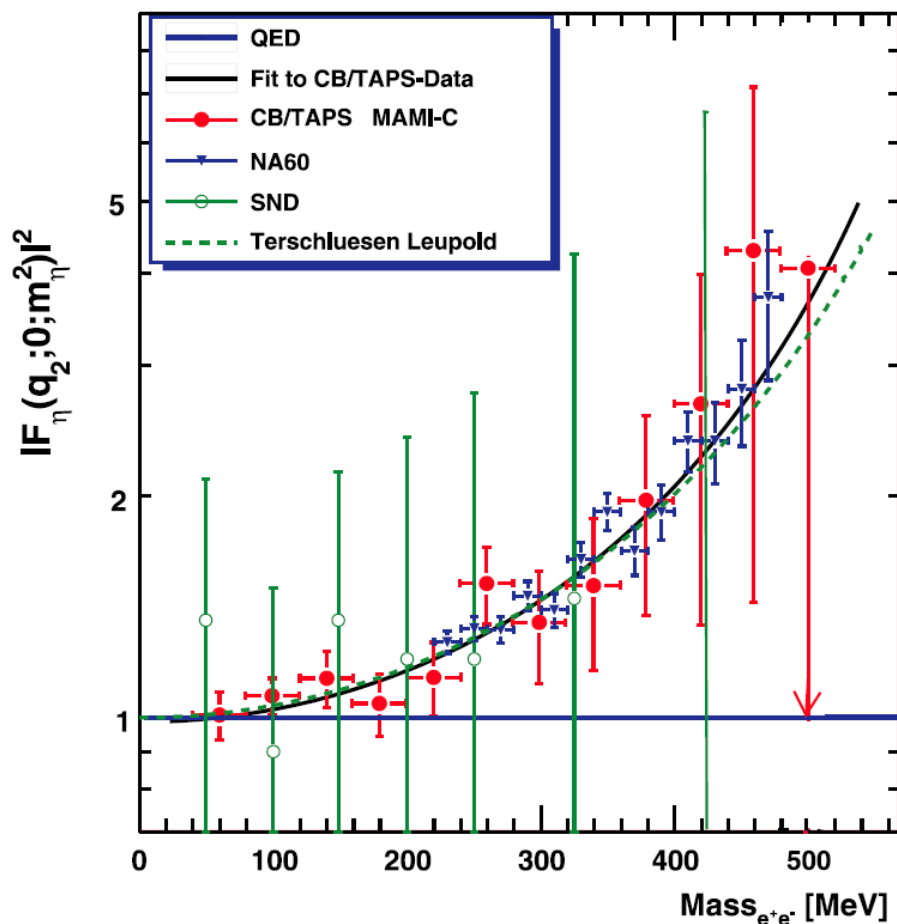
H. Berghäuser et al. (A2-Collaboration), Phys. Rev. B 701 (2011) 562-567.

- Using $\eta \rightarrow e^+e^-\gamma$
- Based on kinematic cuts
- Small amount of data
- Limited photoproduction energy range



First A2 Result for η TFF

H. Berghäuser et al. (A2-Collaboration), Phys. Rev. B 701 (2011) 562-567.



CB/TAPS MAMI-C: 1350 $\eta \rightarrow e^+e^-\gamma$ events
 NA60: 9000 $\eta \rightarrow \mu^+\mu^-\gamma$ events
 SND: 109 $\eta \rightarrow e^+e^-\gamma$ events

$$|F(m^2)|^2 = \left(1 - \frac{m^2}{\Lambda^2}\right)^{-2}$$

$$\Lambda^{-2} = (1.92 \pm 0.35_{\text{stat}} \pm 0.13_{\text{syst}}) \text{ GeV}^{-2}$$

NA60, In-In: R. Arnaldi et al., Phys. Lett. B **677** (2009) 260.

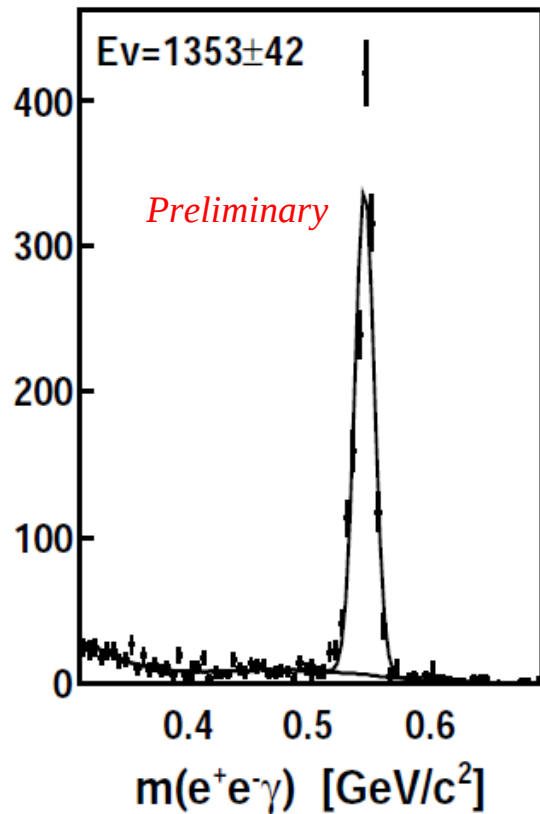
SND: M.N. Achasov et al., Phys. Lett. B **504** (2001) 275.

Terschluesen Leupold: C. Terschluesen, Diploma thesis, University Gießen, Germany, 2010.

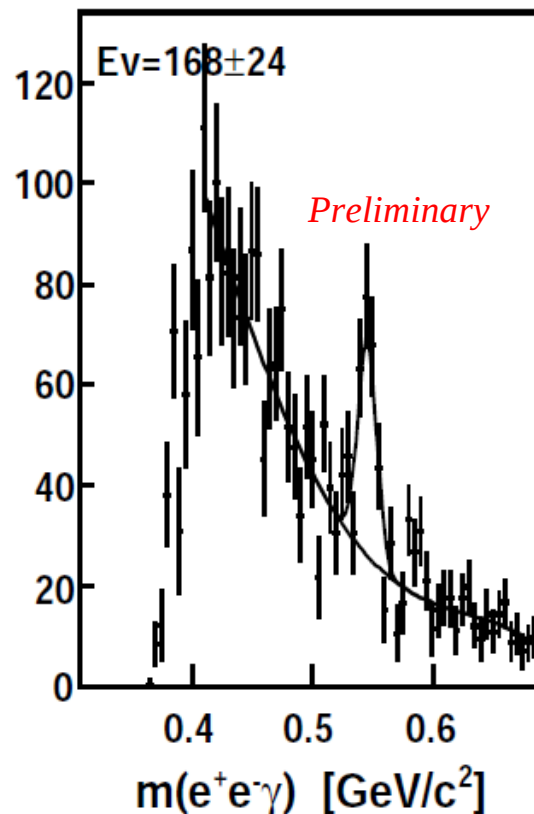
New Analysis of η TFF

- Based on **kinematic fitting**
- **3x** more data
- **Full η photoproduction** range accessible at MAMI used
- **18,000 events** (no proton requirement: 22,000 events), **most precise $\eta \rightarrow e^+e^-\gamma$ up to now**

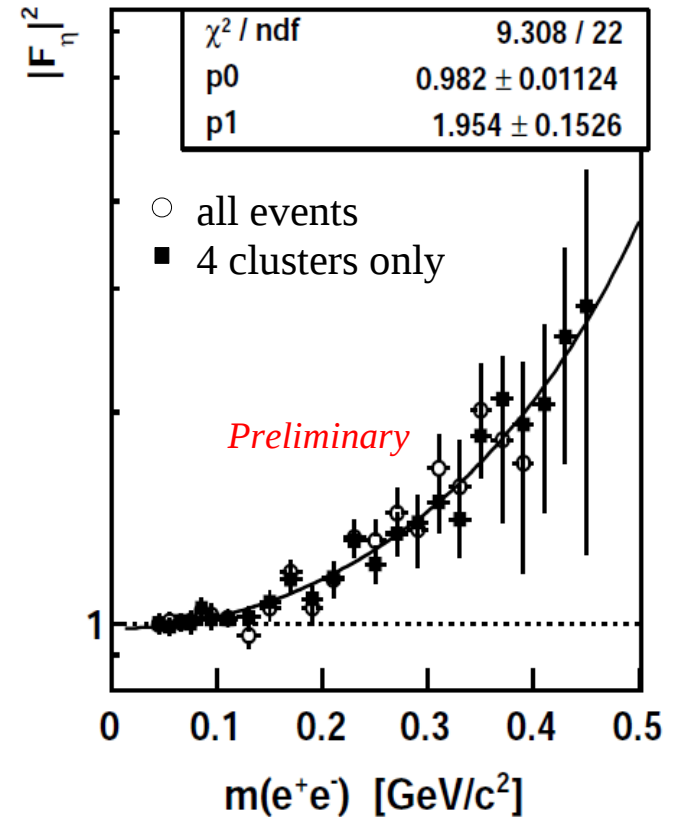
$m(e^+e^-)=45 \pm 5$ MeV



$m(e^+e^-)=285 \pm 5$ MeV

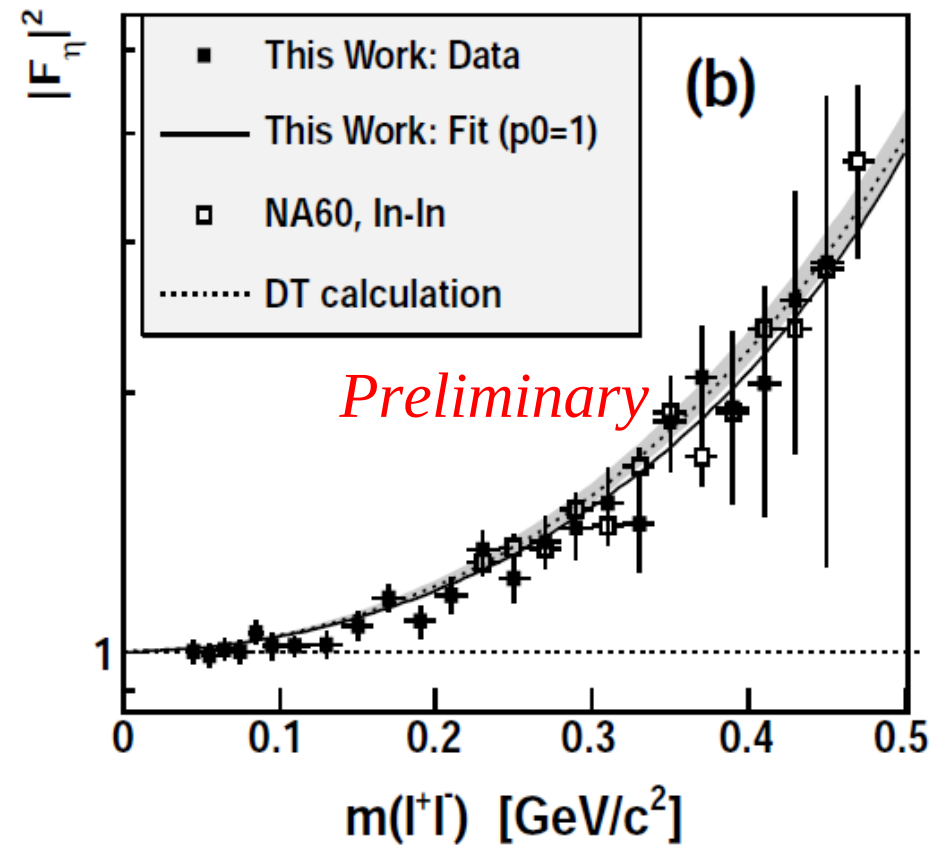
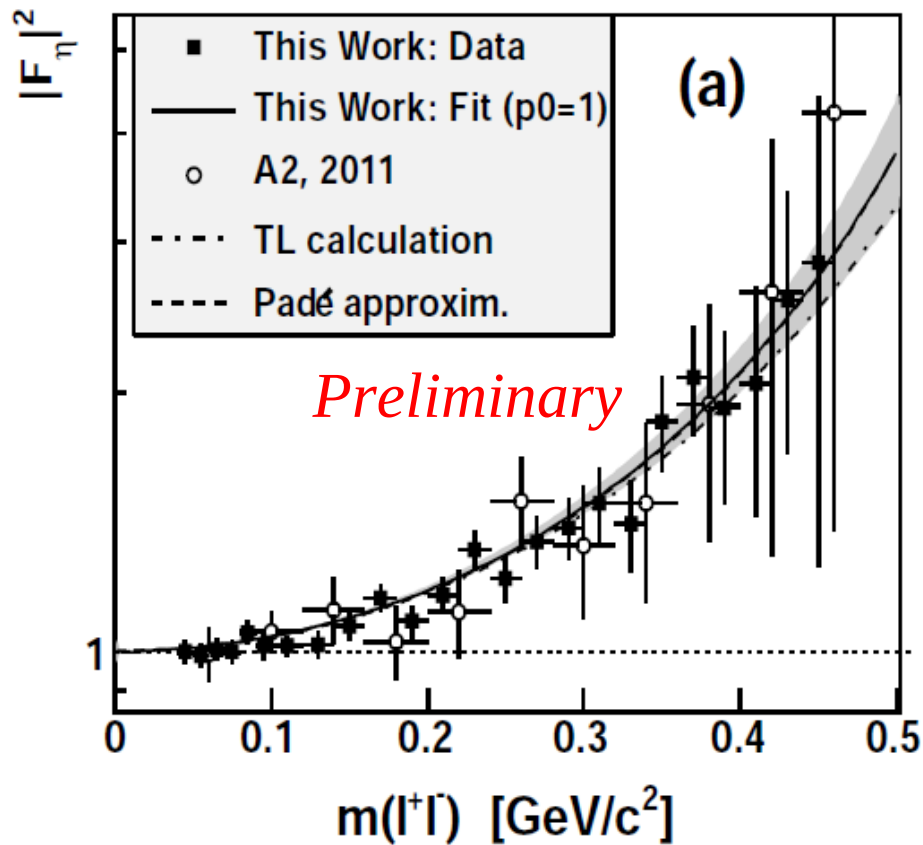


Solid line: Pole-approximation fit
Normalisation p_0 and $\Lambda^{-2}=p_1$ as free parameters



New A2 Result for η TFF

S. Prakhov, M. Unverzagt et al., accepted by Phys. Rev. C, arXiv: 1309.5648 [hep-ex]



$$\Lambda^{-2} = (1.95 \pm 0.15_{\text{stat}} \pm 0.10_{\text{syst}}) \text{ GeV}^{-2} \quad \textit{preliminary}$$

A2, 2011: H. Berghäuser et al., Phys. Rev. B **701** (2011) 562-567.

NA60, In-In: R. Arnaldi et al., Phys. Lett. B **677** (2009) 260.

TL calculation: C. Terschlüsen, Diploma thesis, University Gießen, 2010.

Padé-approximants: R. Escribano, P. Masjuan, P. Sanchez-Puertas, arXiv:1307.2061 [hep-ph].

DT calculation: C. Hahnart, A. Kupś, U.-G. Meißner, F. Stollenwerk, A. Wirzba, Eur. Phys. J. C **73** (2013) 2668.

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C/CP-Violation

Sacharov criterium: C/CP-violation is one of three criteria to explain dominance of matter over antimatter (Baryogenesis)

Electromagnetism, and strong force are assumed to be invariant under C and CP transformation

CP-violation in weak interaction not strong enough to explain Baryogenesis

CHARGE CONJUGATION (C) INVARIANCE

$\Gamma(\pi^0 \rightarrow 3\gamma)/\Gamma_{\text{total}}$	$<3.1 \times 10^{-8}$, CL = 90%
η C-nonconserving decay parameters	
$\pi^+ \pi^- \pi^0$ left-right asymmetry	$(0.09^{+0.11}_{-0.12}) \times 10^{-2}$
$\pi^+ \pi^- \pi^0$ sextant asymmetry	$(0.12^{+0.10}_{-0.11}) \times 10^{-2}$
$\pi^+ \pi^- \pi^0$ quadrant asymmetry	$(-0.09 \pm 0.09) \times 10^{-2}$
$\pi^+ \pi^- \gamma$ left-right asymmetry	$(0.9 \pm 0.4) \times 10^{-2}$
$\pi^+ \pi^- \gamma$ parameter β (D-wave)	-0.02 ± 0.07 (S = 1.3)
$\Gamma(\eta \rightarrow \pi^0 \gamma)/\Gamma_{\text{total}}$	$<9 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow 2\pi^0 \gamma)/\Gamma_{\text{total}}$	$<5 \times 10^{-4}$, CL = 90%
$\Gamma(\eta \rightarrow 3\pi^0 \gamma)/\Gamma_{\text{total}}$	$<6 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow 3\gamma)/\Gamma_{\text{total}}$	$<1.6 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow \pi^0 e^+ e^-)/\Gamma_{\text{total}}$	[a] $<4 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow \pi^0 \mu^+ \mu^-)/\Gamma_{\text{total}}$	[a] $<5 \times 10^{-6}$, CL = 90%
$\Gamma(\omega(782) \rightarrow \eta \pi^0)/\Gamma_{\text{total}}$	$<2.1 \times 10^{-4}$, CL = 90%
$\Gamma(\omega(782) \rightarrow 2\pi^0)/\Gamma_{\text{total}}$	$<2.1 \times 10^{-4}$, CL = 90%
$\Gamma(\omega(782) \rightarrow 3\pi^0)/\Gamma_{\text{total}}$	$<2.3 \times 10^{-4}$, CL = 90%
asymmetry parameter for $\eta'(958) \rightarrow \pi^+ \pi^- \gamma$ decay	-0.03 ± 0.04
$\Gamma(\eta'(958) \rightarrow \pi^0 e^+ e^-)/\Gamma_{\text{total}}$	[a] $<1.4 \times 10^{-3}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \eta e^+ e^-)/\Gamma_{\text{total}}$	[a] $<2.4 \times 10^{-3}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow 3\gamma)/\Gamma_{\text{total}}$	$<1.0 \times 10^{-4}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \mu^+ \mu^- \pi^0)/\Gamma_{\text{total}}$	[a] $<6.0 \times 10^{-5}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \mu^+ \mu^- \eta)/\Gamma_{\text{total}}$	[a] $<1.5 \times 10^{-5}$, CL = 90%
$\Gamma(J/\psi(1S) \rightarrow \gamma \gamma)/\Gamma_{\text{total}}$	$<5 \times 10^{-6}$, CL = 90%

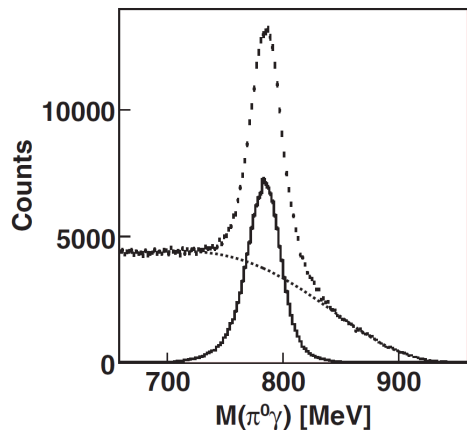
CP INVARIANCE

$\text{Re}(d_{\tau}^W)$	$<0.50 \times 10^{-17}$ e cm, CL = 95%
$\text{Im}(d_{\tau}^W)$	$<1.1 \times 10^{-17}$ e cm, CL = 95%
$\eta \rightarrow \pi^+ \pi^- e^+ e^-$ decay-plane asymmetry	$(-0.6 \pm 3.1) \times 10^{-2}$
$\Gamma(\eta \rightarrow \pi^+ \pi^-)/\Gamma_{\text{total}}$	$<1.3 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow 2\pi^0)/\Gamma_{\text{total}}$	$<3.5 \times 10^{-4}$, CL = 90%
$\Gamma(\eta \rightarrow 4\pi^0)/\Gamma_{\text{total}}$	$<6.9 \times 10^{-7}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \pi^+ \pi^-)/\Gamma_{\text{total}}$	$<2.9 \times 10^{-3}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \pi^0 \pi^0)/\Gamma_{\text{total}}$	$<1.0 \times 10^{-3}$, CL = 90%
$K^{\pm} \rightarrow \pi^{\pm} \pi^+ \pi^-$ rate difference/average	$(0.08 \pm 0.12)\%$
$K^{\pm} \rightarrow \pi^{\pm} \pi^0 \pi^0$ rate difference/average	$(0.0 \pm 0.6)\%$
$K^{\pm} \rightarrow \pi^{\pm} \pi^0 \gamma$ rate difference/average	$(0.9 \pm 3.3)\%$
$K^{\pm} \rightarrow \pi^{\pm} \pi^+ \pi^- (g_+ - g_-) / (g_+ + g_-)$	$(-1.5 \pm 2.2) \times 10^{-4}$
$K^{\pm} \rightarrow \pi^{\pm} \pi^0 \pi^0 (g_+ - g_-) / (g_+ + g_-)$	$(1.8 \pm 1.8) \times 10^{-4}$

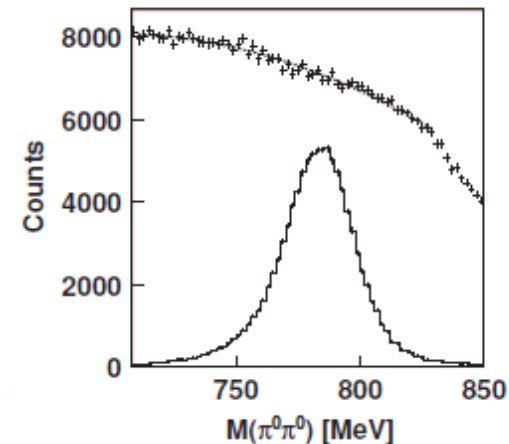
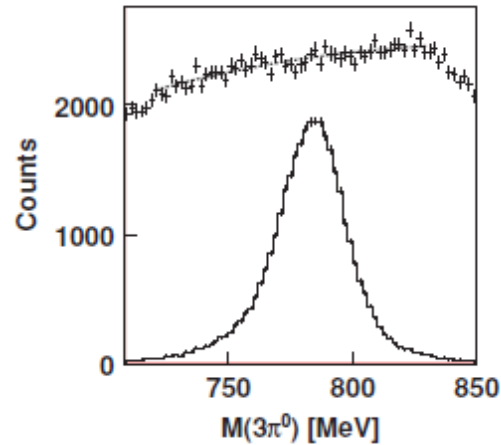
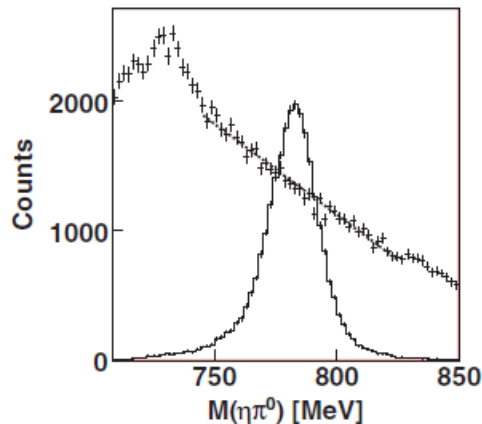
Only weak upper limits

C-Violating ω Decays

- $7 \cdot 10^6$ ω events produced in 3 weeks (parallel to η production)



$1.5 \cdot 10^5$ events



$$\Gamma(\omega \rightarrow \eta\pi^0)/\Gamma_{\text{tot}} < 2.3 \cdot 10^{-4} \quad \text{at 90\% C.L.}$$

$$\Gamma(\omega \rightarrow 3\pi^0)/\Gamma_{\text{tot}} < 2.3 \cdot 10^{-4} \quad \text{at 90\% C.L.}$$

$$\Gamma(\omega \rightarrow 2\pi^0)/\Gamma_{\text{tot}} < 2.4 \cdot 10^{-4} \quad \text{at 90\% C.L.}$$

never been done before

Only CB at MAMI results used by PDG!

A. Starostin et al., Phys. Rev. C 79, 065201 (2009).

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Perspectives for η

Proposed production yields with Crystal Ball at MAMI:

10 weeks: $5 \cdot 10^8 \eta$ (factor 10 improvement)

- Neutral decay modes with unprecedented accuracy with CB:
QCD/ χ PT related (Dalitz plot analysis): $\eta \rightarrow 3\pi^0$
Further effects: kinematic boundaries, second order term in expansion,
cusp effect (few %), $\pi\pi$ -scattering
- Transition Form Factor:
Improve single Dalitz decay $\eta \rightarrow e^+e^-\gamma$
Double Dalitz decay $\eta \rightarrow e^+e^-e^+e^-?$
- C/CP-violation:
 $\eta \rightarrow 2\pi^0\gamma$, $\eta \rightarrow 3\pi^0\gamma$, $\eta \rightarrow 3\gamma$, $\eta \rightarrow 4\pi^0$
- Fix parameters for EFT
Charged decays $\eta \rightarrow \pi^+\pi^-\gamma$, $\eta \rightarrow \pi^+\pi^-\gamma\gamma$
- Measurements of absolute branching ratios/forbidden decays

A. Denig, W. Gradl, M. Ostrick, M. Unverzagt (University Mainz), S. Prakhov, (UCLA/Mainz)

Perspectives for η'

Proposed production yields with Crystal Ball at MAMI:

10 weeks: $2 \cdot 10^7$ η' (factor 4 improvement) in fall 2014

- Neutral decay modes with unprecedented accuracy with CB: unstable particles in EFT
BR($\eta' \rightarrow \omega\gamma/\eta' \rightarrow \eta\pi^0\pi^0$) improve by factor 2-5
PDG 2012: BR($\eta' \rightarrow \omega\gamma/\eta' \rightarrow \eta\pi^0\pi^0$) = 0.147 ± 0.016
- QCD/ χ PT related (Dalitz plot analyses) $\eta' \rightarrow 3\pi^0$, $\eta' \rightarrow \eta\pi^0\pi^0$ (~ 400.000 events expected)
Further effects: cusp effect (8%), $\pi\pi$ - and $\pi\eta$ -scattering
- Transition Form Factor:
Single Dalitz decay $\eta' \rightarrow e^+e^-\gamma$ (800 events proposed)

A. Denig, W. Gradl, M. Ostrick, M. Unverzagt (University Mainz), S. Prakhov, (UCLA/Mainz)

Rate Estimation $\eta' \rightarrow e^+e^-\gamma$

S. Wagner, Master thesis, University Mainz, 2013

M. Unverzagt, A. Denig

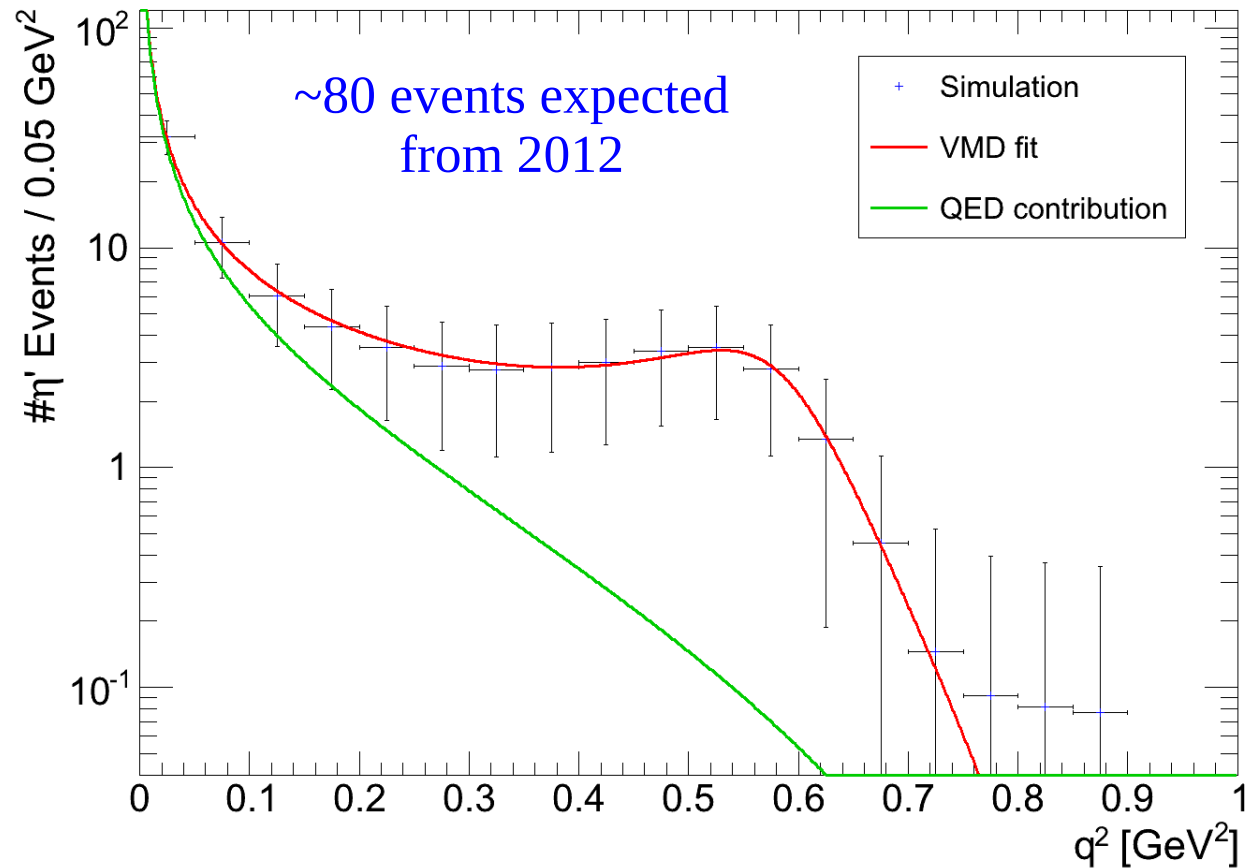
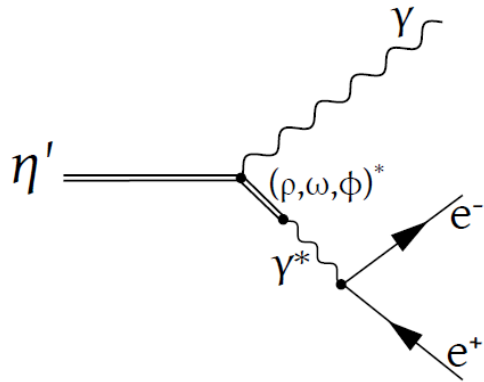
- $\eta' \rightarrow e^+e^-\gamma$ no observation published yet worldwide
- 5.5 weeks of η' photoproduction in 2012
 - Analysis of $\eta' \rightarrow \eta\pi^0\pi^0$
 - Total 1.5 million η' produced
- Simulation based on
 - PDG upper limit for branching ratio
 - 20 background channels simulated
 - Kinematic cuts (try kinematic fit ?)
 - Most critical backgrounds: $\pi^0\pi^0$, $\pi^0\eta$
 - Acceptance $\sim 8.5\%$ (preliminary)
- Expected: ~ 80 $\eta' \rightarrow e^+e^-\gamma$ events from 2012 data

Kanal	σ [μb]	BR	simulierte Statistik
$\eta' \rightarrow e^+e^-\gamma$	0,76	$< 9 \cdot 10^{-4}$	10M
$\eta' \rightarrow \pi^+\pi^-\eta$	0,76	43,40 %	5M
$\eta' \rightarrow \rho^0\gamma$	0,76	29,30 %	8M
$\eta' \rightarrow \mu^+\mu^-\gamma$	0,76	$1,07 \cdot 10^{-4}$	5M
$\eta' \rightarrow \gamma\gamma$	0,76	2,18 %	6M
$\eta \rightarrow e^+e^-\gamma$	1,85	$6,9 \cdot 10^{-3}$	5M
$\eta \rightarrow \pi^+\pi^-\gamma$	1,85	4,60 %	5M
$\eta \rightarrow \pi^+\pi^-\pi^0$	1,85	22,74 %	5M
$\eta \rightarrow \mu^+\mu^-\gamma$	1,85	$3,1 \cdot 10^{-4}$	5M
$\eta \rightarrow \gamma\gamma$	1,85	39,31 %	5M
$\omega \rightarrow e^+e^-\pi^0$	6,44	$7,7 \cdot 10^{-4}$	5M
$\omega \rightarrow \pi^+\pi^-\pi^0$	6,44	89,20 %	5M
$\omega \rightarrow \pi^+\pi^-$	6,44	1,53 %	5M
$\rho^0 \rightarrow e^+e^-$	19,00	$4,72 \cdot 10^{-5}$	5M
$\rho^0 \rightarrow \pi^+\pi^-$	19,00	$\sim 100\%$	5M
$\pi^0 \rightarrow e^+e^-\gamma$	10,52	1,17 %	5M
$\pi^0 \rightarrow \gamma\gamma$	10,52	98,82 %	10M
$\gamma p \rightarrow \pi^+\pi^-\pi^0$	15,00	—	5M
$\gamma p \rightarrow \pi^+\pi^-$	68,62	—	10M
$\pi^0\pi^0 \rightarrow 4\gamma$	6,87	97,65 %	20M
$\pi^0\eta \rightarrow 4\gamma$	4,09	38,85 %	20M

Time-like TFF for η'

S. Wagner, Master thesis, University Mainz, 2013

M. Unverzagt, A. Denig



$$|F(m^2)|^2 = \frac{\Lambda^2(\Lambda^2 + \gamma^2)}{(\Lambda^2 - m^2)^2 + \Lambda^2\gamma^2}$$

- New Goal: $\sim 800 \eta' \rightarrow e^+e^-\gamma$ events in fall 2014 measurement
- Only possible if acceptance holds, has to be improved (use kinematic fit?)
- Next: analyse old data (S. Prakhov, S. Wagner)

Perspectives for η'

Proposed production yields with Crystal Ball at MAMI:

10 weeks: $2 \cdot 10^7$ η' (factor 4 improvement) in fall 2014

- Neutral decay modes with unprecedented accuracy with CB: unstable particles in EFT
BR($\eta' \rightarrow \omega\gamma/\eta' \rightarrow \eta\pi^0\pi^0$) improve by factor 2-5
PDG 2012: BR($\eta' \rightarrow \omega\gamma/\eta' \rightarrow \eta\pi^0\pi^0$) = 0.147 ± 0.016
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Further effects: cusp effect (8%), $\pi\pi$ - and $\pi\eta$ -scattering
- Transition Form Factor:
Single Dalitz decay $\eta' \rightarrow e^+e^-\gamma$ (800 events proposed)
Double Dalitz decay $\eta' \rightarrow e^+e^-e^+e^-$?
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Charged decays $\eta' \rightarrow \pi^+\pi^-\gamma$, $\eta' \rightarrow \pi^+\pi^-\gamma\gamma$
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A. Denig, W. Gradl, M. Ostrick, M. Unverzagt (University Mainz), S. Prakhov, (UCLA/Mainz)

Perspectives for ω

Proposed production yields with Crystal Ball at MAMI:

8 weeks: $2 \cdot 10^8$ ω (factor 30 improvement)

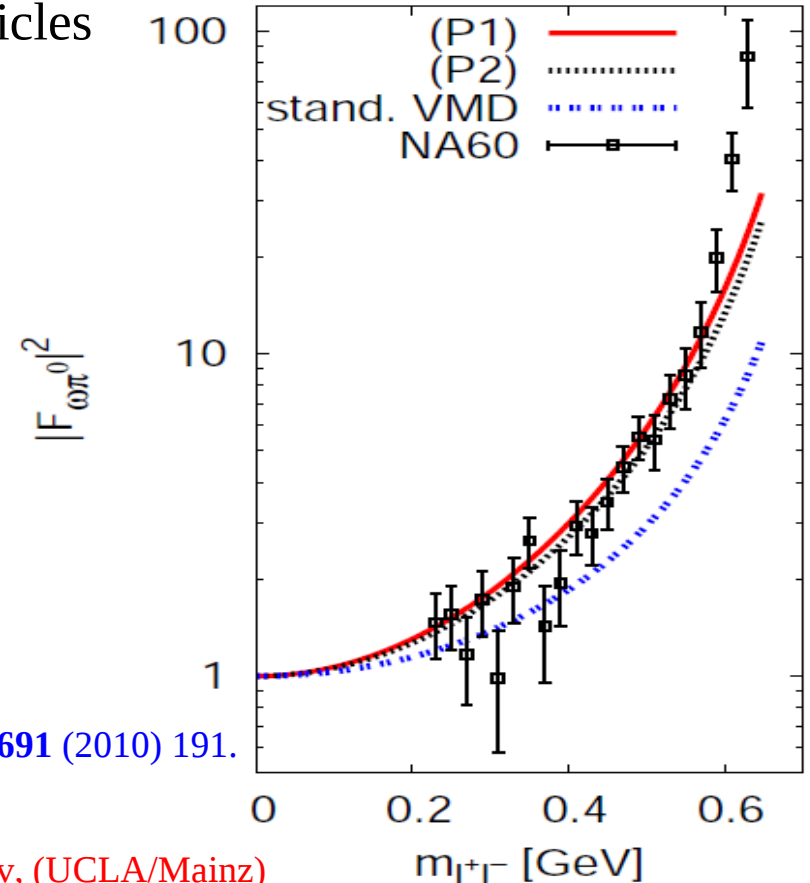
Neutral decay modes with unprecedented accuracy with CB:

- BR($\omega \rightarrow \eta\gamma/\omega \rightarrow \pi^0\gamma$) improve by factor 2-5

PDG 2010: BR($\omega \rightarrow \eta\gamma/\omega \rightarrow \pi^0\gamma$) = 0.0098 ± 0.0024 (not used anymore)

$\omega \rightarrow \eta\gamma/\omega \rightarrow \pi^0\gamma$: power counting for unstable particles
in effective field theory

- Transition Form Factor for $\omega \rightarrow \pi^0 e^+ e^-$



C. Terschlüssen, S. Leupold, Phys. Lett. B **691** (2010) 191.

A. Denig, W. Gradl, M. Ostrick, M. Unverzagt (University Mainz), S. Prakhov, (UCLA/Mainz)

Perspectives for π^0

C-violating decay: $\pi^0 \rightarrow 3\gamma$

Current bound: $BR(\pi^0 \rightarrow 3\gamma) < 3.1 \cdot 10^{-8}$ (90 %C.L.)

Crystal Box Experiment at Los Alamos in $\pi^- + p \rightarrow \pi^0 + n$

J. McDonough et al., Phys. Rev. **D38** (1988) 2121.

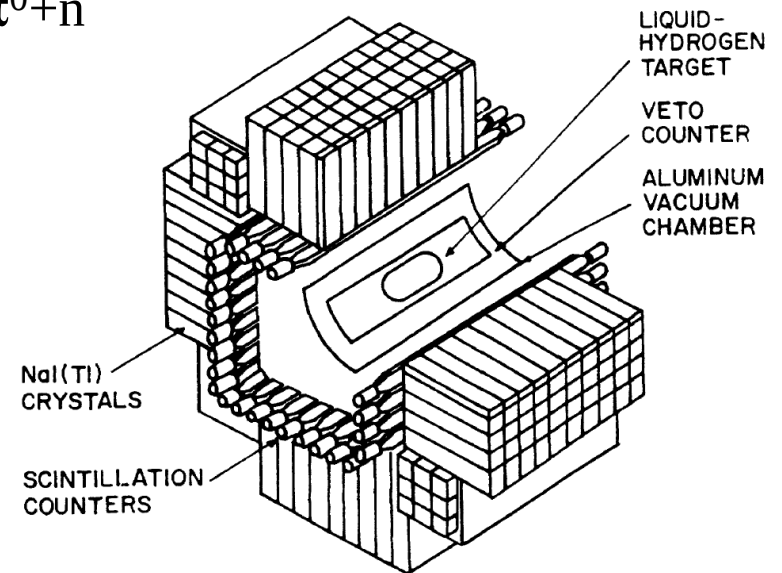
Main background channels:

$\pi^0 \rightarrow 2\gamma$

$\pi^0 \rightarrow e^+e^-\gamma$

$\pi^0\pi^0$ production

Reduce at trigger level
by factor 100!



$\pi^0 \rightarrow 4\gamma$ (allowed high order process, never seen yet, can be improved in parallel)

$BR(\pi^0 \rightarrow 4\gamma) < 2 \cdot 10^{-8}$ (90 %C.L.)

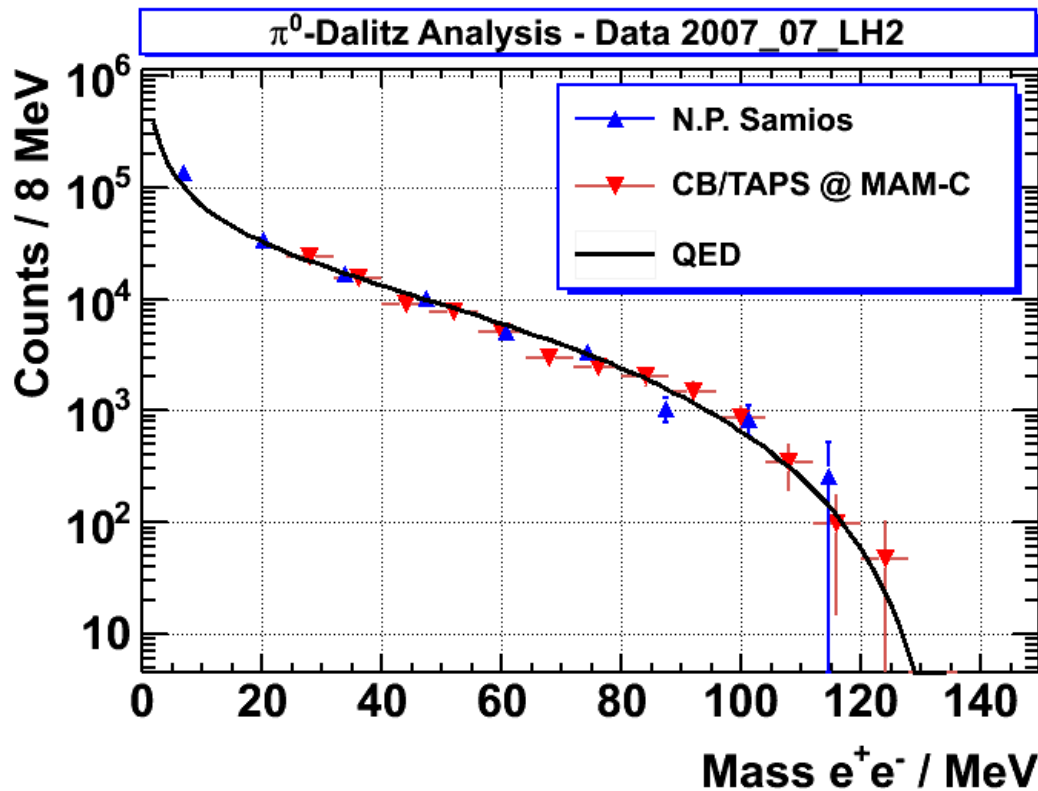
J. McDonough et al., Phys. Rev. **D38** (1988) 2121.

$$BR_{4\gamma}^{\text{QED}} = \frac{\Gamma_{\pi^0 \rightarrow 4\gamma}}{\Gamma_{\pi^0 \rightarrow 2\gamma}} \sim 2.6 \cdot 10^{-11} \quad \longleftrightarrow \quad BR_{4\gamma}^{\text{hadr}} \sim 10^{-9} - 7.1 \cdot 10^{-18}$$

W. Gradl, M. Unverzagt, Jennifer Wettig (University Mainz), G. Ron (Jerusalem)

Conclusion π^0

- Within 100h of beamtime on ^{208}Pb or ^{236}U upper limits for $\pi^0 \rightarrow 3\gamma/4\gamma$ may be improved by up to two orders of magnitude, deviations from Standard Model indicate New Physics
- Pilot test for more rare decays (also η/ω ?) and possibly decay studies with higher rate
- Especially look at $\pi^0 \rightarrow e^+e^-\gamma$



N.P. Samios et al. (BNL), Phys. Rev. 121 (1961) 275-281.

H. Berghäuser, PhD Thesis, University Gießen, Germany, 2010.

W. Gradl, M. Unverzagt, Jennifer Wettig (University Mainz), G. Ron (Jerusalem)

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Summary

- **World leading results** from Crystal Ball at MAMI
Dalitz plot parameter: $\eta \rightarrow 3\pi^0$
 χ PT, VMD: $\eta \rightarrow \pi^0\gamma\gamma$
Transition Form Factor: $\eta \rightarrow e^+e^-\gamma$
C-violation: neutral ω decays
- Further analyses in η/ω decays possible with existing data
- Main focus: η' studies
Data taking planned for 2nd half of 2014
Goals: 400,000 $\eta' \rightarrow \eta\pi^0\pi^0$
800 $\eta' \rightarrow e^+e^-\gamma$
- New programme with **very rare decays** under investigation
 $\pi^0 \rightarrow 3\gamma/4\gamma$, extend to other rare π^0 , η , ω decays
- New detector possibilities under discussion

Chiral Symmetry Breaking

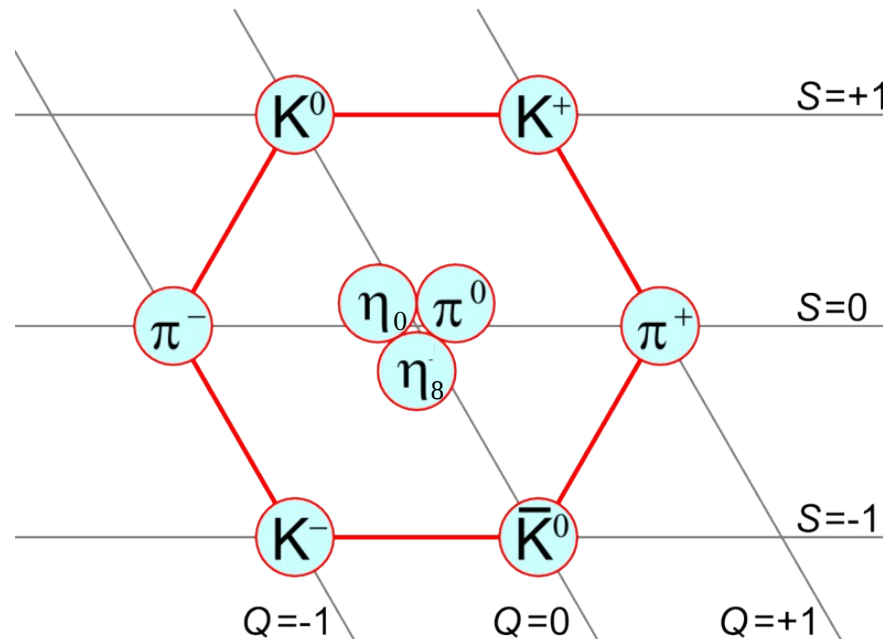
$$L_{\text{QCD}} = \bar{q} (i \not{D} - M) q - \sum_{a=1}^8 \frac{1}{4} G_{\mu\nu,a} G_a^{\mu\nu}$$

- Chiral limit ($m_u = m_d = m_s = 0$):

$$U(3)_L \times U(3)_R = SU(3)_L \times SU(3)_R \times U(1)_V \times U(1)_A \text{ symmetry}$$

Hadrons do not come in parity doublets
 → Chiral symmetry must be broken (spontaneously)

- $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V$ gives rise to 8 massless, pseudoscalar Goldstone bosons



Explicit Symmetry Breaking

Quarks have finite masses

- SU(3) flavor symmetry: $m_u = m_d = m_s \neq 0$
- SU(2) isospin symmetry: $m_u = m_d \neq m_s$
- Isospin breaking: $m_u \neq m_d$
- Electromagnetic effects also break isospin symmetry

Using: $\eta \rightarrow 3\pi$, $\eta' \rightarrow 3\pi$; $\eta' \rightarrow 2\pi\eta$

Extract:
$$Q^2 = \frac{m_s^2 - \hat{m}^2}{m_d^2 - m_u^2} \quad \hat{m} = \frac{m_u + m_d}{2}$$

η/η' mixing

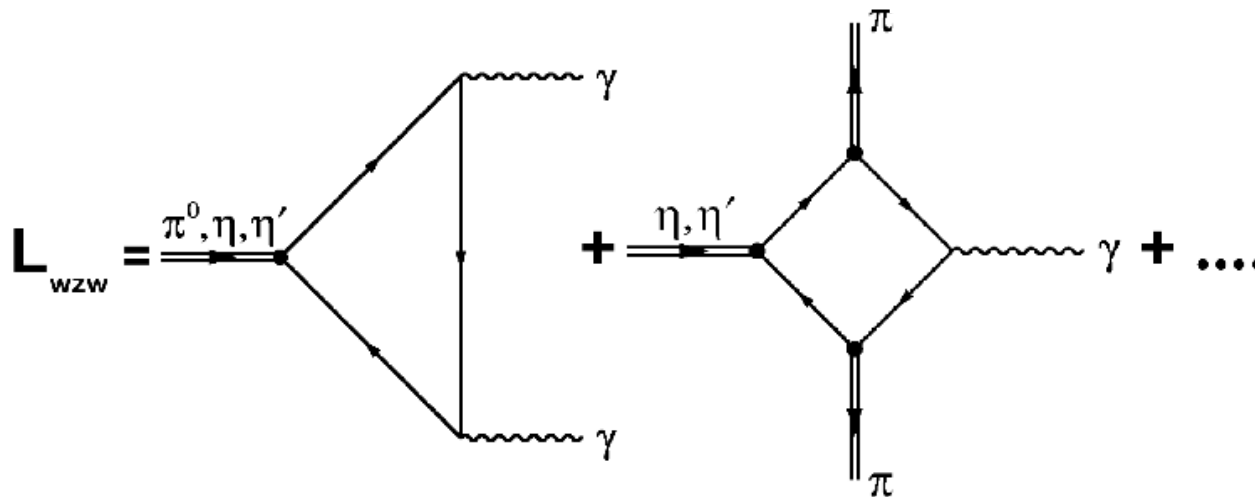
η and η' are admixtures of pure SU(3) singlet and octet states

$$\eta = \eta_0 \sin\theta - \eta_8 \cos\theta$$

$$\eta' = \eta_0 \cos\theta + \eta_8 \sin\theta$$

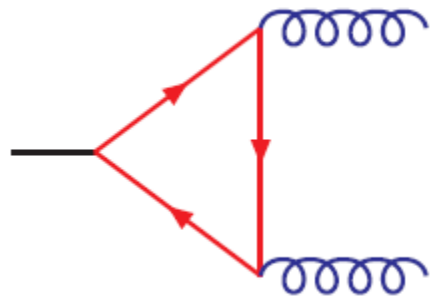
$$\eta/\eta': I^G(J^P C) = 0^+(0^- +)$$

- Mixing caused by SU(3) breaking due to strange quark mass AND the chiral anomaly
- Beyond leading-order single mixing angle not sufficient, possible gluonium content



$U(1)_A$ Anomaly

- Quantum fluctuations destroy singlet axial-vector current conservation



The diagram shows a quark loop (red lines) with two gluon insertions (blue wavy lines). An arrow points from the diagram to the equation below.

$$\partial_\mu A^{0\mu} = 2\sqrt{N_C} \omega = \frac{2\sqrt{N_C}}{16\pi^2} \varepsilon^{\mu\nu\alpha\beta} \text{tr} G_{\mu\nu} G_{\alpha\beta} \neq 0$$

- Why is the η' so heavy?
- ω -term includes gluons \rightarrow strongly interacting $\rightarrow \eta'$ heavy
- Applicability of χ PT to η' ? (chiral symmetry breaking scale: $4\pi f_\pi \approx 1.2$ GeV, η' as a Goldstone boson) (theory)

CP-Violation in SM

CP-violation in SM: quark mass eigenstates are different from weak eigenstates:

→ quark mixing matrix (Cabibbo, Kobayashi, Maskawa)

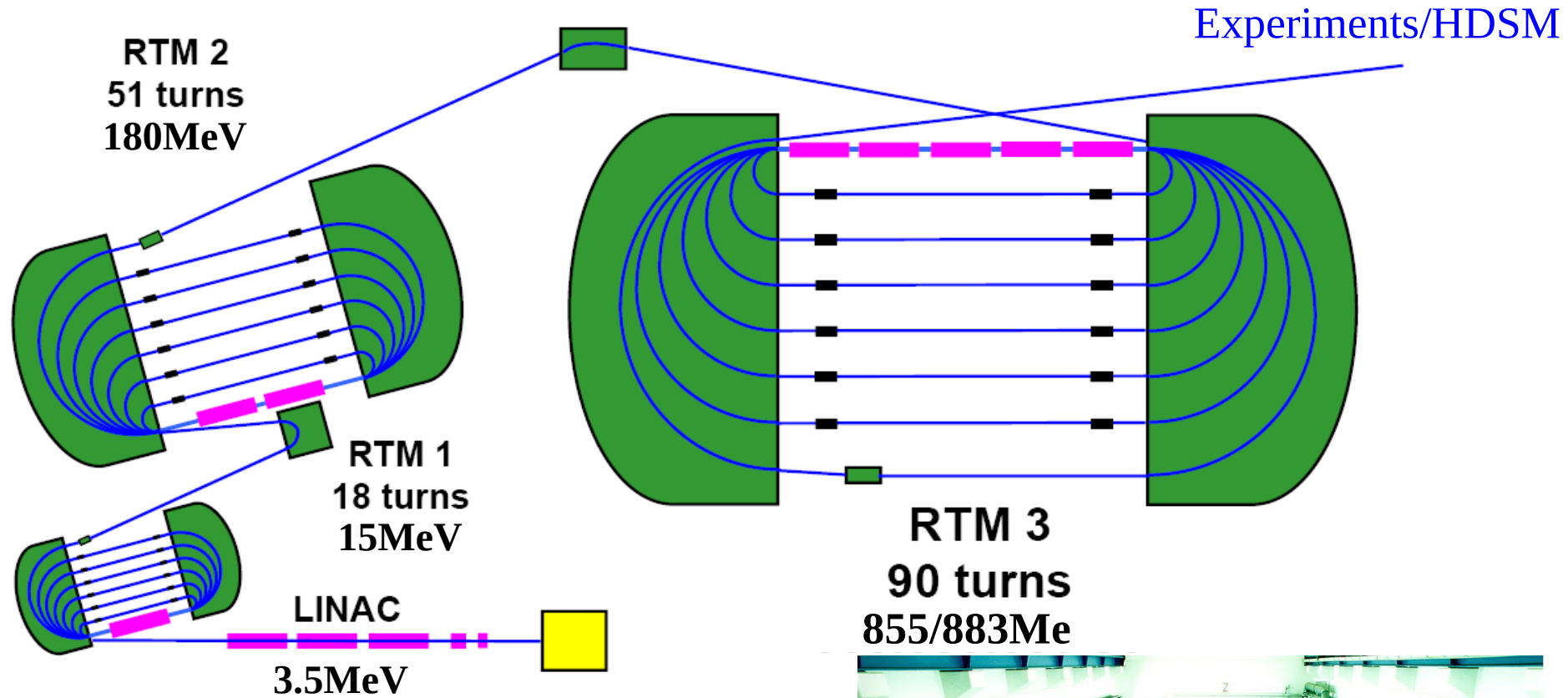
→ different mixing matrices for quarks and antiquarks → CP-violation

CKM-matrix complex and unitary → 4 parameters (e.g. 3 angles and one phase)

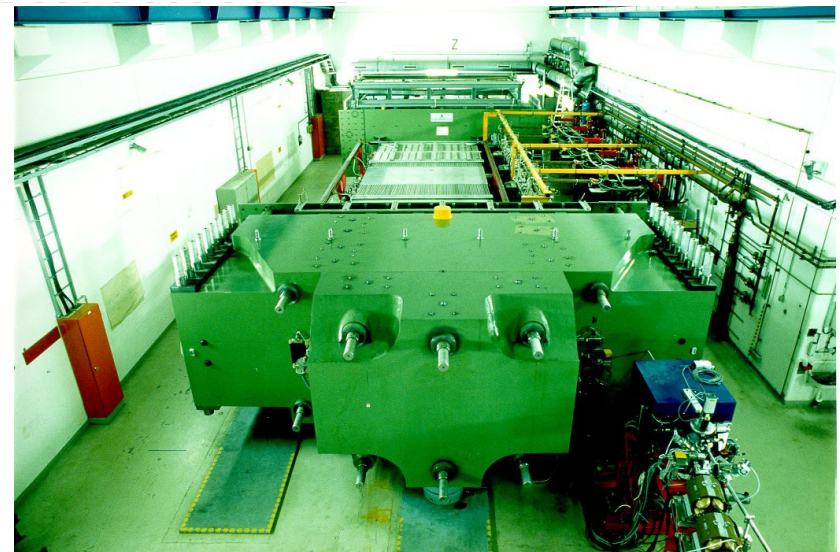
Single phase in CKM-matrix responsible for CP-violation

	weak states	<u>CKM matrix</u>	mass states
Quarks	$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}$	$= \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$	$\begin{pmatrix} d \\ s \\ b \end{pmatrix}$
Anti-quarks	$\begin{pmatrix} \bar{d}' \\ \bar{s}' \\ \bar{b}' \end{pmatrix}$	$= \begin{pmatrix} V_{ud}^* & V_{us}^* & V_{ub}^* \\ V_{cd}^* & V_{cs}^* & V_{cb}^* \\ V_{td}^* & V_{ts}^* & V_{tb}^* \end{pmatrix}$	$\begin{pmatrix} \bar{d} \\ \bar{s} \\ \bar{b} \end{pmatrix}$

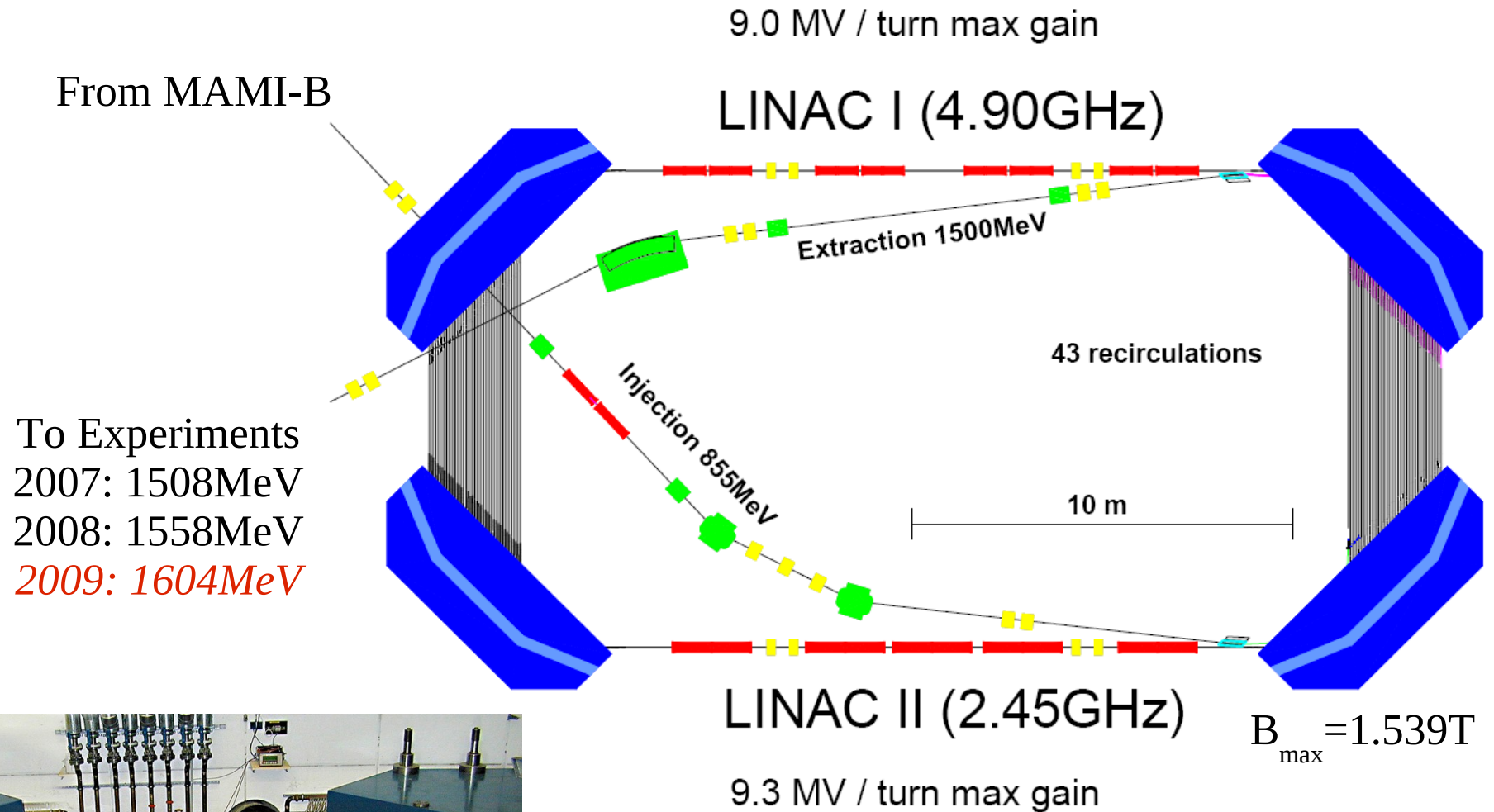
Mainz Microtron (MAMI-B)



Acceleration via em wave (2.45GHz)
cw: bunch structure $\sim 0.4\text{ns}$
Injektion LINAC
3 cascaded Race-Track-Microtrons
Magnet of RTM 3 $\sim 450\text{t}$ per Magnet, 1.28T

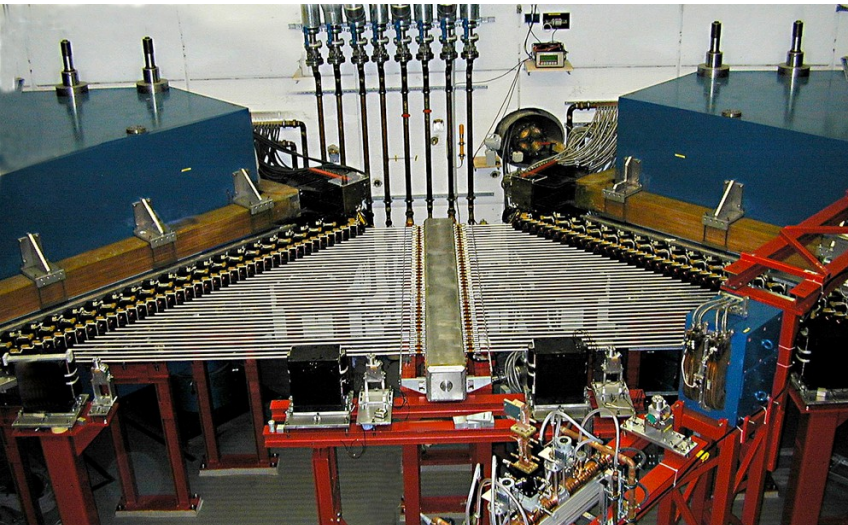


HDSM (MAMI-C)

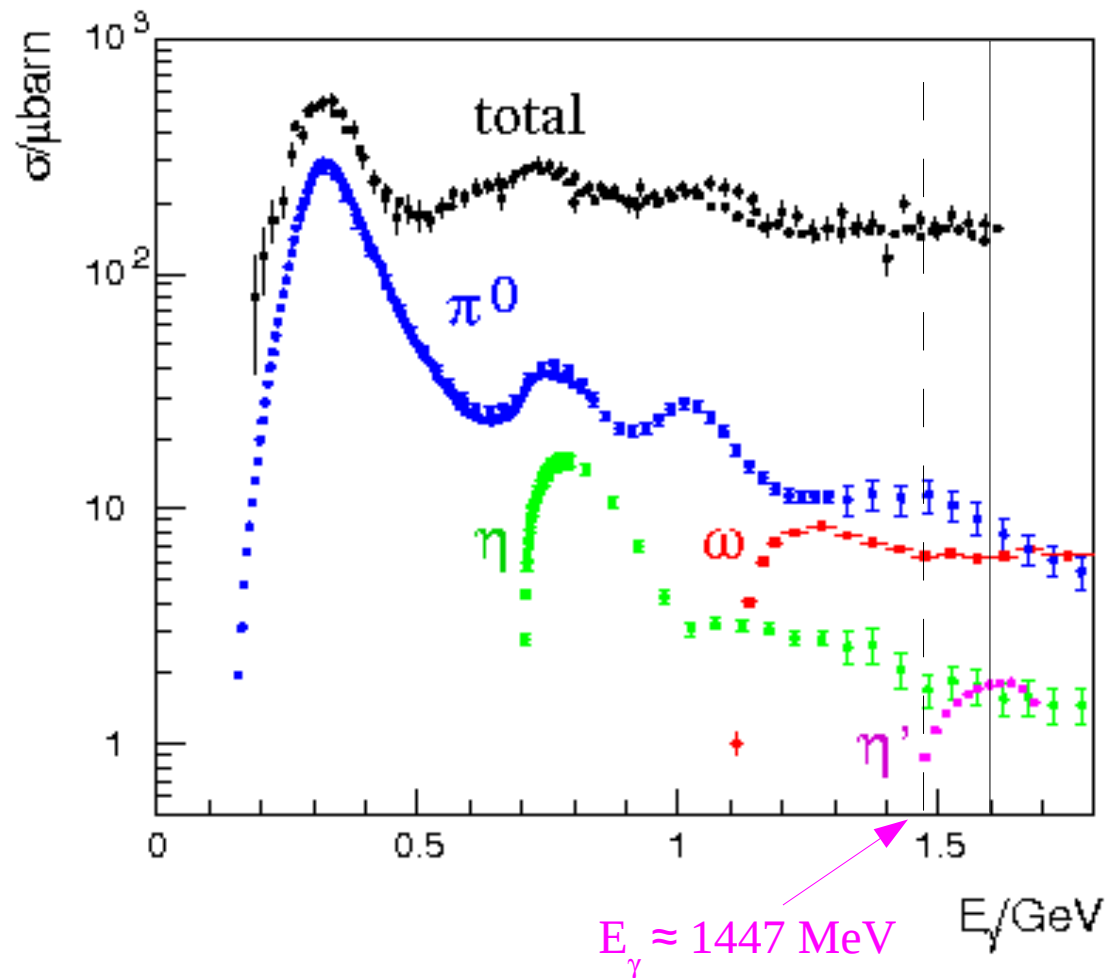
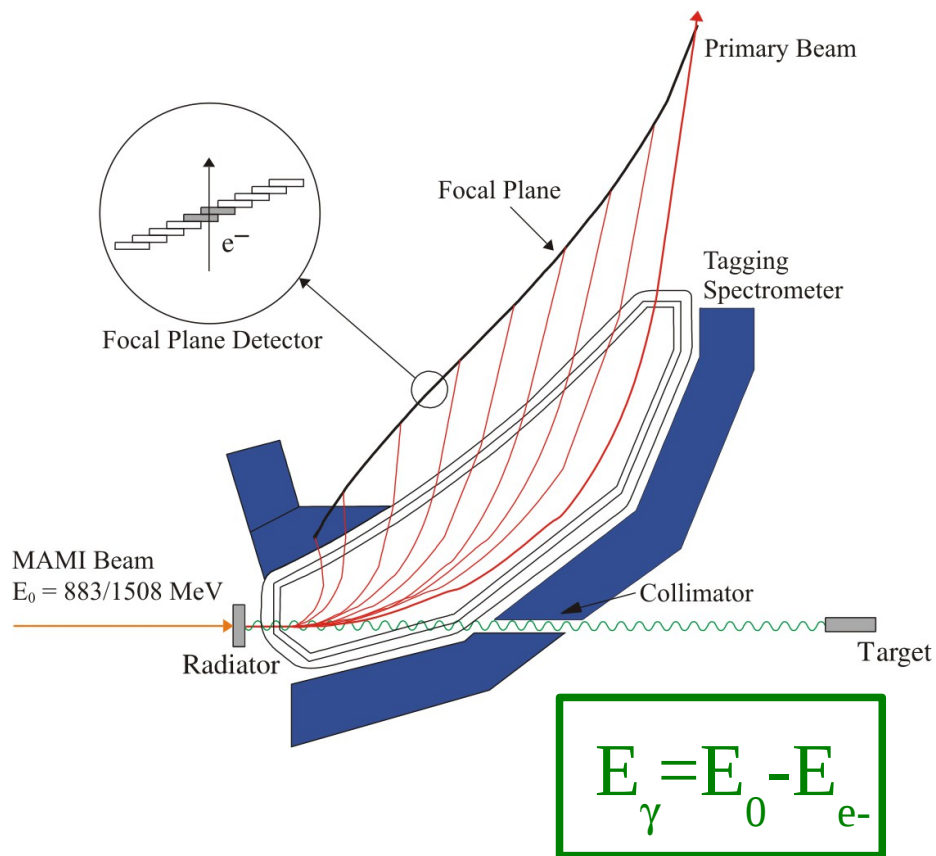


Harmonic Doubled Sided Microtron (HDSM)

K.-H. Kaiser et al., NIM A 593, 159 (2008).



Tagging Spectrometer

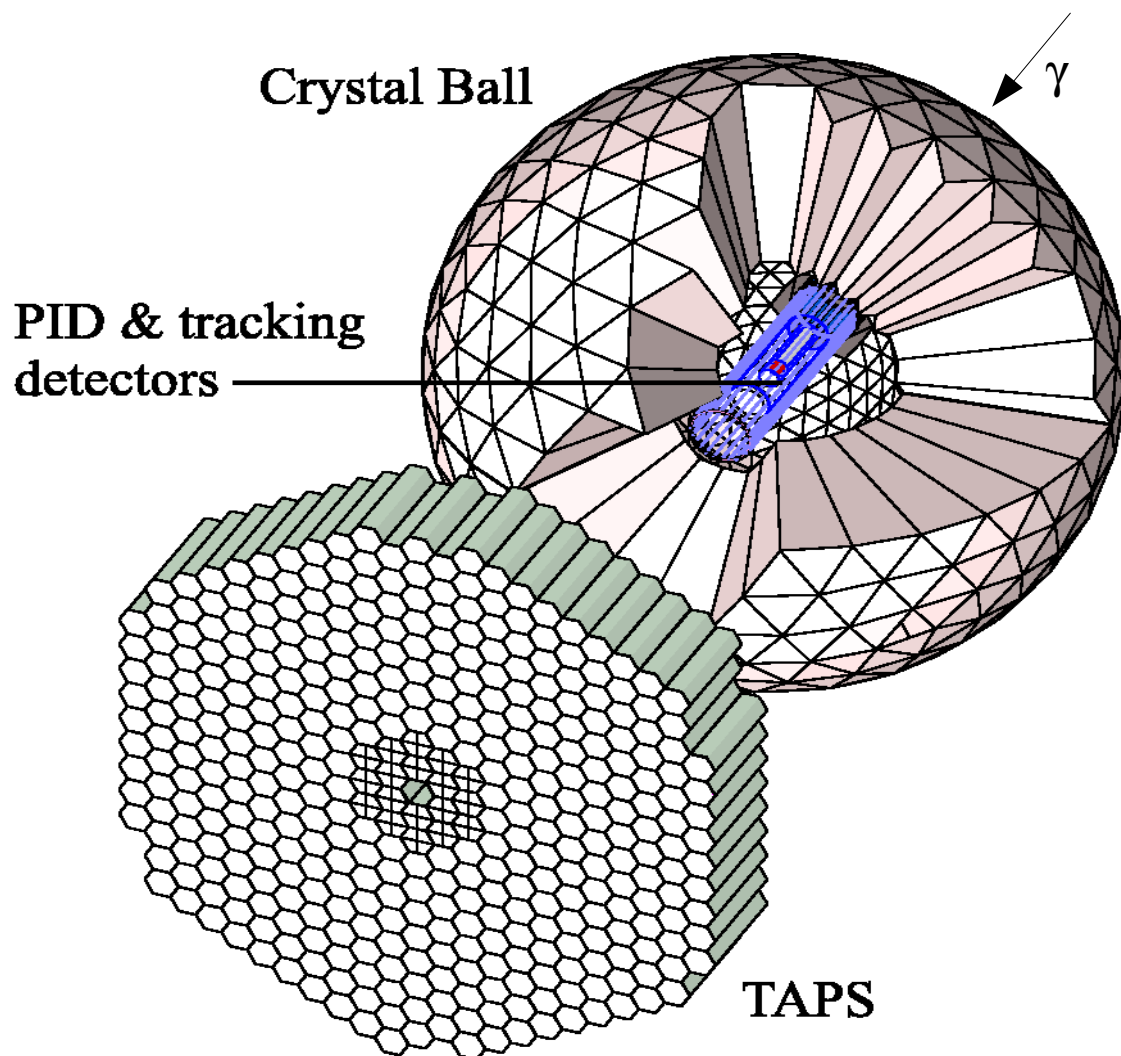


Tagging range: 5.1 to 93% of E_0

Maximum energy tagged for $E_0 = 1604 \text{ MeV}$ is 1491 MeV

→ New tagging device for η' experiments needed!

4 π -Setup



Crystal Ball:

672 NaI(Tl) crystals
93,3% of total solid angle
Each crystal equipped with PMT

$$\frac{\sigma}{E_\gamma} = \frac{2\%}{(E_\gamma/\text{GeV})^{0.25}} \quad \sigma(\theta) = 2^\circ \dots 3^\circ$$
$$\Delta t = 2.5 \text{ ns FWHM} \quad \sigma(\phi) = \frac{2^\circ \dots 3^\circ}{\sin(\theta)}$$

TAPS:

Up to 510 BaF₂ crystals
Polar acceptance: 4-20°

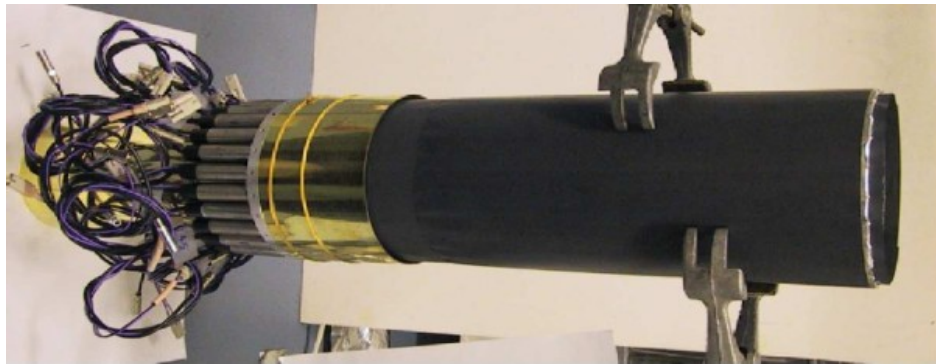
$\Delta t = 0.5 \text{ ns FWHM}$

$$\frac{\sigma}{E_\gamma} = \frac{0,79\%}{\sqrt{E_\gamma/\text{GeV}}} + 1,8\%$$

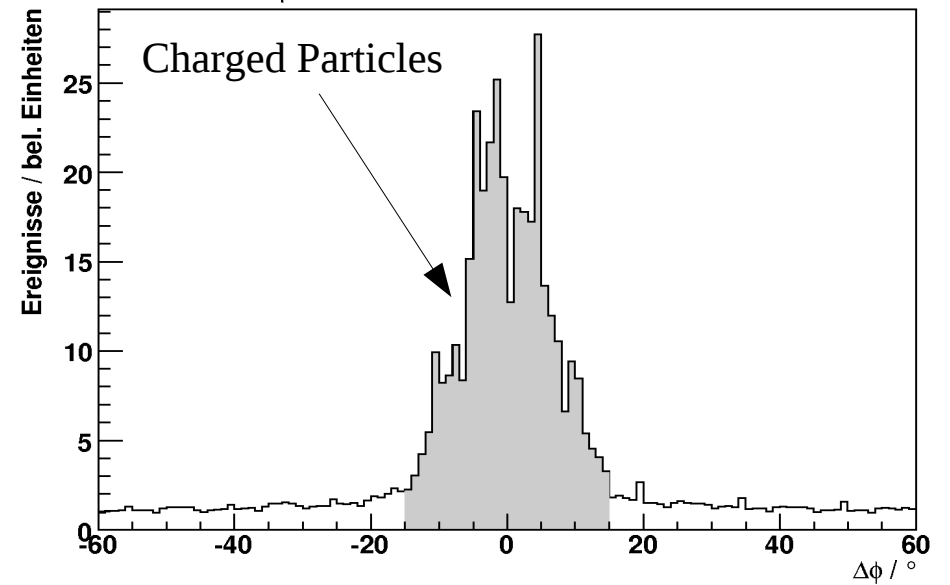
CB PID

Particle Identification Detector (PID):

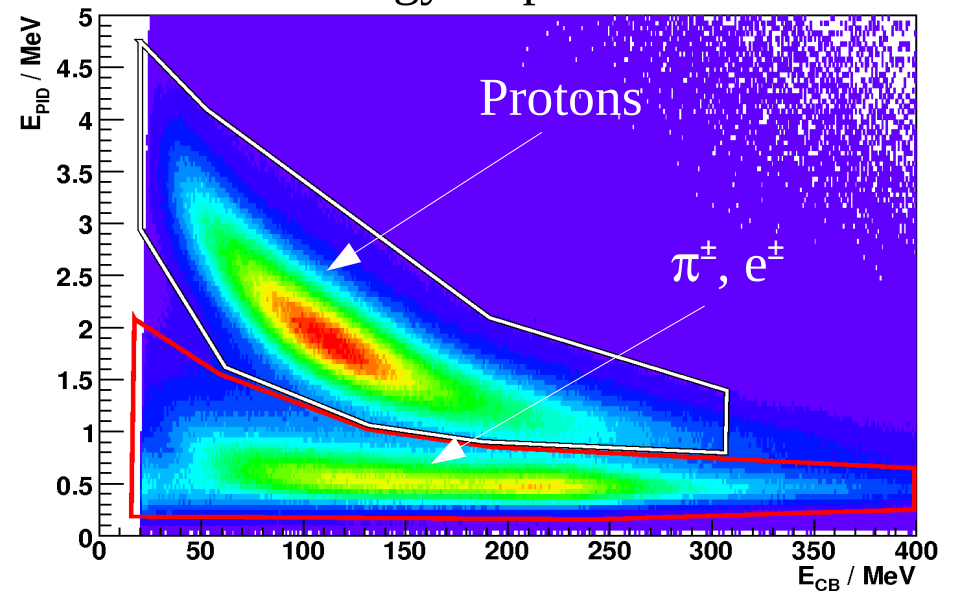
- Cylindrical Detector inside CB
- 24 scintillator strips
- PMT readout



$\Delta\phi$ - between CB and PID

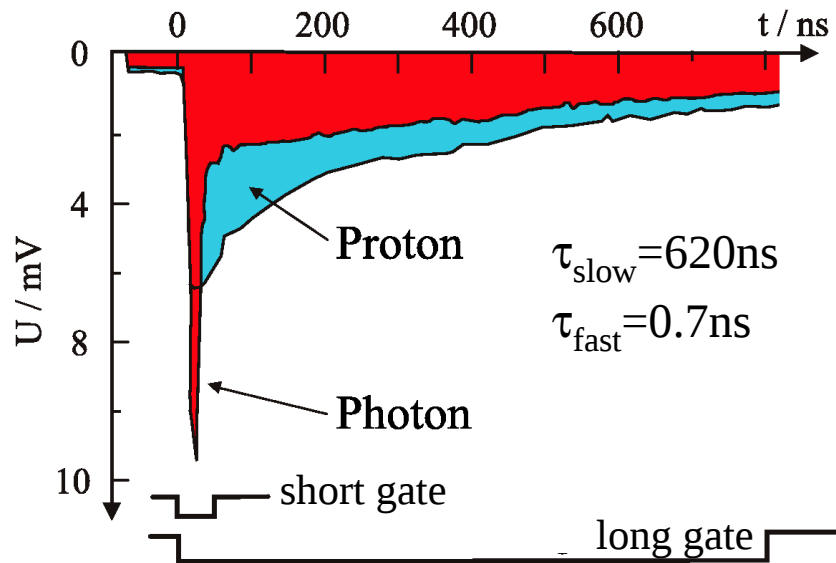
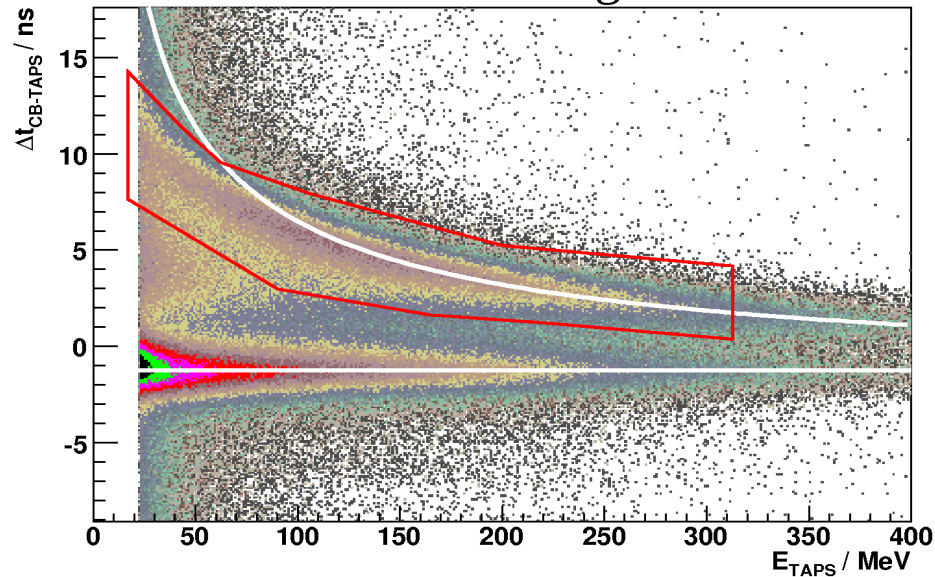


Energy Dependence



TAPS PI

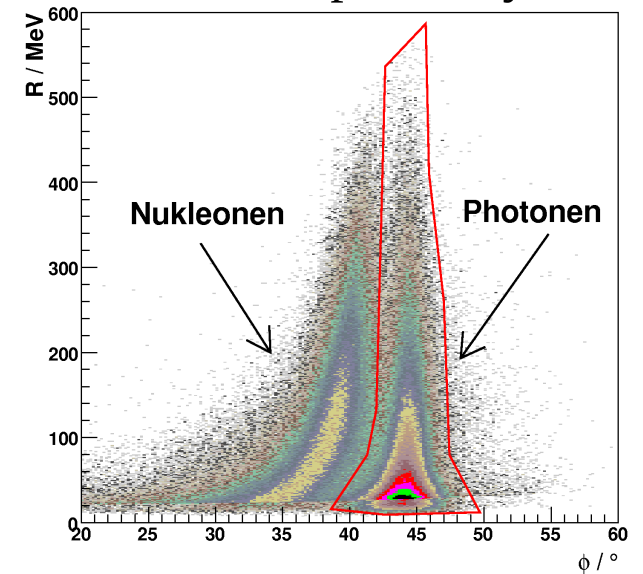
Time-of-Flight



$$R = \sqrt{E_{short}^2 + E_{long}^2}$$

$$\phi = \arctan\left(\frac{E_{short}}{E_{long}}\right)$$

Pulse-Shape-Analysis

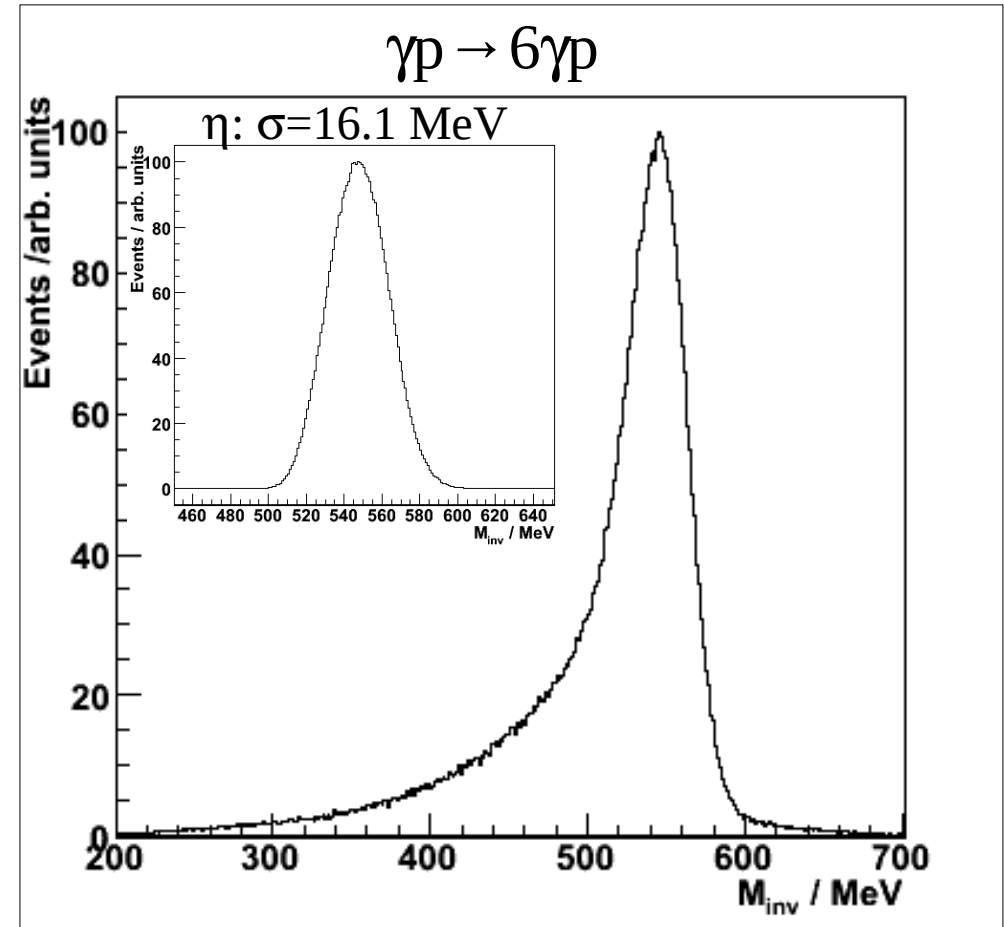
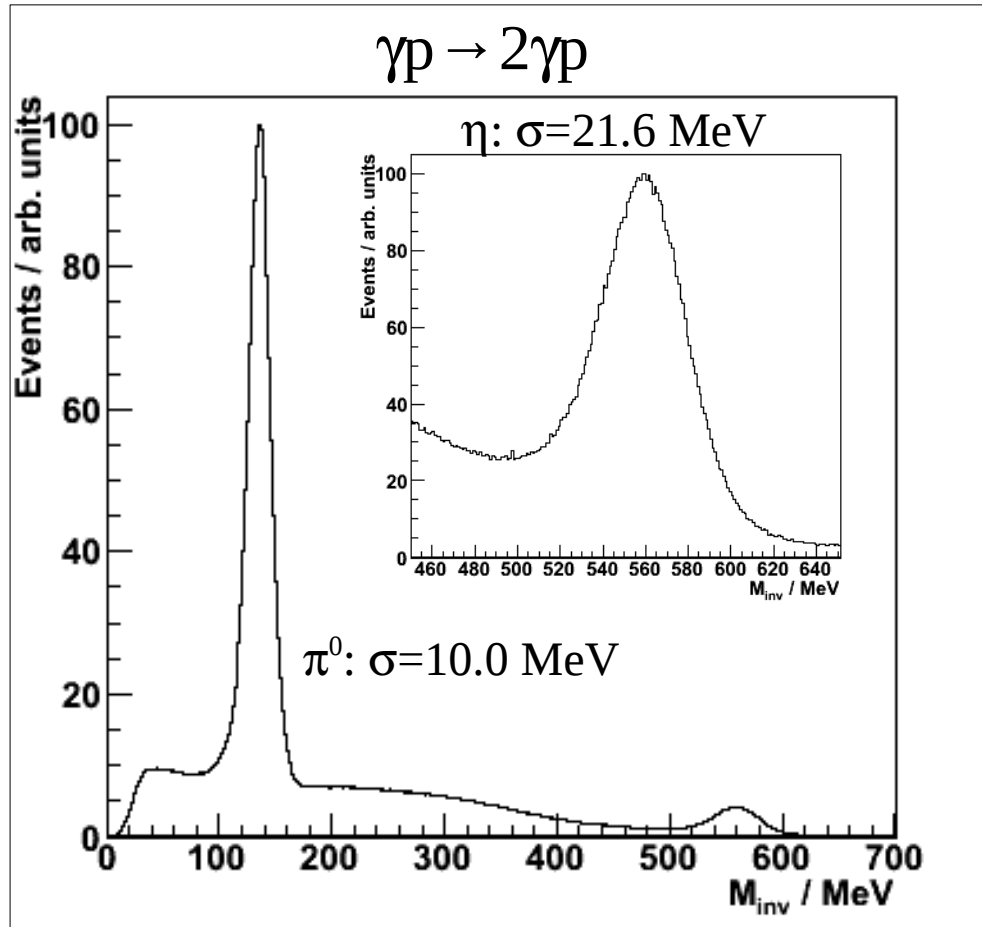


Setup Performance

Two main η decay modes:

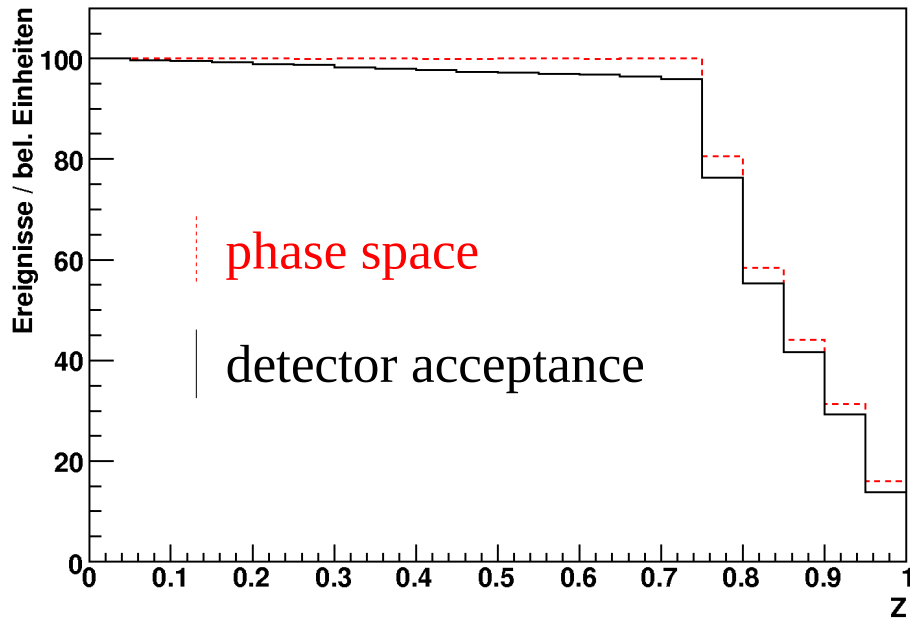
$$\text{BR}(\eta \rightarrow 2\gamma) = 39.38\%$$

$$\text{BR}(\eta \rightarrow 3\pi^0) = 32.51\%$$

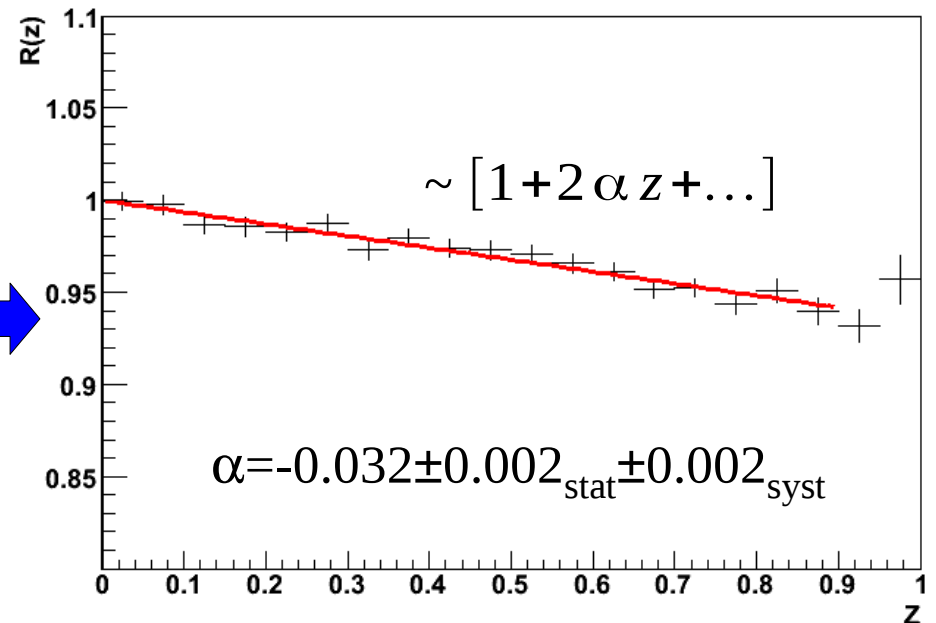
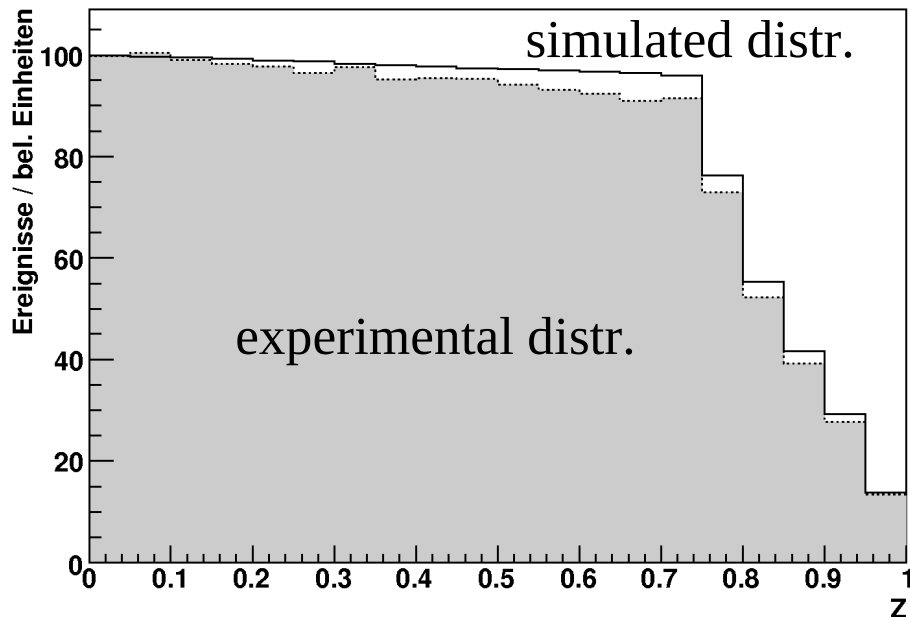


$3 \cdot 10^6 \eta \rightarrow 3\pi^0$ analysed from ~ 6 weeks $\rightarrow 30M \eta$ produced

Result for α



- precise simulation required



Understanding α : order-by-order decomposition

	$\alpha \times 10^{-3}$
	+11.3
	+11.7
	-43.5
	+1.7
	(-5.6)
isospin-breaking effects	-0.6
	-22.2 ± 5.0

- representation up to $\mathcal{O}(a_{\pi\pi}^2 \epsilon^4)$,
partial $\mathcal{O}(a_{\pi\pi}^2 \epsilon^6)$, $\mathcal{O}(a_{\pi\pi}^2 \epsilon^8)$

error: (1) $\pi\pi$ scattering

Ananthanarayan et al. 2001 vs. Kamiński et al. 2008

(2) estimate of higher orders ("bubble resummation")

Understanding α : interpretation of the ChPT result

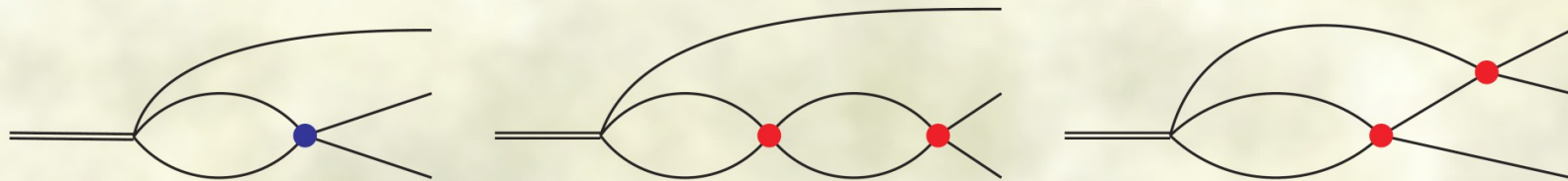
Remember: ChPT at $\mathcal{O}(p^6)$

Bijnens, Ghorbani 2007

$$\alpha_{\text{ChPT}} = (13 \pm 32) \times 10^{-3} \quad \text{vs.} \quad \alpha_{\text{NREFT}} = (-22.2 \pm 5.0) \times 10^{-3}$$

- Why the difference?

Emulate ChPT $\mathcal{O}(p^6)$ calculation:



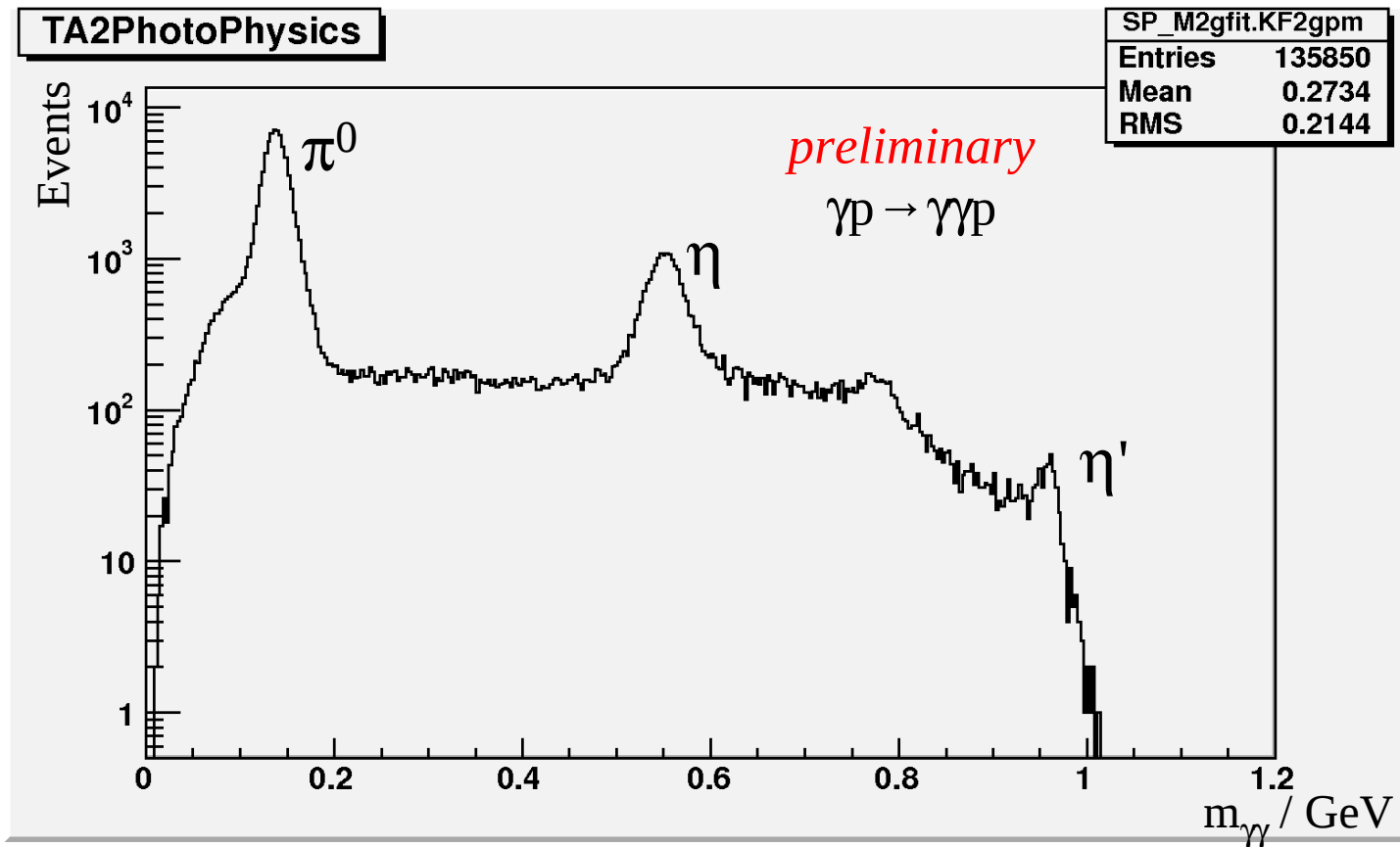
- rescattering parameters at $\mathcal{O}(p^4)$ in one-loop graphs
- rescattering parameters at $\mathcal{O}(p^2)$ in two-loop graphs ($a_0^0 = 0.16, \dots$)

Result:

- we find $\alpha = (-0.7 \times 10^{-3})$
 \Rightarrow “weaker” rescattering leads to completely different result!

η' Production

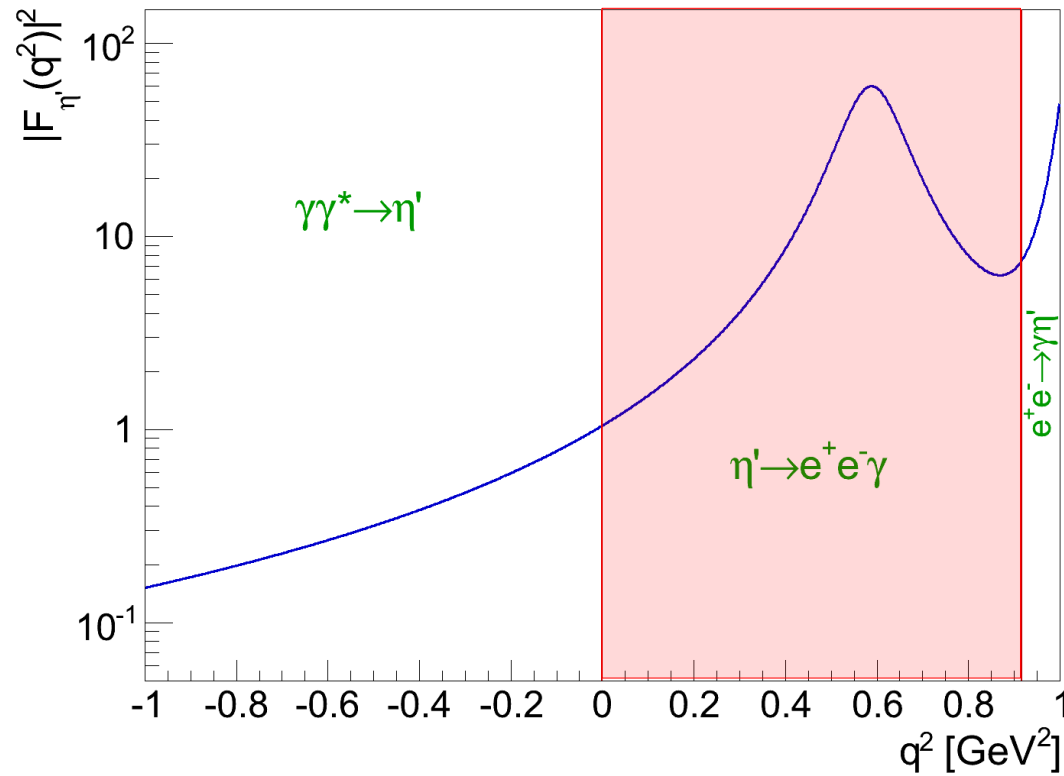
- Installation EPT fall 2011
- First test run December 2011
- **First test/production measurement successful in March 2012!**
- **η' production runs (each 2,5 weeks) successful May/August 2012!**



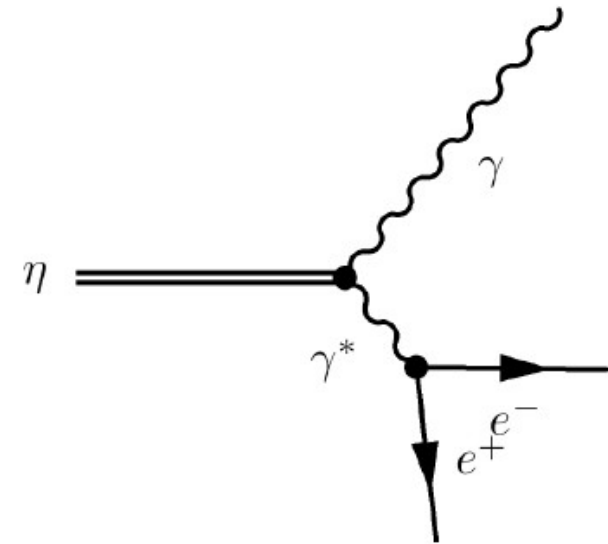
Only small part of available statistics

S. Prakhov (UCLA)

Time-like TFF at MAMI



$q^2 = (\Delta E/c)^2 - \Delta p^2 = m_1^2$
 momentum transfer carried
 by virtual photon



Time-like momentum transfer (meson decays):

- $(2m_1)^2 < q^2 < M^2$
- Crystal Ball, WASA, KLOE, Crystal Barrel, BESIII, CLAS

$$\frac{d\Gamma(P \rightarrow e^+e^-\gamma)}{dm \Gamma(P \rightarrow \gamma\gamma)} = \frac{4\alpha}{3\pi m} \sqrt{1 - \frac{4m_e^2}{m^2}} \left(1 + \frac{2m_e^2}{m^2}\right) \left[1 - \frac{m^2}{m_P^2}\right]^3 |F(q^2)|^2$$

- Also $\mu^+\mu^-\gamma$ decays possible: NA60

Setup Upgrades?

- Old trigger scheme replaced by **FPGA based trigger module**
 - **Triggerless readout** (TRB boards)? (A. Neiser, W. Gradl)
 - Branching fractions: **trigger detector** under construction (M. Hillenbrand, M. Ostrick)
 - Charged decays e.g. $\eta \rightarrow \pi^+\pi^-\gamma(\gamma)$ need dedicated **tracking detector**
 - High resolution **forward tracking system**?
 - **New detector setup**?
- Development of **high-rate TPC with?**
Complete new setup?

